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SH - A COMPUTER PROGRAM FOR GENERATING FAR-FIELD TANGENTIAL TIME HISTORIES FOR POINT EARTHQUAKE SOURCES

BY

ROBERT B. HERRMANN AND CHIEN Y. WANG

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DEPARTMENT OF EARTH AND ATMOSPHERIC SCIENCES SAINT LOUIS UNIVERSITY 221 NORTH GRAND BOULEVARD SAINT LOUIS, MISSOURI 63103

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ABSTRACT

A computer program is presented for the computation of far-field tangential time histories due to point earthquake sources. The program provides accurate results for frequencies of 0-10 Hz and for receiver distances from one source depth to 500 kilometers. Comparisons are made with an independent half-space solution to test the validity of the far-field assumption in representing time histories.

A package of four computer programs is given: SHSPEC yields Fourier spectra on the surface of a multilayered medium at a specified distance from the point dislocation earthquake source; SHVEL combines the output of SHSPEC with a predetermined source pulse to generate velocity time histories; DSVLAC uses the output of SHVEL to generate displacement, velocity and acceleration time histories; and SDSVSA uses the output of DSVLAC to compute and tabulate the response spectra of each time history.

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PART I. INTRODUCTION

This report is an update of a publication by Herrmann (1977) for the U.S. Army Corps of Engineers. Since that time, there have been many advances in techniques for generating realistic earthquake ground motion time histories. At present, developments are being pursued with two approaches involving Laplace transform and Fourier transform techniques.

The Laplace transform, or Cagniard-de Hoop technique consists of generalized ray techniques, by which the seismic trace is constructed by a superposition of seismic arrivals which have taken separate paths between the earthquake source and receiver. An advantage is that the method is valid at high frequencies. Unfortunately, for large distances in a reasonable earth model, the number of rays contributing to the time history becomes very large so that considerable effort is involved in keeping track of the rays as well as computing them.

Helmberger and Malone (1975) applied the method to a study of local earthquakes. Heaton and Helmberger (1977, 1978) used the method to model the displacement time histories obtained from integrated accelerograms of the Borrego Mountain and Brawley earthquakes. To a certain extent, the earth model was a variable which could be modified under constraints to obtain a better fit to the data. However, good fits were obtained, demonstrating the effect of the transmission medium upon the ground displacements.

Displacements, rather than velocities or accelerations were modeled since lateral heterogeneities in the earth structure should affect the lower frequency displacements less.

The other approach involves expressing the solution in terms of a double integral transformation over wave number and frequency (Haskell, 1964; Hudson, 1969). This method does not consider the contribution of individual seismic arrivals, but rather yields the complete solution for an arbitrarily layered halfspace. A drawback is some difficulty encountered at high frequencies. On the other hand the complete solution is found.

The numerical solution is complicated by the presence of singularities in the wavenumber integrand. For an elastic medium, branch points and poles in the complex wavenumber plane are encountered. The solution may be obtained by a numerical approach to contour integration (Herrmann, 1977; Herrmann, 1979), or the by artifice of using slightly complex angular frequency to shift the complex singularities from the axis of integration (Bouchon and Aki, 1977). If an anelastic medium is considered, the singularities no longer lie on the real k-axis, so integration may procede simply. This is quite realistic since the earth is not perfectly elastic, so one assumes this from the start (Apsel, 1977).

The approach taken here is to expand Herrmann (1977, 1979) in detail because it is an independent method and because previous studies by Nuttli (1973, 1978) have indicated a very low rate of

anelastic attenuation in the central United States. The method of Herrmann (1977) handles these conditions well.

PART II. THEORY

Haskell (1964) and Hudson (1969) obtained the solution for displacements generated by an elementary point force in the m'th layer of a structure consisting of plane parallel layers overlying a uniform halfspace. Each layer is homogeneous and isotropic with compressional wave velocity α_k , shear wave velocity β_k and density ρ_k (k = 1, N). The N'th layer corresponds to the halfspace. A cylindrical coordinate system (r, ϕ , z) is used with origin at the free surface above the source, with z-axis taken positive downward. The layer interfaces are the planes $z=z_k$ (k=1, 2, ..., N-1) and the source is located on the plane $z=z_m + h_m$. For the purpose of derivation, the source is required to lie in a layer above the halfspace.

The expressions for the Fourier transformed displacements at the free surface z=0 are the following;

$$\overline{u}_{z} (\mathbf{r}, \phi, 0, \omega) = \sum_{n=0}^{\infty} \int_{0}^{\infty} d\mathbf{k} \{g_{z}^{nc} \cos n\phi + g_{z}^{ns} \sin n\phi\} J_{n}(\mathbf{k}\mathbf{r})/F_{R}\}$$

$$\overline{u}_{r} (\mathbf{r}, \phi, 0, \omega) = \sum_{n=0}^{\infty} \int_{0}^{\infty} d\mathbf{k} \{g_{r}^{nc} \cos n\phi + g_{r}^{ns} \sin n\phi\} kJ_{n-1} (\mathbf{k}\mathbf{r})/F_{R}$$

$$- (n/r) (g_{r}^{nc} \cos n\phi + g_{r}^{ns} \sin n\phi) J_{n} (\mathbf{k}\mathbf{r})/F_{R} \qquad (1)$$

$$- (n/r) (g_{\phi}^{nc} \cos n\phi + g_{\phi}^{ns} \sin n\phi) J_{n}(kr)/F_{L}$$

$$\overline{u}_{\phi}(r,\phi,0,\omega) = -\sum_{n=0}^{\infty} \int_{0}^{\infty} dk \{g_{\phi}^{ns} \cos n\phi - g_{\phi}^{nc} \sin n\phi) k J_{n-1}(kr)/F_{L}$$

$$-(n/r) (g_{\phi}^{ns} \cos n\phi - g_{\phi}^{nc} \sin n\phi) J_{n}(kr)/F_{L}$$

$$-(n/r) (g_{r}^{ns} \cos n\phi - g_{r}^{nc} \sin n\phi) J_{n}(kr)/F_{R}$$

The displacements are defined such that the vertical displacement $u_z(r,\phi,0,t)$ is positive downward, that the radial displacement $u_r(r,\phi,0,t)$ is positive in a direction away from the source, and that the tangential displacement $u_{\phi}(r,\phi,0,t)$ is positive in a clockwise direction when looking in the positive z-direction.

Since this report is concerned with far-field tangential time histories, SH, explicit expressions for the P-SV functions g_z , g_r and F_R are not given here (c.f. Haskell, 1964). The expressions for the SH functions are as follow:

$$g_{\phi}^{nc} = (L_{21} - L_{11})S_{1}^{nc} + (L_{22} - L_{12})S_{2}^{nc}$$

$$g_{\phi}^{ns} = (L_{21} - L_{11})S_{1}^{ns} + (L_{22} - L_{12})S_{2}^{ns}$$
(2)

and

$$F_{L} = J_{11} - J_{21}$$

where L_{ij} and J_{ij} are the elements of the L and J matrices which are

defined as the matrix products.

$$J = E_{N}^{-1} A_{N-1} (d_{N-1}) ... A_{1} (d_{1})$$

$$L = E_{N}^{-1} A_{N-1} (d_{N-1}) ... A_{m+1} (d_{m+1}) D_{m} (d_{m} - h_{m}).$$
(3)

The layer matrices of Equation 3 are defined as

$$\mathbf{E}_{N}^{-1} = \begin{bmatrix} \rho_{N} v_{\beta_{N}} & 0\\ 0 & -1/\beta_{N}^{2} \end{bmatrix}, \qquad (4)$$

$$A(z) = \begin{bmatrix} c_{\beta} & s_{\beta} \gamma \rho \beta v_{\beta} \\ \rho \beta^{2} v_{\beta} s_{\beta} & c_{\beta} \end{bmatrix}$$
(5)

and

$$D(z) = \begin{bmatrix} C_{\beta} / \rho & -S_{\beta} / \rho v_{\beta} \\ 2 & \beta v_{\beta} S_{\beta} & -\beta C_{\beta} \end{bmatrix}, \qquad (6)$$

where $C_{\beta}(z) = \cosh v_{\beta} z$, $S_{\beta}(z) = \sinh v_{\beta} z$, $k_{\beta} = \omega/\beta$,

and

$$v_{\beta} = \begin{cases} (k^{2} - k_{\beta}^{2})^{1/2} & k \ge k_{\beta} \\ i(k_{\beta}^{2} - k^{2})^{1/2} & k \le k_{\beta}. \end{cases}$$
(7)

The elements of the matrices are to be evaluated using the layer parameters indicated by the matrix subscripts in Equation 3.

For a point shear dislocation model of an earthquake source, the source can be represented by two perpendicular dipoles. Let the orientation of the pressure and tension axes be given by the vectors $P = (p_1, p_2, p_3)$ and $T = (t_1, t_2, t_3)$, respectively. The source coefficients S_i^{nc} and S_i^{ns} are all zero except for the terms

$$s_{1}^{1c} = -2 (t_{1} t_{3} - p_{1} p_{3})/4\pi\beta_{m}^{2}$$

$$s_{1}^{1s} = -2 (t_{2} t_{3} - p_{2} p_{3})/4\pi\beta_{m}^{2}$$
(8)
$$s_{2}^{2c} = k(t_{2}^{2} - t_{1}^{2} - p_{2}^{2} + p_{1}^{2})/4\pi\beta_{m}^{2}$$

$$s_{2}^{2s} = -2k(t_{1} t_{2} - p_{1} p_{2})/4\pi\beta_{m}^{2},$$

where k is the wavenumber and β_m is the shear velocity in the source layer. The expressions for E_N^{-1} , D and $S_i^{nc,s}$ differ from those given by Haskell (1964) in that they have been modified to eliminate some apparent singularities. The ratio $g^{nc,s}/F_L$ does not differ from that given by Haskell (1964) or Hudson (1969).

A simple examination of the excitation coefficients in Equation 8 shows that the SH contribution to the tangential displacements involves just a linear combination of two equivalent sources, a vertical dip-slip source which has only the n=1 term and a vertical strike-slip source which has only the n=2 term (a 45° dip-slip source is another source which involves just the n=2 term). This well known observation (Langston and Helmberger, 1975 and Harkrider, 1976) means that the tangential displacements from an arbitrary fault motion

model can be represented by a linear combination of the solutions due to these two sources.

A right lateral vertical strike-slip motion on a fault striking north would be represented by P=(.707, .707, 0) and T=(-.707, .707, 0). Reverse faulting on a fault dipping 45° to the east or west and striking north would be represented by P=(0,1,0) and T=(0,0,1). Vertical dip-slip faulting on a fault striking north with the east side downthrown would have P=(0, -.707, .707) and T=(0,.707,.707).

The transformed displacements in Equation 1 represent the displacements due to a delta function time history of motion on the fault. Usually this delta function response is convolved with s(t), the time history of the faulting process of the dislocation source, s(t) = 0 for t<0 and $s(t) = M_0$ for t>>0. The seismic moment M_0 is defined by the relation $M_0 = \mu u A$, where μ is the rigidity modulus of the medium, \bar{u} is the average dislocation and A is the fault area. M_0 has units of dyne-cm in CGS units. The ground motion as a function of time is then obtained by taking the inverse Fourier transform of each transformed displacement in Equation 1. For example,

$$u_{\phi}(r,\phi,o,t) = (2\pi)^{-1} \int_{-\infty}^{\infty} s(\omega) \overline{u}_{\phi}(r,\phi,o,\omega) \exp(i\omega t) d\omega$$
(9)

where $s(\omega)$ is the Fourier transform of s(t).

Contour Integration

For a perfectly elastic medium, the evaluation of the wave number integrals of Equation 1 is complicated by complex singularities along the real k-axis. The integrals to be evaluated are of the form

$$F(\mathbf{r},\omega) = \int_{0}^{\infty} f(\mathbf{k},\omega) J_{n}(\mathbf{k}\mathbf{r})d\mathbf{k}, \qquad (10)$$

where the function $f(k,\omega)$ has poles and branch points k_{α_N} and k_{β_N} along the real k-axis. The SH functions $g_{\phi}^{nc,s}$ and F_L do not have the k_{α_N} branch point because of the absence of the ν_{α_N} term in Equations 4, 5 and 6. Following Ewing, Jardetzky and Press (1957), branch cuts are taken along the negative imaginary k-axis [-i ∞ , 0] and along the real k-axis [0, k_{β_N}].

Expressing the Bessel function as a sum of Hankel functions of the first and second kinds, performing contour integration in the first and fourth quadrants of the complex k-plane, $\xi = k + i\tau$, it is not difficult to show that Equation 10 becomes

$$F(\mathbf{r},\omega) = \frac{1}{2} \int_{0}^{k} \beta_{N} [f_{+}(\mathbf{k},\omega) - f_{-}(\mathbf{k},\omega)] H_{n}^{(2)}(\mathbf{k}\mathbf{r}) d\mathbf{k}$$
$$-\pi \mathbf{i} \sum \operatorname{Res} f(\mathbf{k},\omega) H_{n}^{(2)}(\mathbf{k}\mathbf{r}) \qquad (11)$$
$$+(1/\pi) \int_{0}^{\infty} [f_{+}(\mathbf{i}\tau,\omega) \exp(-\mathbf{i}n\pi/2)]$$
$$+f_{-}(-\mathbf{i}\tau,\omega) \exp(\mathbf{i}n\pi/2)] K_{n}(\tau\mathbf{r}) d\tau,$$

where $K_n(z)$ is the modified Bessel function. The + or - subscripts indicate that Im ν_{α_N} , $\nu_{\beta_N} > 0$ or that Im ν_{α_N} , $\nu_{\beta_N} < 0$

respectively, be used to evaluate the expression for $f(k,\omega)$. Equation 11 contains the contributions of a real axis branch line integral, the surface wave poles and the imaginary axis branch line integral. This expression can be used for P-SV terms as well as for SH terms since the two real axis branch line integrals can be combined into one in the case of P-SV functions if one is not interested in evaluating the individual contributions of each branch line integral.

PART III: NUMERICAL TECHNIQUES

Contour Integration

Since both the Hankel function and modified Bessel function are undefined for zero argument, there are some inherent limitations in evaluating Equation 10, even before the problems of numerical integration are introduced. Following Fuchs and Muller (1971) the real axis branch line integral is evaluated using the transformation k = $k_{\beta_N} \sin \gamma, \gamma = [0, \pi/2]$. The real-axis branch line integral is now of the form

$$k_{\beta_{N}} \int_{0}^{\pi/2} g(k_{\beta_{N}} \sin \gamma,) H_{n}^{(2)}(k_{\beta_{N}} \sin \gamma r) \cos \gamma d\gamma, \qquad (12)$$

where

$$g(\mathbf{x},\omega) = \frac{1}{2} \left[f_{+}(\mathbf{x},\omega) - f_{-}(\mathbf{x},\omega) \right].$$

The reason for this transformation is that it permits the evaluation of the Sommerfeld integral, which is basic to the wave propagation problem. A trapezoidal rule can be used to evaluate Equation 12, but such a rule becomes inefficient at large distances and high frequencies due to the rapidly oscillating nature of the Hankel function and the $g(x,\omega)$ term. To address this problem, it is assumed that a $\Delta\gamma$ be chosen such that $g(x,\omega)$ varies slowly enough over the range $[\gamma, \gamma + \Delta\gamma]$ that it can be approximated by linear segments. The integral of Equation 12 is now

$$k_{\beta_{N}} \sum_{i=1}^{M} \int_{\gamma_{i}}^{\gamma_{i+1}} \left[(A_{i} + B_{i}(\gamma - \gamma_{i})) \right] H_{n}^{(2)}(k_{\beta_{N}} r \sin \gamma) d\gamma, \qquad (13)$$

where

$$\gamma_i = (i-1)\Delta\gamma$$
 and $\Delta\gamma = (\pi/2M)$.

To evaluate Equation 13, a tabulated integral of the Hankel function from Abramowitz and Stegun (1964) is used together with recurrence relations of the Hankel functions. Define

$$h(x) = \int_{0}^{x} H_{0}^{(2)}(z) dz, \qquad (14)$$

where the integral can be expressed in terms of Hankel functions and Struve functions (Abramowitz and Stegun, 1964). The following are indefinite integrals of the Hankel functions which are of use in this study:

$$\int H_{0}^{(2)}(z) dz = h(z)$$

$$\int z H_{0}^{(2)}(z) dz = z H_{1}^{(2)}(z)$$

$$\int H_{1}^{(2)}(z) dz = - H_{0}^{(2)}(z)$$

$$\int z H_{1}^{(2)}(z) dz = - z H_{0}^{(2)}(z) + h(z)$$

$$\int H_{2}^{(2)}(z) dz = - 2 H_{1}^{(2)}(z) + h(z)$$

$$\int z H_{2}^{(2)}(z) dz = - 2 H_{0}^{(2)}(z) - z H_{1}^{(2)}(z) .$$
(15)

It can be shown that

$$\int_{\gamma_{i}}^{\gamma_{i}+\Delta\gamma} [A_{i} + B_{i}(\gamma-\gamma_{i})] H_{n}^{(2)}(k_{\beta_{N}}r \sin \gamma) d\gamma$$

$$= \int_{N}^{k_{\beta_{N}}r \sin(\gamma_{i}+\Delta\gamma)} [C_{i} + D_{i}(t-t_{i})] H_{n}^{(2)}(t) dt$$

$$= \int_{k_{\beta_{N}}r \sin(\gamma_{i})}^{k_{\beta_{N}}r \sin(\gamma_{i}+\Delta\gamma)} [C_{i} + D_{i}(t-t_{i})] H_{n}^{(2)}(t) dt$$

$$= (C_{i} - D_{i}t_{i}) [h(t)_{i+1}) - h(t_{i})]$$

+ $D_{i} [t_{i+1} H_{1}^{(2)} (t_{i+1}) - t_{i}H_{1}^{(2)} (t_{i})] \text{ for } n=0$

and

$$= - C_{i} [H_{o}^{(2)} (t_{i+1}) - H_{o}^{(2)} (t_{i})] + D_{i} [h(t_{i+1}) - h(t_{i}) - (t_{i+1} - t_{i}) H_{o}^{(2)} (t_{i})]$$

for n=1

(16)

where

$$t_{i} = k_{\beta_{N}} r \sin \gamma_{i}$$

$$t_{i+1} = k_{\beta_{N}} r \sin (\gamma_{i} + \Delta \gamma)$$

$$C_{i} = A_{i} / k_{\beta_{N}} r \cos \gamma_{i}$$

$$D_{i} = B_{i} / (k_{\beta_{N}} r \cos \gamma_{i})^{2}.$$

In evaluating Equation 12, a test is made to determine if it is sufficient to calculate the integral using a trapezoidal rule rather than using Equation 16.

The residue contribution of a function g(z)/h(z) having a simple pole at $z = z_0$ is very simply $g(z_0)/h'(z_0)$, where h'(z) is the first derivative of h(z) with respect to z. The simple poles of Equation 1 arise due to the zeroes of the functions F_R or F_L . The third expression in Equation 11 is an integral of the form

$$\int_{0}^{\infty} G(\tau,\omega) K_{n}(\tau r) d\tau \qquad (17)$$

Since the function $K_n(z)$ decreases in an exponential manner and since it has a singularity at z=o, the use of a Gauss-Laguerre integration rule is suggested if $G(\tau,\omega)$ does not oscillate too rapidly. After a change in variable and some manipulation, application of the Gauss-Laguerre rule yields the following approximation to Equation 17:

$$(1/r) \sum_{\substack{j=1 \\ j=1}}^{m} W_{j} G(x_{j}/r, \omega) \exp(x_{j}) K_{n}(x_{j}), \qquad (18)$$

where x_j and W_j are the abscissas and weights of an m'th order integration rule. Error is introduced due to the oscillatory nature of the function $G(\tau, \omega)$. However, this can be mitigated by using a very high order rule, so that the abscissas are spaced closely enough to sample the oscillations of $G(\tau, \omega)$. Because the weights decrease rapidly for large x_j , one can truncate the number of terms in the summation without significantly affecting the result. Following the suggestion of Davis and Rabinowitz (1975), the first 24 abscissas and weights of an m=68 rule are used.

The numerical contour integration techniques were tested by applying them to two integrands for which known analytic solutions exist. These are

$$\int_{0} \exp(-\nu_{\beta} z) J_{0}(kr) k dk$$

$$= (z/R^{2}) (1/R + ik_{\beta}) \exp(-ik_{\beta} R) \qquad (19)$$

and

$$\int_{0}^{n} \exp(-\nu_{\beta} z) (k/\nu_{\beta}) J_{1}(kr) k dk$$

= $(r/R^{2}) (1/R + ik_{\beta}) \exp(-ik_{\beta}R)$ (20)

where $R^2 = r^2 + z^2$. Equations 19 and 20 are obtained by taking the partial derivatives $-\partial/\partial z$ and $-\partial/\partial r$, respectively, of the Sommerfeld integral. A detailed study of Equations 1-8 shows that the functions of Equations 19 and 20 are directly proportional to the far-field SH wave solution in an infinite medium excited by vertical dip-slip and vertical strike-slip sources, respectively. To a first order, SH wave displacements in a layered medium will involve similar terms. Thus these integrals provide a realistic test of the numerical integration techniques. The branch point at $k = k_{\beta}$ introduces a singularity in the real axis integration for Equation 20, but the change in variable $k = k_{\beta} \sin \gamma$ removes the singularity. In a layered halfspace, surface wave poles can coincide with the branch point. Even though the change in variable may alleviate this problem, it is avoided numerically by taking the range of γ as $[0, \pi/2-\varepsilon]$. An $\varepsilon = 0.0001$ gives good results for Equations 19 and 20 even at r = 500 km and

frequencies up to 10 hz.

The integrals of Equations 19 and 20 were evaluated numerically using the techniques outlined in Equations 13 and 18. A value of β = 3.55 km/sec was used. The results of the tests are simply outlined. First, the numerical solution is valid at distances, r, as small as one-half source depth z, for all frequencies. At smaller distances, numerical evaluation of Equation 17 using the Gauss-Laguerre rule of Equation 18 breaks down due to inadequate sampling of the oscillating function $G(x_i/r,\omega)$ at low frequencies; a higher order rule would have to be used. At large distances and high frequencies the numerical integration of Equation 12 can fail due to the rapidly oscillating nature of the Hankel functions. Good results were obtained for Equation 20 at distances up to 500 km and frequencies up to 10 Hz using M=100, 200 and 300 for the frequency intervals (0,1), (1,5), and (5,10) Hz, respectively. On the other hand, the same choices of M only yielded good results for Equation 19 to distances of 100 km at frequencies of 10 Hz. This is due to the more rapid oscillation of the integrand of the real axis integral for Equation 19 than for Equation 20. Equation 19 really fails since one is trying to duplicate a z/R^2 dependence numerically for R>>z. Experience with more complicated earth models indicates that the size of the error in evaluating the real axis branch line integral for a vertical dip-slip source is acceptable, since the contribution of the branch line integrals are quite small compared to the larger contributions of the surface wave poles,

It can be shown that the function $g(x,\omega)$ in Equation 12 can be written as

$$g(k,\omega) = i \operatorname{Im} f_{\perp}(k,\omega) , \qquad (21)$$

since $f_{+}(k,\omega)$ is the complex conjugate of $f_{-}(k,\omega)$ for the SH problem and also for similar terms of the P-SV problem. Since $g(k,\omega)$ is an oscillatory function, it is informative to plot Im $f_{+}(k,\omega)$ as a function of frequency and wavenumber for various sources and earth models to obtain an appreciation of the nature of the integrand in Equation 12. In the following figures GII is kIm $f_{+}(k,\omega)$ for the vertical dip-slip source and G2I is Im $f_{+}(k,\omega)$ for the vertical strike-slip source excitation of SH waves.

Figures 1, 2 and 3 show normalized G1I and G2I for focal depths of 1, 10 and 20 km, respectively, in a homogeneous halfspace model given in Table 1. The horizontal axis varies from k=0 to k=k_{β_N}. The functions are plotted at frequencies of 0.1, 0.5, 1.0, 5.0 and 10.0 Hz. The singularity at k=k_{β_N} is due to the branch point for the halfspace problem.

Figures 4-6 present G1I and G2I for various depths in the single layer over a halfspace model of Table 1, while Figures 7-9 present the integrands for the four layer over a halfspace model of Table 1.

The integrands of Figures 1-3 are just those of Equations 19 and 20. It is seen that an increase in frequency or in focal

Table 1

Earth Models

d(km)	$\alpha(km/sec)$	β(km/sec)	$\rho(gm/cm^3)$
Halfspace			
	6,00	3.55	2.8
Simple Crustal Model	(SCM)		
40	6.15	3,55	2.8
	8.09	4.67	3,3
Central U. S. Model (CUS)	•	
1	5.00	2.89	2.5
9	6,10	3.52	2.7
10	6.40	3.70	2.9
20	6.70	3.87	3.0
~~	8.15	4.70	3,4

















Fig. 3. GlI and G2I for a source at a depth of 20 km in a simple halfspace.





Fig. 4. GII and G2I for a source at a depth of 1 km in the simple crustal model.











Fig. 6. G1I and G2I for a source at a depth of 20 km in the simple crustal model.





Fig. 7. GlI and G2I for a source at a depth of 1 km in the central U.S. model.





Fig. 8. Gll and G2I for a source at a depth of 10 km in the central U. S. model.





Fig. 9. GlI and G2I for a source at a depth of 20 km in the central U. S. model.

depth causes the function $g(k,\omega)$ to oscillate more rapidly. The effect of a more complicated structure is to introduce character to $g(k,\omega)$, but the simple observations still hold. The integration techniques used in the program SHSPEC have proven to work well to distances of 500 km and frequencies of up to 4 Hz (we have not yet run higher frequencies routinely).

The numerical techniques just described in this section are used by the computer program SHSPEC.
Velocity Time Histories

The spectra computed by the program SHSPEC are combined with a source time function in the program SHVEL to yield a velocity time history. A velocity time history is computed rather than a displacement time history because a discrete Fourier transform is used to convert spectra to time histories. Near the earthquake source, a final static offset is expected in the ground displacements. This offset cannot be handled by a discrete Fourier transform because of the inherent periodicity of the time series. To obtain the velocity time history of the ground motion, one need only convolve the impulse response of the medium with the velocity time history of the rupture process. The following two pulses are possible representations of this source function.

$$\tau s_{1}(t) = \begin{cases} 0 & t \le 0 \\ t/\tau & 0 \le t \le \tau \\ 2 - t/\tau & \tau \le t \le 2\tau \\ 0 & t > 2\tau \end{cases}$$

and

$$2\tau \ s_{2}(t) = \begin{cases} 0 & t \le 0 \\ \frac{1}{2} (t/\tau)^{2} & 0 \le t \le \tau \\ -\frac{1}{2} (t/\tau)^{2} + 2(t/\tau) - 1 & \tau \le t \le 3\tau \\ \frac{1}{2} (t/\tau)^{2} - 4(t/\tau) + 8 & 3\tau \le \tau \le 4\tau \\ 0 & t \ge 4\tau \end{cases}$$

(22)

(23)

These pulses have been normalized such that the area under each pulse equals unity. The Fourier amplitude spectrum of $s_1(t)$ is such that its shape can be enveloped by an f^o and f^{-2} asymptote, which intersect at a corner frequency $f_c = (1/(\pi \tau) Hz)$. The Fourier amplitude spectrum of the other pulse can be enveloped by f^o and f^{-3} asymptotes which intersect at a corner frequency of $f_c = 1/(4.36\tau)$.

The corner frequencies are mentioned since the estimation of the corner frequency and seismic moment of an earthquake is current practice in the specification of an earthquake by seismologists today. Most observations of the ground motion spectra of earthquakes indicate that the high frequency spectra varies as f^{-2} . Thus the source pulse s₁(t) might be favored. However, this choice is not very appealing on theoretical or numerical grounds since the whole-space solutions of Equation 19 and 20 would indicate delta function discontinuities in the acceleration time history at large distances, whereas the $s_2(t)$ large distance accelerations have only step discontinuities. Boore and Joyner (1978) provided a partial explanation. While $s_{2}(t)$ might be a good representation of a source time function to use for a small portion of the fault surface or for a faulting process involving coherent rupture, if one were to superimpose many $s_2(t)$ sources on the fault surface which "turn on" during an incoherent rupture process, the observed far-field spectrum will be enriched in high frequencies due to

this incoherence. In the case of incoherent rupture one might be able to have both finite far-field accelerations as well as a high frequency spectral asymptote varying as f^{-2} .

Since the input to SHSPEC specified layer velocities in units of km/sec, distances in units of km and densities in units of gm/cm³, source velocity pulses with unit area, such as $s_1(t)$ and $s_2(t)$, will correspond to sources with a seismic moment of 1.0E+20 dyne-cm.

Two time histories are presented, Gl and G2. Gl is the solution for the vertical dip-slip source and G2 is the solution for the vertical strike-slip source. Combining Equations 1, 2 and 8, the general equation for far-field displacements (those involving only $g_{\phi} = kJ_{n-1}$) are

$$U_{\phi}(t) = G_{1}[-2(t_{2}t_{3}-p_{2}p_{3})\cos\phi + 2(t_{1}t_{3}-p_{1}p_{3})\sin\phi]$$
(24)
+ $G_{2}[-2(t_{1}t_{2}-p_{1}p_{2})\cos2\phi - (t_{2}^{2}-t_{1}^{2}-p_{2}^{2}+p_{1}^{2})\sin2\phi]$

Displacement and Acceleration Time Histories

The program DSVLAC uses the velocity time history output of SHVEL to compute the ground displacement and acceleration time histories. The numerical realization of these time histories is not as obvious as it seems, especially for the ground accelerations. The output of SHVEL consists of ground velocity time histories at discrete points in time. Some assumption has to be made concerning the velocity variation at times in between, prior to integration or differentiation of the time series. Several approaches were considered, including the use of cubic spline interpolation. After much thought, the variation of ground velocity was assumed to be linear between the discretely sampled values. Thus, ground displacements can be computed using a simple two-point trapezoidal integration rule.

The acceleration time history then consists of a sequence of step segments. While this method of presenting the acceleration time history may seem odd, there are certain advantages. The cubic spline interpolation method was discounted because the smoothing process introduced ripples, which were purely an artifact of the smoothing process, into the acceleration time histories. The use of linear segments for the velocity time history permits an estimate of the acceleration that is not obscured by a smoothing process and also points out the discrete nature of the ground motion synthesis.

Response Spectra

The program SDSVSA uses the output of the program DSVLAC to compute the response spectra of the seismic traces. The input to SDSVSA from DSVLAC consists of the velocity time history at a given distance for the particular source as well as the computed maximum displacement, velocity and acceleration of the time history. The development of SDSVSA follows that of Nigam and Jennings (1969), with the modification that the velocity varies linearly between two time samples for the reasons used in discussing DSVLAC,

The equation of motion of a single degree of freedom oscillator with natural frequency ω and fraction of critical damping ζ subjected to a base acceleration a(t) is

$$\ddot{x} + 2 \zeta \omega \dot{x} + \omega^2 x = -a(t).$$
 (25)

To find the motion x(t) in the time interval $t_i \leq t \leq t_{i+1}$, the change of variable $\tau = t-t_i$ is introduced so that the equation of motion becomes

$$\frac{d^2 \mathbf{x}(\tau)}{d\tau^2} + 2\zeta \omega \frac{d \mathbf{x}(\tau)}{d\tau} + \omega^2 \mathbf{x}(\tau) = -\mathbf{a}(\tau).$$
(26)

Integrating with respect to τ , one obtains

$$\dot{\mathbf{x}}(\tau) - \dot{\mathbf{x}}(0) + 2\zeta \omega \mathbf{x}(\tau) - 2\zeta \omega \mathbf{x}(0) + \omega^2 \int_0^{\tau} \mathbf{x}(\tau') d\tau'$$
$$= - \{\mathbf{v}(\tau) - \mathbf{v}(0)\}$$
(27)

When $v(\tau)$ is given by linear segments, then

$$\mathbf{v}(\tau) = \mathbf{v}(0) + \frac{\Delta \mathbf{v}(0)}{\Delta \tau} \cdot \tau \quad . \tag{28}$$

Equation 27 now becomes

$$\dot{\mathbf{x}}(\tau) + 2\zeta\omega\mathbf{x}(\tau) + \omega^2 \int_0^{\tau} \mathbf{x}(\tau')d\tau' = \dot{\mathbf{x}}(o) + 2\zeta\omega\mathbf{x}(o) - \frac{\Delta \mathbf{v}(o)}{\Delta \tau} \cdot \tau$$
(29)

This equation can be solved by using Laplace transform techniques. After some algebraic manipulation, the motion of the oscillator at time t_{i+1} can be found iteratively by the relation

$$\begin{vmatrix} \mathbf{x}_{i+1} \\ \mathbf{x}_{i+1} \\ \mathbf{x}_{i+1} \end{vmatrix} = \begin{vmatrix} \mathbf{a}_{11} & \mathbf{a}_{12} \\ \mathbf{a}_{21} & \mathbf{a}_{22} \\ \mathbf{a}_{21} & \mathbf{a}_{22} \end{vmatrix} \begin{vmatrix} \mathbf{x}_{i} \\ \mathbf{x}_{i} \\ \mathbf{x}_{i} \end{vmatrix} = \begin{vmatrix} \mathbf{b}_{1} \\ \mathbf{b}_{2} \\ \mathbf{b}_{2} \end{vmatrix} \mathbf{v}_{i+1} \mathbf{v}_{i}$$
(30)

where

$$a_{11} = C + \omega\zeta S$$

$$a_{12} = S$$

$$a_{21} = -\omega^{2}S$$

$$a_{22} = C - \omega\zeta S$$

$$b_{1} = (-1 + C + \omega\zeta S) / \omega^{2}\Delta t$$

$$b_{2} = -S/\Delta t$$

$$C = \exp(-\zeta\omega\Delta t) \cos(\omega_{d}\Delta t)$$

$$S = \exp(-\zeta\omega\Delta t) \sin(\omega_{d}\Delta t) / \omega_{d}$$

and

$$\omega_{\rm d} = \omega (1 - \zeta^2)^{1/2}$$

These results could also be obtained from Nigam and Jennings (1969) by setting their $a_i = a_{i+1}$.

(31)

The response spectra are defined as

SD = MAX [
$$x_i(\omega, \zeta)$$
]
SV = MAX [$x_i(\omega, \xi)$]

and

where

$$\ddot{z} = -(2\zeta \omega x_{i} + \omega^{2} x_{i})$$
.

SA = MAX [$\frac{1}{2}(\omega,\zeta)$],

The pseudo velocity spectra is defined as

 $PSV = \omega SD$.

PART IV. NUMERICAL EXAMPLES

Truncation

A term by term inspection of Equation 1 shows that the tangential displacement can be thought to be made up of a far-field SH term, a near-field SH term, and a near-field P-SV term. Since it is much easier and faster to compute the SH functions than the P-SV terms, it is of interest to see the distance range at which a truncated version would provide acceptable results. To do this, a computer program developed by Johnson (1974) was used to compute the tangential displacements at the surface of an elastic halfspace for a north-south striking right lateral strike-slip source and for a north-south striking vertical dip-slip source, with west side down-thrown, at a receiver azimuth of 0° . A seismic moment of 3.53 E +21 dyne-cm was used together with the source function $s_2(t)$ with $\tau = 0.5$ sec at a depth of 10 km in a halfspace with $\alpha = 6.15$ km/sec, $\beta = 3.55$ km/sec and $\rho = 2.8$ gm/cm³.

Figures 10, 11 and 12 show the computed displacement, velocity and acceleration time histories, respectively, at distances of 10,25, 50 and 75 km for the vertical dip-slip source. Figures 13, 14 and 15 are the corresponding displacement, velocity and acceleration time histories, respectively, for the vertical strike-slip source. The units for displacement, velocity and acceleration are cm, cm/sec and cm/sec², respectively. At each distance, the trace on the left



Fig. 10. Study of truncation effect for tangential displacement time histories for a vertical dip-slip source at a depth of 10 km in a halfspace. Left column is complete solution, center column includes near and far field SH contribution, and the right column corresponds to the far field SH contribution at various distances.



Fig. 11 Same as Fig. 10. but for corresponding velocity time histories.



Fig. 12. Same as Fig. 10, but for corresponding acceleration time histories.



Fig. 13. Same as Fig. 10, but for displacement time histories for the vertical strike-slip source.



Fig. 14. Truncation study for velocity time histories of a vertical strike-slip source.



Fig. 15. Same as Fig. 13, but for acceleration time histories of a vertical strike-slip source.

corresponds to the complete solution, the center trace corresponds to the solution when the g_r/F_R term is dropped, while the trace on the right corresponds to the far-field SH solution obtained by using only the term $g_{\phi}kJ_{n-1}(kr)/F_L$ in Equation 1.

Remarkably, the complete solution (left trace) and the far-field solution (right trace) are very similar at distances greater than 25 km. At nearer distances, the near-field P and SV wave contributions change the character of the signal, especially for the ground displacements. The center trace shows the presence of non-causal, non-propagating arrivals, especially for the vertical dip-slip source. Herrmann (1978) interpreted this as an effect of improper truncation, in that the non-causal arrival must be cancelled by a similar "arrival" in the P-SV term. The difference between the true and farfield solution is clearly frequency dependent, with the difference becoming smaller at higher frequencies, as can be seen by comparing the displacement, velocity and acceleration time histories, or by a study of the wave number dependence of the terms in Equation 1.

Similar figures were computed using $\tau = 1.0$ which indicated significant differences between true and far-field displacements at distances less than 50 km, whereas the velocity and acceleration time histories were reasonally close at distances as small as 25 km. Because of the lack of a similar complete solution for a layered medium problem, it is assumed that the observations made here concerning the adequacy of the far-field solution will still hold.

From this point onward only the time histories associated with far-field SH contributions will be computed.

Contribution of Singularities

To understand the relative importance of each term in Equation 11, a series displacement of time histories were prepared. These are shown in Figures 16 and 17 for a source at a depth of 10 km in the Central U.S. model of Table 1 with a seismic moment of 3.53 E +22 dyne-cm, a source time function $s_2(t)$ with $\tau = 0.5$ sec and a low pass filter set at 1.0 Hz. The traces on the left and right of Figure 16 correspond to solutions at a distance of 25 km due to vertical dipslip and vertical strike-slip sources, respectively. Solution (a) is just the contribution of the poles, (b) is the effect of adding the real axis branch line integral to the pole contribution, and (c) is the complete solution consisting of the pole contributions and real and imaginary axis branch line integrals. The pole contributions yield a non-causal arrival for both sources (the later arrivals are in fact early negative time arrivals due to the inherent periodicity of the discrete Fourier transform). The addition of the real axis branch line integral improves causality and raises signal amplitudes to their final levels. The branch line integral along the negative imaginary k-axis, affects the signal amplitude slightly while making the signal causal.

Figure 17 is similar to Figure 16 except that the comparison



integration on the far field SH contribution to displacement time together with real axis and negative imaginary axis branch line r = 25 km. (a) pole contribution alone; (b) pole contribution plus real axis branch line integral; and (c) pole contribution histories for a vertical dip-slip source, left column, and a Fig. 16. Study of contribution of various components of contour vertical strike-slip source, right column, at a distance of integrals.





is made at a distance of 300 km. Surprisingly, this figure shows that at large distances the pole contributions describe the signal quite well, even the S_n phases. The addition of the real axis branch line integral just improves causality, while the imaginary axis branch line integral has little effect because of the 1/r factor in Equation 18. Using other values of τ the waveform distortion obtained at short distances using just the poles, or poles and real axis branch line integrals, is found to get worse as higher frequencies are excluded.

An insight has been obtained on saving computer time. At short distances, the complete solution with poles and branch line integrals is required for proper description of low frequency response. At large distances, especially if one is not bothered by low amplitude non-causal arrivals, the pole contributions are all that are required for a realistic estimate of the solution. By not having to perform the imaginary axis branch line integral at distances greater than 100 km, computer time savings can be significant. Swanger and Boore (1978) presented some examples showing how the individual surface wave modes add to form the solution. Their study also shows how well the pole contributions alone can fit real strong motion data.

Model Studies

To obtain an idea of the process of wave propagation, far-field time histories were computed for two of the earth models given in Table 1. A point dislocation source with a seismic moment of 3.53 E +22 dyne-cm and a source time function $s_2(t)$ with τ = 0.5 sec is placed at a depth of 10 km. The signals have been windowed to exclude all frequencies greater than 1.0 Hz. The resulting ground velocity time histories at various distances are given in Figure 18 for the single layer over a halfspace crustal model and in Figure 19 for the four layer over a halfspace crustal model. In these figures, the traces in column "a" correspond to a receiver at the given distance due north of a north-south striking vertical dip-slip source with the west side downthrown while those in column "b" correspond to ground motions due north of a north-south striking right lateral vertical strike-slip source. In Figure 18, it is seen that the first arrival is followed by two similar pulses of lower amplitude for the dip-slip source. These arrivals are the first Moho reflections due to downward and upward rays leaving the source. As distance increases, these reflections undergo a phase change when supercritical reflection occurs. The subcritical, non-phase changed, reflections are of low amplitude relative to the supercritical reflections. The surface wave can be said to emerge at a distance greater than 75 km as the number of supercritical reflections in the signal increases. A similar effect can be seen with the vertical strike-slip source,



Fig. 18. Suite of far field tangential velocity time histories for the simple crustal model of Table 1 for a vertical dip-slip source (a) and for a vertical strike-slip source (b) as a function of distance in kilometers.

column "b", except that the near vertical reflections at short distances are not very large. This is because the vertical dip-slip source has a maximum in its SH radiation pattern at vertical take-off angles, while the vertical strike-slip source has a mode for vertical take-off angles (Helmberger, 1974).

For a complicated structure, Figure 19, interpretation of the various arrivals in terms of particular ray paths is not very obvious. The vertical dip-slip source, column "a", shows some very distinct reflected phases which can be followed out to 75 km. At larger distances, the number of significant arrivals within a short time interval becomes so large that they are not seen as distinct arrivals, but rather as a composite surface wave. Refracted S_n arrivals can be seen emerging from the surface wave group at larger distances. An interesting point is the significant variation in the signal character over distances of only fifty kilometers, whereas gross properties such as maximum velocity only vary slightly.

Figures 20 and 21 show the pseudo velocity response spectra at distances of 25 and 300 km, respectively for a vertical strike slip source at a depth of 5 km in the central U. S. model of Table 1. A seismic moment of $5.0 \pm +19$ dyne-cm, a source pulse $s_2(t)$ with $\tau = 0.5$ sec, and a low pass filter set at 4.0 Hz were used. The insert in each figure shows the computed acceleration time histories. Tabulated values of the output of SDSVSA corresponding to the plots, Figures 20 and 21, are given in Figures 22 and 23.



Fig. 19. Suite of far field tangential velocity time histories for the central U. S. model of Table 1 for a vertical dip-slip source (a) and for a vertical strike-slip source (b) as a function of distance in kilometers.



Fig. 20. Pseudo velocity response spectra of a vertical strike-slip source at a distance of 25 km for 0, 2, 5, and 10 percent critical damping. The inset is the acceleration time history.



Fig. 21. Pseudo velocity response spectra of a vertical strike-slip source at a distance of 300 km for 0, 2, 5 and 10 percent critical damping. The inset is the acceleration time history.

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03

DMAX= 0.338504 AMAX# 0.186403 VMAX# 0.536404

DAMP=0.10	PSV	79-5	9355	1204	1354	1404	16-4	20-4	24.44	25.4	28=4	33-4	52=4	76=4	94-4	10 = 1 = 1 = 1	.11-3	98-4	82-4	72.4	10344	54-4	4664	3404	25-4	21-4	2004	100	16-4	404	4021	1104	98-5	79-5	67.5	57 55	.50-5	. 45 55	4105	34.5	29-5	20.5	2015	
	S≜	20=3	14953	22=3	20=3	2053	2053	2453	, 22=3	2053	, 20=3	,2153	, 27 <u>5</u> 3	59463	37=3	37.53	3553	2553	1853	10.04	10=3	7854	,61=4	. 38c4	. 25-4	19e4	16=4	1404	10=4	81 ⊡ 101	, 6655]56≝5	48=5	3405	27=5	225	1855	1000			92-6	79=6	69=66 61=6	
	δġ	25-5	29-5	.50-5	. 80-5	. 75-5	72-5	. 11-4 .	4-47.	.20-4	.19-4	. 22-4	41-4	4-29.	. 84-4	. 96-4	.10-3	.11-3	98-4	89-4	8774	. 84-4	.81-4	.76-4	.72-4	68-4	.66-4	64-4	61-4	59-4	.58-4	57-4	.56-4	55-4	. 55-4	54-4	.54-4	54-4	54-4	5344	53-4	53-4	1 1 4 4 4 4	
	SD	31-0	44=0	.67 <u>-6</u>	81=6	.10=5	1359	19-5	. 26-5	. 32=5	41.5	53-9	699 69	.17=4	24=4	30=4	35.4	0.9 0.0	3964	40=4	40.4	3654	.3764	32=4	2804	27=4	28=4	2964	30=4	3054	31=4	31e4	31e4	32-4	3264	.32=4	32-4	3294	32=4	3294	3254	.32=4	5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	
DAMP=0.05	PSV	. 80 - 5	69 <u>-</u> 5	444	14-4	16=4	17=4	22=4	26=4	29-4	31=4	.36=4	58.4	90m4	5.1.5	13=3	513-3	5121	94.4	79.4	.68=4	58-4	4014	. 35=4	.26=4	22-4	20-4	19-4	10=4	1404	12-4	11-4	10-4	. 80 c 5	67.5	58=5	51-5	45=5	.41.5	34.5	29.5	26.5		
	SA	.20-3	2767	25-3	23-3	. 22-3	5113	23-3	23-3	, 23-3	.2243	23-3	5414	.40-3	45-3	45+3	42-3	, 30Å3	20-3	14-3	110		. 62-4	3844	2444	1-8-4	15-4	12-4	5 0 4 B	69-5	54-5	6-44-5	37-5	26-5	19-5	. 5-5	12-5	,10-5	.88-6	68-6	55-6	46-6	4 M 104 M 104 M	, , , , , ,
	SV	2845	32.5	62-29	10-4	, 77 = 5	67.5	.12=4	.21-4	.23.4	20.4	23-4	46-4	75=4	10-3	13-3	13:03	13=3	11:3	95-4	91-4	87=4	83-4	77.44	13-4	, 69 . 4	66.4	64.4	61-4	59-4	58-4	57.4	56=4	55.4	54=4	54=4	54=4	53.4	-53-4	15344	53=4	53.4	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	
	SD	32-6	42-6	. 77-6	.92-6	.11-5	. 14-5	21-5	29-5	37-5	.44+5	57-5	.11-4	.20-4	29-4	37-4	42-4	48-4	45-4	44-4	43-4	41-4	.39-4	34-4	29-4	28-4	.29-4	.30-4	30-4	4-10.	31-4	. 32-4	32-4	32-4	4-25.	. 32-4	.32-4	32-4	.32-4	33-4	4+20	.33-4	4-00 94-0	
DAMPE0.02	ΡSΥ	.80¢5	89-5	.16=4	.1854	.17=4	.18c4	. 23 - 4	. 28-4	33:4	.3364	. 38e4	6454	.1003	1303	.1553	.15-3	14=3	.1100	. 8 4 - 4	.71e4	.61-4	404	3664	.26=4	.23=4	.21=4	1954	.16=4	1454	.12=4	1124	.10=4	.8105	. 6855	.58.5	.5105	45.5	.41.5	34.5	29-3	.2655	200 200 200 200 200	
	SA	20-3	2=615	28-3	28=3	.24-3	. 22-3	24-3	. 25=3	.26=3	. 23-3	. 24=3	. 33-3	45=3	51-3	51•3	48-3	34=3	, 22=3	15-3	11-3	, 85e4	6404	.38=4	2404	18=4	15c4	,12=4	. 85 = 5	. 64=5	50-5	. 40°5	. 33-5	22 5	15-5	, 12 - 5	91-6	, 73=6	.61-6	45-6	35-6	.28=6	, 23 • 6	• > •
	SV	.29-8	5-62	83-5	13-4	. 83-5	63-59	.12-4	24-4	.25-4	.22-4	. 25-4	50-4	89-4	1303	15-5	5-3-51-	14-5	12-3	98-4	4-26	. 89-4	. 85c4	78-4	. 73-4	69-4	66-4	64-40	. 61-4	59-4	57-4	56-4	56-4	551	5414	54-4	53-4	. 5G	53-4	. 53 E 4	100	53-4	10 10 10 10 10 10 10 10 10 10 10 10 10 1	5)
	đs	32-6	.43=6	.87-6	,11-5	12=5	.14=5	22=5	.31=5	5=24	.47=5	61-5	,12=4	.23=4	4.00	42=4	48=4	54=4	50=4	47=4	45-4	4364	.40-4	.35=4	. 29 = 4	, 29=4	30=4	30=4	31-4	4140.	32=4	32=4	32=4	32=4	32=4	. 32=4	4=00.	.33=4	.33=4	4=00.	33-4	4 B 2 2 4	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,
DAMPEO.	PSA	.80-5	.95=5	.17-4	.22-4	.18-4	.18=4	24=4	.30=4	37=4	.34=4	40-4	.68-4	.11=3	15-3	.18-3	.18-3	.15-3	,12=3	. 89=4	74=4	. 62-4	. 52-4	.37=4	, 27=4	.23=4	.21=4	19=4	.16-4	.14=4	4=21.	.11=4	10-4	.81+5	• 68=3	59-55	51-5	46=5	.41-5	34=5	29 19	2645	5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	1 45.0
	SA	20=3	20-3	.31-3	54-35	25=3	23-3	. 26-3	27-3	, 29-3	.24-3	. 25-3	. 35=3	2=64	60-3	,62=3	56-3	5.85	25	16-3	.12-3	.87-4	,66=4	.39-4	.24-4	,18-4	15-4	12-4	.86-5	64=5	49-5	39-12	32-5	20-2	14-5	11-5	.81-6	64=6	52=6	36-6	26-6	20-6	-10 -10 -1-))++
	SV	.30=5	5112	.10-4	.18-4	. 87=5	. 64=5	1344	.26-4	.28=4	.23=4	.27-4	54-4	99-4	15=3	,18-3	.18-3	15-31	13=3	.10-3	95-4	90-4	.86-4	79-4	13-4	. 69-4	. 66-4	64-40.	61-4	59-4	57-4	56-4	56-4	55.4	. 54=4	5444	193-4	53-4	53-4	5374	53-4	94-26	10 M 10 M 10 M 10 M	~ ~ ~ ~
	as S	32-6	45-6	9-16	4	5101		23-5	34-5	47-5	49-5	64-5	13-4	24-4	39-4	51-4	56-4	60-4	56-4	49-4	47-4	45-4	42-4	35-4	30-4	30-4	30-4	4-15	4 - 1 - 1	32-4	32-4	32-4	32-4	32-4	33-4	33-4	4-20.	33-4	33-4	4.00	33-4	33-4	4 - 1 1 1 1	7 - > > -
	5	:16-7	. 41.15	.79=5	.17-4	. 28 5	.15-7	63=5	.21=4	.24=4	13-4	.10-7	.36=4	.98-4	15-31	18-3	5-01.	.15=3	12:0	. 88-4	.70-4	. 56-4	46-4	.32-4	23=4	.18-4	14=4	, 11-4	. 78=5	. 55 . 5	- 42 - 42 - 15	. 3355	.27=5	8 . 5	.13=5	.99=6	.79-6	.65=6	.54=6	.41=6	.34-6	.29-62.	23.56	ンドンシー
	PERIOD	0,25	0,30	0,35	0.40	0.45	0.50	0,60	0.70	0.80	0.00	1.00	1.20	1.40	1.60	1,80	2,00	2,50	3,00	3,50	4,00	4.50	5,00	6,00	7.00	8,00	00.6	10.00	12,00	14,00	16.00	18,00	20.00	25,00	30.00	35,00	40.00	45,00	50.00	60.00	70.00	80.00	90.00 100.00	*ントンス i

Fig. 22. Tabulated output of SDSVSA corresponding to Fig. 20 plot.

(R4 800.00 KM DEPTHE N.00 KB)

G S AMAX# 0.22E-04 VMAX= 0.80E-05 DMAX# 0.38Ec05

1997 00 1991 99 9 1991 99 DAMP=0.1 0 0 1 × 1 × 1 1 × 1 × 1 145 54 3-2 1-5 9 10 4 10 4 10 3-2 8-4 ŝ 4-5 50 œ 44<u>6</u>5 0.4 0.0 0101000 0101000 010101010 01010101010 01010101010 100 10 101 0 300 ŝ 6 - 6 0 60=5 4 15=4 \$2**~2** のまままりの ののみの方の まままままま であるのの 59-65 5=2 . 25=4 4-47 68=6 ø ŝ 25=4 ÷ 100 25 52 4 39-4 4 (V (V 10 10 4 10 (0 4) 4 (10 (0 1 1 1 1 1 1 1) 4 4 4 4 4 4 4 - **1** 16-6 4 0 0 0 0 0 0 1 1 0 0 1 4 4 1 4 4 4 4 4 4 4 39-4 DAMP=0\$05 \$1 40.00 10 140400 00000000 100000000 5.0 0=2 55 -4 4 * 4 α 37-7 10.0 1001 1001 11111 11111 11111 8-19 10 5 1944 1964 1964 1964 • 44 10 07 07 44 40 05 14 44 40 65 19 10 10 10 10 10 10 10 47.95 00014 00014 4555 1564 0 0 0 0 0 0 0 0 0 0 Ś 79.55 29°22 .14-4 4 0 0 . 69 e5 .67.5 .69-6 .59-66 2894 ŝ N M 44444444444449000 ままで、 ままで、 ままで、 しまで、 しまで、 しまで、 しまで、 しまで、 しまで、 しまで、 しまで、 しまで、 したで、 しまで、 したで、 したで 0000 0000 0000 0000 2=0 1.7 25 . 7 8 DAMR=0,02 40404030 1111111 ະ 1:1:1 ເອີຍ .19-4 444 0000 1111 .16=6 482 4 10 N 1 8 8 4 4 4 0.00004 FFFFF 4.00000 0000 0000 0000 0000 50 a 5 4615 •. •. • •. •. •. •. • 32=4 .26-4 66=5 23=5 2015 20-4 71=4 33=4 M = 180 . 69 - 6 . 60 - 6 52-6 9=2**+** 0 11 10 9-0 9-0 37=5 .19-4 40-4 16=4 9 a 9 S 4 0400044044 000000470 111111111111 4044400440 4-4-6-1 I I 1 I 1 I 1 I 1 I 1 I 0 - 5 000000 1111 1111 99 1 1 9 9 91-19 91-19 64-4 40-4 4 - 0 .14-7 9-4 DăMP≊0 71-4 19-4 4-40 41-4 26-4 .20-4 .14-4 .10-4 . 88 - 5 44 10 10 10 10 10 10 43-5 9-9 00:440 1:1:1:1:1:1: 4:10:10:10:10 5-0 6-2 47-5 72-8 9997777 サーサウ 242 6 2 ER100 0.25 0.30 . 60 44 0.6° 00.00

Fig.

It is interesting to note how much character is introduced into the response spectrum at the larger distance, which is due just to wave propagation effects.

As a practical application of the theory presented, the variation of maximum velocity with distance, focal depth, and source duration was studied. The signals were generated using a frequency window of 0 - 1 Hz, as before. To enable comparison with a simpler model, the single layer over a halfspace crustal model was used, and the results were compared to those for a uniform halfspace with properties of just the layer. Figure 24 shows the effect of focal depth. The source pulse had $\tau = 1$ sec and a seismic moment of 3.53 E + 21 dyne-cm. The computed single layer over a halfspace solutions are given by the symbols, while the halfspace solutions are given by the solid curves. Figure 25 shows the variation with source pulse duration, seismic moment fixed. Several points are immediately apparent. First, out to distances of about 75 km the halfspace solution is quite good. At distances greater than 75 km the halfspace solution breaks down, especially for the vertical dipslip source, for which the apparent geometrical spreading changes from r^{-2} to r^{-1} . This is the result of the contribution of supercritically reflected arrivals, or equivalently, the process of surface wave formation. Note the difference in apparent geometrical spreading between the vertical dip-slip and vertical strike-slip sources. Finally the variation of maximum velocity with source pulse



Fig. 24. Effect of variation in focal depth upon the maximum ground velocity for a vertical dip-slip source, G1, and for a vertical strike-slip source, G2, for fixed source pulse duration. The symbols correspond to the corresponding simple crustal model solid curves correspond to a halfspace solution, while the solution.

57 :



Fig. 25. Effect of variation in source pulse duration upon the maximum ground velocity for a vertical dip-slip source, G1, and for a vertical strike-slip source, G2, fixed focal depth The halfspace solutions, solid curves, are compared to the simple crustal model solutions, symbols.

duration can be used with source spectrum scaling laws to see how this parameter varies with the size of the earthquakes, e.g. if seismic moment is proportional to the cube of source pulse duration, "constant stress drop" scaling, an increase in seismic moment by a factor of 8 would yield an increase in maximum velocity by a factor of about 2. This may be of value in scaling strong motion. Since only the far-field SH term was used, the scaling at short distances is only approximate,

PART V. CONCLUSIONS

The theory for the far-field ground motion due to dislocation earthquakes has been presented together with a description of the numerical techniques used for this realization. Some examples were presented to provide an insight to the numerical methods as well as to present some examples of how wave shapes are affected by propagation through a layered earth.

The computer programs documented in this report should be useful for more detailed studies of wave generation due to complex earthquake rupture processes as well as for inferring more realistic ground motion scaling rules than are currently being used.

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APPENDIX A: COMPUTER PROGRAM SHSPEC

Function

This program computes the far-field complex Fourier spectra for point vertical strike-slip and vertical dip-slip earthquake sources at a fixed depth in a layered medium. The program is written in FORTRAN IV for the Honeywell 6023 digital computer at Saint Louis University. The programming has been kept simple to facilitate conversion to other computers. As it stands, the program provides good results for the distance range of about 5 km to 500 km for frequencies up to 10 Hz. Special normalization has been introduced to take into account the fact that the Honeywell 6023 floating point number is limited to the range 10^{-38} to 10^{+38} .

Input

Input is from card through File 60. A description of input variables is given in Table A1.

Output

Output is through File 61 and also through standard printer output using the PRINT statement. A description of printer output is given in Table A2.

File Codes

The following file codes are used for I/O functions:

- 11 Mass storage file used for temporary storage by subroutines EXCIT and WVINT
- 12
- Mass storage file used to store G1 and G2 solutions in frequency domain for specified
 - distances. Contents of this file are used as

input by the program SHVEL.

60	Card Reader
61	Printer output using WRITE(61,n) statement.
	Printer output using PRINT n, statement.

Sample Input

Sample input data for generating the traces of Figure 19 are given in Table A3.

Program Listing

A description of the various subroutines of the program is given in Table A4, while a listing of the program is given in Table A5.

Table Al

Input	Var	riab	les
TUDUC	vai	au	1.00

Card	Variable	Name	Columns	Format	Description
1	DEPTH		1-10	F10.5	Focal depth in km
	FL		11-20	F10.5	Low frequency cutoff in Hz
	FU		21-30	F10.5	High frequency cutoff in Hz
	DT		31-40	F10.5	Sample interval in seconds. Time series in N*DT seconds long.
	N		41-45	15	Number of points in time series. Must be power of two and .LE.1024. Large N requires much computer time
	VRED		46-55	F10.5	Used to compute reduced travel time t-R/VRED for shifted time axis. If VRED.EQ.O, no reduced time used.
2	D		1-10	F10.5	Layer thickness in km. Read Card 2's until end of model indicated by D.LE.O
	A		11-20	F10.5	Layer P wave velocity in km/sec
	В		21-30	F10.5	Layer S wave velocity in km/sec
	RHO		31-40	F10.5	Layer density in gm/cm ³
3	R		1-10	F10.5	Epicentral distance in km. Keep reading Card 3's until one found with R.LT.O, then end program and close files.
	XOUT		11-20	F10.5	Control variable XOUT=0complete solution XOUT=1solution using poles and real axis branch line integral XOUT=2solution using poles only
	то		21-30	F10.5	.EQ.0 use VRED to plot time series as a function of reduced travel time .NE.0 TO is the time shift for plot

Table A2

Output Variables

Name	Descritpion
Output File 61:	
FL	Low frequency cutoff
FU	High frequency cutoff
DF	Frequency interval (DF=1/(N*DT))
N1	Index to indicate array position of FL
N2	Index to indicate array position of FU
DEPTH	Focal depth in km
FREQ	Frequencies at which theoretical response is calculated
R	Epicentral distance in km
IOUT	Type of output. IOUT=3-XOUT, XOUT defined in Tabel A1
то	Computed time shift from input TO of VRED input
Output File for	PRINT statement
D	Layer thickness in km
А	Layer P waye velocity in km/sec
В	Layer S wave velocity in km/sec
RHO	Layer density in gm/cm ³

Тa	ь1	e	A3

Sample Input

0 1	1 0	2 0	3 0	4 0	4 5	5 0	6 0	7 0
				<u>u</u>				
10.	0.0	1.0	0.25		256			
1.0	5.0	2.89	2.50					
9.0	6.1	3.52	2.70					
10.	6.4	3.70	2.90					
20.	6.7	3.87	3.00					
0.0	8.15	4.70	3.40					
25.	0.0							
50.	0.0							
75.	0.0							
100.	0.0							
150.	0.0							
200.	0.0							
250.	0.0							
350.	0.0							
450.	0.0							
-1.0								

Table A4

Subroutine Description

Subroutine Name	Function
RSHOF	Computes the functions of Equation 2 for given values of real wavenumber k and frequency
EXCIT	Computes ratios of the type g_1/F_L and g_1/F_L' for
	various values of k for each frequency and stores the results on File 11 for later calls by WVINT
WVINT	Performs numerical integration
HANK	Evaluates Hankel functions $H_{1,2}^{(2)}(kr)$
IHANK	Evaluates $\int_0^z H_0^{(2)}(z) dz$
AXIMAG	Performs numerical integration along negative imagi- nary k-axis
SHCFIK	Computes ratio of the type g_1/F_L for imaginary values of wavenumber
BESMOD	Computes modified Bessel function values
SRCMOD	Reads in earth model parameters
SRCLYR	Using the given focal depth, this searches for source layer
SHCOEF	Computes matrix products of Equation 3

Table A5

SHSPEC PAGE 1

00000		PROGRAM SHSPEC COMPLEX DUM1,DUM2 COMMON / MODEL / D(15),A(15),B(15),RHQ(15),MMAX COMMON/SOURCE/DEPTH,LMAX,DPH COMMON / INT / IOUT DIMENSION DATA(2048),DATA1(2048) THIS PROGRAM EVALUATES THE SH WAVE GENERATION BY A SOURCE IN A LAYERED MEDIUM, FOR REFERENCES SEE J.A.HUDSON (1969) GEOPHYS,J, VOL 18 PP 353-370, N,A.HASKELL (1964) B.S.S.A, VOL 54 PP 377-393,
C		DATA SHOULD BE ENTERED IN THE FOLLOWING ORDER
000000000000		CARD 1 DEPTH,FL,FU,DT,N CARD 2 D.A.B.RHO EARTH MODEL READ IN MORE CARD 2 - D.LE,O FOR HALFSPACE CARD 3 R,IOUT,TO MORE CARD 3 - USE R.LT,O TO END CARD 3 SEQUENCE TO SAVE COMPUTER STORAGE, INTERMEDIATE RESULTS ARE WRITTEN ON FILE 11. FILE 12 CONTAINS COMPLEX SPECTRA
0000		AT DISTANCE R. READ IN FOCAL DEPTH, LOWER AND UPPER FREQUENCY BOUNDS, DT AND N READ(60.1) DEPTH.FL.FU.DT.N.VRED
	1	FORMAT(4F10,5,15,F10,5) ÎF(DEPTH,LT,0,0) GO TO 9998 WRITE(12,1) DEPTH,FL,FU,DT,N,VRED CALL \$RCMOD CALL \$RCLYR DF = 1./(N+DT)
		N1 = FL/DF N2 = FU/DF N1 = N1 + 1 N2 = N2 + 1 NYQ = (N/2) + 1 NYQ = 2 + NYQ
	9 1	WRITE(01,9) FL,FU,DF,N1+N2,DEPTH FORMAT(1H0,4HFL =,F10,5,5X,4HFU =,F10,5,5X,4HDF =,F10, 5,5X,4HN1 =,I4,5X,4HN2 =,I4,5X,7HDEPTH =,F10.2) WRITE(61,2)

2 FORMAT(1H0,39HFREQUENCIES FOR WHICH RESPONSE COMPUTED)

```
DO 100 I = N1.N2
      PREQ ₹ (I+1) + DP
      WRITE(61,3) FREQ
    3 FORMAT(1H , F10, 6)
      CALL EXCIT(FREQ)
  100 CONTINUE
 500 READ(60,1) B,XOUT,TO
      R = EPICENTRAL DISTANCE
C
      XOUT = 0.0 POLES + REAL AXIS BRANCH LINE + IMAGINARY
Ĉ
C
      AXIS BRANCH LINE INTEGRALS
C
      XOUT = 1.0 POLES + REAL AXIS BRANCH LINE
Č
      XOUT = 2.0 POLES
C
      TO .EQ. O USE REDUCED TRAVEL TIME, OTHERWISE USE TO
      IF(XOUT, LT, 0, 0, 0R, XOUT, GT, 2, 0) XOUT = 0,0
      10UT = 3. - XOUT
      REWIND 11
      REDUCED TRAVEL TIME TIME SHIFT
С
      \dot{T} = 0.0
      IF(VRED, GT. 0.0) TO = R/VRED
      WRITE(12,601)R, IOUT, TO
  601 FORMAT(E11, 4, 15, E11, 4)
      IF(R.LT.0.0) GO TO 9998
      WRITE(61,580) DEPTH, R, IQUT, TO
  580 FORMAT(1X,6HDEPTH=,F6,2,3X,2HR=,F6,2,3X,5HIOUT=,14,3X,
     13HT0=,E11.4)
      EVALUATION OF WAVENUMBER INTEGRALS
С
      NN # 2 # N
      00 250 I = 1,NN
      DATA1(I) = 0.0
  250 \text{ DATA(I)} = 0.0
      D0 300 I = N1, N2
      FREQ = (1-1) + DF
      FAC = 6,2831853 * FREQ * TO
      XR = COS(FAC)
      XI = SIN(FAC)
      CALL WVINT(R, FREG, AR1, AI1, AR2, AI2)
      DUM1 = CMPLX(XR,XI) + CMPLX(AR1,AI1)
      DUM2 = CMPLX(XR,XI) + CMPLX(AR2,A12)
      AR1 = REAL(DUM1)
      AI1 = AIMAG(DUM1)
      AR2 = REAL(DUM2)
      AI2 = AIMAG(DUM2)
      J = 2 + I - 1
      K = 2 + 1
      DATA(J) = AR1
```

DATA(K) = AI1DATA1(J) = AR2 DATA1(K) = AI2300 CONTINUE WRITE(12,600)(DATA(I),1=1,NY02) WRITE(12,600)(DATA1(I), I=1, NY02) 600 FORMAT(8E11.4) GO TO 500 9998 CONTINUE REWIND 12 STOP END SUBROUTINE EXCIT(FREQ) DIMENSION P1(300), P2(300), WVN(300), WVC(300) COMPLEX G1(300), G2(300) COMPLEX X1, X1P, X1M, X2, X2P, X2M, FL, FLP, FLM COMPLEX EYEPI COMMON / MODEL / D(15), A(15), B(15), RHQ(15), MMAX COMMON/ SPACE / G1,G2,P1,P2,WVN,WVC $E\bar{Y}EPI = (0.0, -3.1415927)$ LATER ON ADD BMAX AND BMIN INTO MODEL ČMAX = B(MMAX) $\dot{C}MIN = B(1)$ OMEGA = 6.2831853*FREQ WVMN = OMEGA/CMAX WVMX = OMEGA/CMIN IF (FREG, E0.0.0) 60 TO 4000 APPROXIMATE NUMERICAL INTEGRATION TEST FOR A FINER GRID FOR HIGHER FREQUENCIES THIS SHOULD BE VALID FOR DISTANCES UP TO ABOUT ⁵00 km AT PREQUENCIES LESS THAN 10HZ. NGAM = 100 IF (FREQ.GE.1.0, AND.FREQ.LT.5.0) NGAM # 200 IF(FREQ, GE, 5.0) NGAM = 300 DGAM = 1.57079633/NGAM NROOTE NGAM - 1 DD 3998 IE1,NGAM GAM - I + DGAM IF(I.EQ.NGAM) GAM=0.9999+1.57079633 WVNO = WVMN + SIN(GAM) WVNC = WVMN + COS(GAM) CALL RSHOF(X1, X2, FL, OMEGA, WVN0, EXE1, EXL1) WVN(I) = WVNO WVC(T) = WVNC

C

C

C

C

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```
ELJ - EXL1 - EXE1
      FACX = 0.0
      TF(ELJ.GT.-70.) FACX # EXP(ELJ)
      X1 = X1/FL
      X_2 = X_2/FL
      T1 = FACX+WVNO+WVNC
      P_1(1) = AIMAG(X1) * T1
      P2(I) = AIMAG(X2) + T1
 3998 CONTINUE
      WRITE(11,6) OMEGA, NGAM, DGAM
      WRITE(11,2) ((WVN(J), WVC(J), P1(J), P2(J)), J=1, NGAM)
    6 FORMAT(E13,6,15,E13,6)
 4000 CONTINUE
      NROOT = 0
      NMX IS CHOSEN FOR A 40 KM CRUSTAL NODEL, FOR SHALLOWER
C
      THICKNESSES & PROPORTIONATELY SMALL NMX CAN BE USED.
C
      NMX = 100 + (FREQ + 100.)
      DK = (WVMX - WVMN)/NMX
      IF(DK.LT.1.0E-8) GO TO 5001
      SEARCH FOR ROOTS OF PERIOD EQUATION
C
      C1 = WVMN + 0.01*DK
      CALL RSHOF (X1, X2, FL, OMEGA, C1, EXE1, EXL1)
      DEL1 = REAL(FL)
      NMX1 = NMX + 1
      DO 5000 I=2.NMX1
      C2 = WVMN + (I-1) + DK
      CALL RSHOF(X1, X2, FL, OMEGA, C2, EXE1, EXL1)
      DEL2 # REAL(FL)
      IF (SIGN(1.0, DEL1) + SIGN(1.0, DEL2), GE, 0, 0) GO TO 4999
      NROOT = NROOT + 1
      C4 = C2
      DEL4 # DEL2
      DO 4990 II=1,5
      C_3 = 0.5*(C1+C4)
      CALL RSHOF(X1,X2,FL,OMEGA,C3,EXE1,EXL1)
      DEL3 = REAL(FL)
      IF (SIGN(1.0, DEL1) * SIGN(1.0, DEL3), GE, 0.0) GO TO 4991
      DEL4 = DEL3
      C4 = C3
      GO TO 4992
 4991 DEL1 = DEL3
      C_1 = C_3
 4992 CONTINUE
 4990 CONTINUE
      C3 = 0.5*(C1+C4)
```

C

```
CALL RSHOF (X1P, X2P, FLP, OMEGA, C3+0, 1+DK, EJP, ELP)
     CALL RSHOF (X1M, X2M, FLM, OMEGA, C3-0, 1+DK, EJM, ELM)
     DFJ = EJP = EJM
     DFL = ELP-ELM
     ELJ = ELM-EJM
     X1P=X1P+EXP(DFL)
     X2P#X2P+EXP(DFL)
     FLP=FLP+EXP(DFJ)
     FACX # 0.0
     IF(ELJ.GT.-70.) FACX = EXP(ELJ)
     DFDK # (REAL(FLP)-REAL(FLM))/(2,+0,1+DK)
     DFDK = 5.+(REAL(FLP)-REAL(FLM))/DK
     GI(NROOT) = 0,5 * REAL(X1P * X1M) * EYEPI / DFDK
     GI(NROOT) = G1(NROOT)*FACX
     G2(NROOT) = 0.5 + REAL(X2P + X2M) + EYEPI / DFDK
     G_2(NROOT) = G_2(NROOT) + FACX
     WVN(NROOT) = C3
4999 01 # 02
     DEL1 3 DEL2
5000 CONTINUE
5001 CONTINUE
     WRITE(11,5) OMEGA, NROOT
     IF(NROOT.E0.0) GO TO 5002
     WRITE(11,2) ((WVN(J),G1(J),G2(J)),U=1,NROOT)
   2 FORMAT(10E13.6)
   5 FORMAT(E13.6,15)
5002 CONTINUE
     RETURN
     END
     SUBROUTINE WVINT(R, FREQ, AR1, AI1, AR2, AI2)
     DIMENSION P1(300), P2(300), WVN(300), WVC(300)
     COMPLEX G1(300),G2(300)
     COMPLEX HO, H1, H01, H11, HI, SUM, SUMO, SUM1, SUM2
     COMMON / SPACE / G1,G2,P1,P2,WVN,WVC
     COMMON / MODEL / D(15), AA(15), BB(15), RH0(15), MMAX
     COMMON / SOURCE/ DEPTH, LMAX, DPH
     COMMON / ÎNT / IOUT
     FCT = 1./(12.5663706#88(LMAX)#88(LMAX))
     PIL = 3.141592653
     AR1 = 0.0
     A11 = 0.0
     A12 = 0.0
     AR2 = 0.0
     OMEGA = 6.2831853 \circ FREQ
```

С

C

```
SUM1 = CMPLX(0.,0.)
    SUM2 = CMPLX(0.,0.)
    1F(FREQ.EQ.0.0) GD TO 4000
     APPROXIMATE NUMERICAL INTEGRATION
    ALONG BRANCH LINE FROM K = 0 TO K = K-BETA(MAX)
    READ(11,6) OMEGA, NK, DGAM
    READ(11,2) ((WVN(J),WVC(J),P1(J),P2(J)),J+1,NK)
 6 FORMAT(E13.6, 15, E13.6)
    TF(IOUT.EQ.1) GO TO 4000
    WVNO = WVN(1)
    TO1 = WVNO+R
    CALL HANK(T01,1.0,H01,H11)
    SUM1 = 0.5+P1(1)+H01+DGAM
    SUM2 = 0.5*P2(1)*H11*DGAM
    CALL IHANK(TO1, H01, H11, SUMO)
    DO 200 I=2,NK
       = I-1
    11
    WVNO = WVN(I)
         # WVND*R
    TO.
    CALL HANK(TO,1.0.HO,H1)
    CALL IHANK(TO, HO, H1, SUM)
    TTST = 1
    IF((TO-TO1).LT.PIL) ITST=2
    GO TO (150,160), ITST
150 CONTINUE
         ■ SUM-SUMO
    HI
    SLP = WVC(I1) +R
    SLP2 = SLP + SLP
         = P1(11)
    A
         = (P1(I)-P1(I1))/DGAM
    R
    SUM1 = SUM1+A+HI/SLP
    SUM0 = T0 + H1 - T01 + (HI + H11)
    SUM1 = SUM1+B+SUM0/SLP2
         = P2(11)
    Δ
         = (P2(I)-P2(11))/DGAM
    R
    SUM2 = SUM2+A+(H01-H0)/SLP
    SUM0 = HI + (T01 - T0) + H0
    SUM2 = SUM2+B*SUM0/SLP2
    GO TO 170
160 CONTINUE
    SUM1 = SUM1+0.5*(P1(I)+H0+P1(I1)+H01)+DGAM
    SUM2 = SUM2+0.5*(P2(I)+H1+P2(I1)+H11)+DGAM
170 CONTINUE
    Ho1 = HO
    H11 = H1
```

	200	CONTINUE
	200	SIM1 = SIM1 + CMP(X(0, 0, -1, 0))
		SUMT = SUMT OMERCHER(0,0) = 1 0)
		SUM2 A SUM2*UMFLX(U)U\$****V/
_ 4	+000	CONTINUE
С		POLE CUNTRINUTIONS
		READ(11,5) UMEGA1, NK
	5	FORMAT(E13.6,15)
		IF(NK.EQ.0) GO TO 399
		READ(11,2) ((WVN(J),G1(J),G2(J)),J=1,NK)
	2	FORMAT(10E13.6)
		no 300 I = 1, NK
		WVNO = WVN(I)
		CALL HANK (WVNO, R. HO, H1)
		SUM1 = SUM1 - H0 + G1 (T) + WVNO
		SUM2 = SUM2 + H = G2(T) = WVNO
	200	
	300	
		AR1 = REAL(SUM1) + RCT
		ARZ = REAL(SUM2/AFC)
		AIL = AIMAG(SUM1)*FUT
_		AI2 = AIMAG(SUM2) AFUT
С		NUMERICAL INTEGRATION ALONG IMAGINARY AXIS BRANCH LINE
		IF(IOUT.NE.3) GU 10 403
		CALL AXIMAG(CON11, CON12, OMEGA, R)
		AR1 = AR1 - CONTI*FCT
		AR2 = AR2 - CONT2 + FCT
	403	CONTINUE
		RETURN
		END
		SUBROUTINE HANK(WVNO,R,H0,H1)
		COMPLEX HO. HI
		REAL JO. 11. J17
		7 - WVNOAR
	100	ir(7 GT 3 n) GO TO 200
	100	
		$\chi = (L/U_1) + (L/U_1)$
		$J_0 = 1, -\chi_{0}(2, 2479997 - \chi_{0}(1, 2000200 - \chi_{0}(1, 3103000 - \chi_{0}(1, 3103000) - \chi_{0}(1, 3103000) - \chi_{0}(1, 3103000) - \chi_{0}(1, 3103000 - \chi_{0}(1, 3103000) - \chi_{0}(1, 310300) - \chi_{0}($
		1.0444479-X*(.0039444=X*(.0002100)))))
		J12 = U·5*X*(·50249762#X*(·21U905/3*X*(·U0924289*X*(
		1.00443319-X#(.00031/61-^*(.00001109))))))
		J1 = Z * J1Z
		$Y_0 = (2./3.141592/) * ALOG(0.5*Z) * J0 + 0.36746691 + X*($
		1.60559366-X*(.74350384-X*(.25300117-X*(.04261214-X*(

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```
2.00427916-X*(.00024846))))))
    Y1Z = (2./3.1415927)*Z*ALOG(0.5*Z)*J1 - 0.6366198+X*(
   1.2212091+X*(2.1682709+X*(-1.3164827+X*(.3123951+X*(
   2-.0400976+x*(.0027873)))))
    HO = CMPLX(JO, -YO)
    H1 = CMPLX(J1, -Y1Z/Z)
    RETURN
200 CONTINUE
    X = 3.7Z
    FAC = 1./SORT(Z)
    F0 = .79788456+X*(-.00000077 + X*(-.00552740 + X*(
   1-.00009512+X*(.00137237+X*(+.00072805+X*(.00014476))))
   2))
    T0 = 2 - .78539816+X*(-.04166397+X*(-.00003954+X*(
   1.00262573+X*(-.00054125+X*(-.00029333+X*(.00013558))))
   2))
    F1 = .79788456+X*(.00000156+X*(.01659667+X*(.00017105*
   1X*(-.00249511+X*(.00113653+X*(-.00020033))))))
    T1 = Z-2.35619449+X*(.12499612+X*(.00005650+X*(
   1 -.00637879*X*(.00074348+X*(.00079824*X*(-.00029166)))
   2)))
    J_0 = FAC + F0 + COS(T0)
    Y_0 = FAC + F_0 + SIN(T_0)
    J1 = FAC * F1 * COS(T1)
    Y1 = FAC + F1 + SIN(T1)
    HO = CMPLX(JO, -YO)
    H1 = CMPLX(J1, -Y1)
    RETURN
    END
    SUBROUTINE IHANK(X, H0, H1, SUM)
    COMPLEX HO, H1, SUM
    REAL IJO, IYO
    IF(X.GT.5.0) GO TO 1000
    IF(X.GT.2.0) GO TO 101
    1J0=1,49457E-5+X*(.9994805+X*(.0027178+X*(-.0884971+
        X*(.0042605+X*(.0017411))))
   ð
    GO TO 200
101 IF(X.GT.4.0) GO TO 102
    1J0=0.1680514+x*(.6216918+X*(.3516254+X*(-.2553154+
        x*(.0458084+x*(-.0025809)))))
    GO TO 200
102 IJ0=-4.093215+X*(5.493378+X*(-1.870851+
        X*(.2501106+X*(-.0114415))))
200 IF (X.GT.0.5) GO TO 201
```

C

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C C

```
IY0=X*(-2,983395+X*(10,69899+X*(-30,65599+
        X*(48,83985+X*(-30.89077)))))
    8
     GO TO 999
201 IF(X.GT.1.0) GO TO 202
     Iv0=-0.0851148+X*(-1.649919+X*(1.878571+
        X*(-1,218732+X*(,5532593+X*(-,1151309)))))
   8
     GO TO 999
202 TF(X.GT.3.0) GO TO 203
     TY0=-,2089732+x*(-1.081949+x*(.7960879+x*(-.1464996+
         X*(,0037485+X*(.0005744))))
203 IY0=.9766188+X*(-2.799556+X*(1.780798+X*(-.4238574+
        x*(.0416846+x*(-,0013983))))
999 CONTINUE
     SUM=CMPLX(IJ0,-IY0)
     RETURN
1000 Z=1./X
     Sp=-3,08168E-7+Z+(.6366825+Z+(-.0004799+
        Z*(-.6797933+Z*(.889303)))
     S1=+6366201+Z*(-6,88024E-5+Z*(.639624+
        Z*(-.0508577+Z*(-1.689329+Z*(2.711393))))
    ÷.
    SD=SO-AIMAG(H0)
     S1=S1-AIMAG(H1)
     SUM=X*(H0+1.57079633*(S0*H1-S1*H0))
     RETURN
    END
     SUBROUTINE AXIMAG(SM1, SM2, OMEGA, R)
     THIS PERFORMS BRANCH LINE INTEGRATION ALONG THE IMAGIN
     THE INTEGRATION IS PERFORMED BY LAGUERRE S RULE AND IS
     R.GT. 0.5 H , WHERE H IS THE SOURCE DEPTH
     TO IMPROVE THE EVALUATION NOTE THAT BMODO AND BMOD1 AR
     OMEGA, HENCE THIS FUNCTION CAN BE COMBINED WITH THE WE
     AN EARLY INTIALIZATION.
     COMPLEX G1,G2
     DIMENSION X(24), W(24)
    DATA (X(I), I=1,24)/0.02110687,0,11122305,0,27339875,
    10.50775546,0.81442137,1,1935599,1,6453733,2,1701028,
    22.7680303,3.4394792,4.1848148,5.0044459,5#8988261;
   36.8684550.7.9138802.9.0356983.10.234558.11.511161.
    412.866265,14.300688,15.815308,17.411070,19.088986,
   520.850141/, (W(I),I=1,24)/.05303710.0.11284582,
   60.15082452,0.16279133,0.15185641,0.12593625,.09419893,
   70.64078814E-01,0.39845646E-01,0.22724136E-01,
   80.11912235E-01,0.57483106E-02,0,25559349E-02,
   9.10478123E-02, 39617000E-03, 13816206E-03,
```

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A.44439761E-04,.13180466E-04,.36033694E-05.
     B.90760433E-06, 21049269E-06, 44918756E-07,
     C.88129729E-08, 15882974E-08/
      TWOPI = 0.63661977
      SM1 = 0.0
      SM2 = 0.0
      DO 100 II = 1.24
      \dot{1} = 25 - 11
      THE FIRST 24 TERMS OF AN N=68 GAUSS-LAGUERRE INTEGRAL
С
      APPROXIMATION ARE USED. THE ERROR IN DROPPING THE.
C
      HIGHER TERMS SHOULD BE LESS THAN 1,0E-09
С
      TAU = X(I)/R
      Z = X(I)
      CALL SHCFIK(G1,G2,OMEGA,TAU)
      CALL BESMOD(BMOD0, BMOD1, Z)
      SM1 = SM1 + AIMAG(G1) * BMODO * W(I)
      SM2 = SM2 + REAL(G2) + BMOD1 + W(I)
  100 CONTINUE
      SM1 = - TWOPI * SM1 / (R*R)
              TWOPI + SM2 / (R+R)
      SM2 =
      RETURN
      END
      SUBROUTINE SHOFIK(G1,G2,OMEGA,TAU)
      THIS ROUTINE EVALUATES THE G1 AND G2 COEFFICIENTS FOR
C
      A PURELY IMAGINARY WAVENUMBER
C
      COMMON / MODEL / D(15), A(15), B(15), RHO(15), MMAX
      COMMON/SOURCE/DEPTH, LMAX, DPH
      COMPLEX G1,G2
      COMPLEX EJ11, EJ21, EL11, EL12, EL21, EL22, FL, E1, E2
      A11 = 1.0
      A12 = 0.0
      A21 = 0.0
      A22 = 1.0
      ED11 = 1.0
      ED12 = 0.0
      En21 = 0.0
      ED22 = 1.0
      E22 = -1./(B(MMAX) + B(MMAX))
      XKB = OMEGA/B(MMAX)
      E111 = SQRT(TAU+TAU+XKB+XKB)+RHO(MMAX)
      E11R = 0.0
      TO AVOID NUMERICAL PROBLEMS. MATRIX MULTIPLICATION
C
С
      GOES FROM BOTTOM LAYER UPWARD
      MMM1 = MMAX - 1
```

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```
DO 1340 K = 1, MMM1
     M = MMAX - K
     XKB = OMEGA/B(M)
     RB = SQRT(TAU+TAU + XKB+XKB)
     Q = D(M) + RB
     H = \dot{R}HO(M) + B(M) + B(M)
     IF(RB,EQ.0.0) GO TO 1401
     COSQ = COS(Q)
     SINQ = SIN(Q)
     Y = SINQ/(H*RB)
     Z = -H + RB + SINQ
     GO TO 1402
1401 Y = D(M)/H
     Z = 0.0
     COSQ = 1.0
1402 CONTINUE
     EA11 = A11 + COSQ + A12 + Z
     EA12 = A11 + Y + A12 + COSQ
     EA21 = A21 * COSQ + A22 * Z
     EA22 = A21 * Y + A22 * COSQ
     A11 = EA11
     A12 = EA12
     A21 = EA21
     A22 = EA22
     L1 = LMAX + 1
     IF(L1.NE.M) GO TO 1340
     ED11 = A11
     ED12 = A12
     ED21 = A21
     ED22 = A22
1340 CONTINUE
     H = RHO(LMAX) * B(LMAX) * B(LMAX)
     XKB = OMEGA / B(LMAX)
     RB = SQRT(TAU*TAU + XKB*XKB)
     Q = DPH + RB
     IF(RB,EQ.0.0) GO TO 1501
     COSQ = COS(Q)
     SING = SIN(Q)
     \ddot{Y} = SINQ/(H^{+}R^{-}B)
     Z = -H + RB + SINQ
     GO TO 1502
1501 CONTINUE
     Y = D^{P}H/H
     Z = 0.0
     CoSQ = 1.0
```

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```
1502 CONTINUE
      D11 = (ED11 + COSQ + ED12 + Z)/RHO(LMAX)
      D12 =- (ED11 * Y + ED12 * COSQ) *B(LMAX) *B(LMAX)
      D_{21} = (ED_{21} * C^{0}SQ + ED_{22} * Z)/RHO(LMAX)
      D22 =-(ED21 * Y + ED22 * COSQ)*B(LMAX)*B(LMAX)
      E1 = CMPLX(E11R,E11I)
      E2 = CMPLX(E22,0.0)
      EJ11 = E1 + A11
      E_{J21} = E_{2} + A_{21}
      F|11 = E1 + D11
      EL12 = E1 + D12
      E|21 = E2 + D21
      EL22 = E2 + D22
      FL = EJ11 - EJ21
      G_1 = (EL_{21} - EL_{11}) / FL
      G2 = (EL22 - EL12) * CMPLX(0.0, TAU) / FL
      RETURN
      END
      SUBROUTINE BESMOD(BMOD0, BMOD1, Z)
      THIS SUBROUTINE EVALUATES THE FUNCTIONS
C
         BMODO = Z * EXP(Z) * KO(Z)
         BMOD1 = Z + EXP(Z) + K1(Z)
      WHERE KO AND K1 ARE THE MODIFIED BESSEL FUNCTIONS
C
      DIMENSION T(11), U(11), V(11)
      DATA (T(I), I=1,11)/0,0,0.05,0,1,0,2,0,3,0.4,0.5,0,6,
     11.,1.5,2./, (U(I),I=1,11)/0.0,0,163695,0,268232,
     20.428151,0.555788,.665073,.762055,.8500425,1.144463,
     31.437315,1.683136/, (V(1), I=1, 11)/1.0,1.046523,
     41.089018,1.166677,1.237547,1.303469,1.3655048,
     51.424352,1.63615349,1.86474881,2.1349418/
      IF(Z.GT.0.0) GO TO 100
      BMODO = 0.0
      BMOD1 = 1.0
      RETURN
  100 IF(Z,GE,2.0) GO TO 200
      IN THIS RANGE OF FUNCTIONAL, LINEAR INTERPOLATION IS
C
C
      ALL RIGHT
      DO 150 I = 1,10
      1J = 1
      IF(Z.GT.T(I).AND.Z.LE.T(I+1))
                                        GO TO 151
  150 CONTINUE
  151 CONTINUE
      BMOD0=U(IJ)+(Z-T(IJ))+(U(IJ+1)-U(IJ))/(T(IJ+1)-T(IJ))
      BMOD1=V(IJ)+(Z-T(IJ))*(V(IJ+1)-V(IJ))/(T(IJ+1)-T(IJ))
```

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```
RETURN
  200 CONTINUE
      X = 2.72
      BMOD0 = SQRT(Z)*(1,25331414+X*(-,07832358+X*(.02189568
     1+X*(-,01062446+X*(.00587872+X*(-.00251540+X*(.00053208
     2))))))
      BMOD1 = SQRT(Z)*(1.25331414+X*(.23498619+X*(-.03655620
     1+x+(.01504268+x+(-,00780353+x+(,00325614+x+(-,00068245
     2))))))
      RETURN
      END
      SURROUTINE SRCMOD
C
      READ IN EARTH MODEL
      COMMON / MODEL / D(15), A(15), B(15), RHO(15), MMAX
      DO 20 I = 1,15
      READ(60,1) D(I),A(I),B(I),RHO(I)
    1 FORMAT(4F10.3)
      MMAX = I
      IF(D(I), LE.0.0) GO TO 21
   20 CONTINUE
   21 CONTINUE
      MMX1 = MMAX - 1
      PRINT 2
    2 FORMAT(1H0,7X,1HD, 9X,1HA,9X,1HB,9X,3HRH0/)
      \ddot{D}O 400 I = 1,MMX1
    3 FORMAT(1H ,4F10,2)
  400 PRINT 3, D(1), A(1), B(1), RHO(1)
      PRINT 5, A (MMAX), B (MMAX), RHO (MMAX)
    5 FORMAT(1H ,10X,3F10,2/1H0)
      RETURN
      END
      SUBROUTINE SRCLYR
      COMMON / MODEL / D(15), A(15), B(15), RHO(15), MMAX
      COMMON/SOURCE/DEPTH, LMAX, DPH
C
      LMAX = SOURCE LAYER
      DEPTH = SOURCE DEPTH
       DPH = HEIGHT OF SOURCE ABOVE LMAX + 1 INTERFACE
C
      LMAX = 0 IS THE FREE SURFACE
      DEP = 0.0
      MMX1 = MMAX - 1
      DO 100 M = 1, MM \times 1
      \dot{D}EP = DEP + D(M)
      DPH = DEP - DEPTH
```

С

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```
LMAX = M
    IF(DPH.GE.0.0) GO TO 101
100 CONTINUE
101 CONTINUE
    RETURN
    END
    SUBROUTINE RSHOF(GG1,GG2,FL,OMEGA,WVNO,EXE,EXL)
    COMPLEX EJ11, EJ21, EL11, EL12, EL21, EL22, E1, E2, FL, GG1, GG2
    CALL SHCOEF(A11,A12,A21,A22,D11,D12,D21,D22,E11R,E111,
   1E22, OMEGA, WVNO, EXE, EXL)
    E_1 = CMPLX(E_{11R}, E_{11I})
    E_2 = CMPLX(E_{22}, 0, 0)
    E_{J11} = E_{1} + A_{11}
    E_{J21} = E_{2} + A_{21}
    EL11 = E1 + D11
    EL12 = E1 + D12
    EL21 = E2 + D21
    E_{L22} = E_{2} + D_{22}
    GG1 = (EL21 - EL11)
    GG2 = (EL22 - EL12) + WVNO
    FL = EJ11 - EJ21
    RETURN
    END
    SUBROUTINE SHCOEF (A11, A12, A21, A22, D11, D12, D21, D22, E11R
   1, E111, E22, OMEGA, WVNO, EXE, EXL)
    COMMON / MODEL / D(15), A(15), B(15), RHD(15), MMAX
    COMMON /SOURCE/ DEPTH, LMAX, DPH
     SINCE THIS IS WRITTEN FOR A MACHINE WHOSE LARGEST
    NUMBER IS 1,0E+39, SPECIAL NORMALIZATION IS USED TO
    AVOID EXPONENT OVERFLOW OR UNDERFLOW
    A11 = 1.0E - 20
    A21 = 0.0
    A12 = 0.0
    A22 = 1.0E - 20
    ED11 = 1.0E - 20
    ED12 = 0.0
    ED21 = 0.0
    ED22 = 1.0E-20
    E X E = 0.0
    EXL = 0.0
    MANOS = MANO*MANO
    E_{22} = -1./(B(MMAX) * B(MMAX))
    XKB = OMEGA/B(MMAX)
```

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```
RB = SQRT(ABS(WVNO2-XKB*XKB))
      E11R = 0.0
      E111 = 0.0
      FAC = RHO(MMAX)*RB
      IF(WVNO.GT.XKB) E11R=FAC
      IF(WVNO.LT.XKB) E11I = FAC
      TO AVOID NUMERICAL PROBLEMS, MATRIX MULTIPLICATION
C
      GOES FROM BOTTOM LAYER UPWARD
C
      MMM1 = MMAX - 1
      DO 1340 K = 1.MMM1
      M = MMAX - K
      XKB = OMEGA/B(M)
      RB = SQRT(ABS(WVNO2 - XKB*XKB))
      Q = D(M) + RB
      H = RHO(M) * B(M) * B(M)
      IF (WVNO-XKB)1231,1221,1209
 1231 SING = SIN(G)
      \vec{Y} = SINQ/(H*RB)
      Z = -H * RB * SINQ
      COSQ = COS(Q)
      GO TO 1242
 1221 \text{ COSQ} = 1.0
      \ddot{Y} = D(M)/H
      Z = 0.0
      GO TO 1242
 1209 TF(0.GT.5,0) GO TO 1208
      EXOP = EXP(Q)
      EXQM = 1./EXQP
      SING = (EXOP - EXOM)/2.
      Y = SINQ/(H + RB)
      Z = SING + H + RB
      COSQ = (EXQP + EXQM)/2.
      GO TO 1242
 1208 EXE = EXE + Q
      Z = 0.5 \text{+}H \text{+}RB
      Y = 0.5/(H*RB)
      Cosq = 0.5
 1242 CONTINUE
      EA11 = A11+COSQ + A12+Z
      EA12 = A11+Y + A12+COSQ
      EA21 # A21*COSQ + A22*Z
      EA22 = A21+Y + A22+COSQ
      À11 = EA11
      A12 = EA12
      A21 = EA21
```

```
A22 = EA22
     L1 = LMAX+1
     IF(L1, NE.M) GO TO 1340
     EXL = EXE
     ED11 = A11
     ED12 = A12
     ED21 = A21
     ED22 # A22
1340 CONTINUE
     H = RHO(LMAX) * B(LMAX) * B(LMAX)
     XKB = OMEGA/B(LMAX)
     RB = SQRT(ABS(WVN02-XKB+XKB))
     Q = DPH * RB
     IF(WVNO-XKB)1131,1121,1111
1131 SING = SIN(G)
     Y = SINQ/(H + RB)
     Z = -H * RB * SINQ
     COSQ = COS(Q)
     GO TO 1142
1121 COSQ = 1.0
     Y = DPH/H
     Z = 0.0
     GO TO 1142
1111 IF(0.GT.5.0) GO TO 1108
     EXQP = EXP(Q)
     EXQM = 1./EXQP
     SINQ = (EXQP - EXQM)/2.
     Y = SINQ/(H + RB)
     Z = SINQ + H + RB
     \cos \alpha = (\exp + \exp )/2.
     GO TO 1142
1108 EXL = EXL + Q
     Z = H*RB*0.5
     Y = 0.5/(H*RB)
     COSQ = 0.5
1142 CONTINUE
     \dot{n}11 = (ED11*COSQ + ED12*Z)/RHO(LMAX)
     D12 = - (ED11+Y + ED12+COSQ)+B(LMAX)+B(LMAX)
     D21 = (ED21*COSQ + ED22*Z)/RHO(LMAX)
     D22 = -(ED21*Y + ED22*COSQ)*(B(LMAX)*B(LMAX))
     RETURN
     END
```

APPENDIX B: COMPUTER PROGRAM SHVEL

Function

This program performs the inverse Fourier transform of Equation 9, using the source velocity pulse $s_2(t)$ of Equation 23. The source pulse, its Fourier amplitude spectrum and the filtered source pulse are plotted as output. The output of SHSPEC is read in on File 12, the pulse parameters are read from card on File 60, printer output is on File 61, CALCOMP off-line plots are on File 10, and the velocity time histories are on File 20 for use by the program DSVLAC.

The card input is very simple and is given below rather in a table:

Card	Variable Name	Columns	Format	Description
1	TL	1-10	F10.5	The pulse parameter τ of Equation 23.
	XMOM	11-20	E10.3	A scaling factor used to adjust source spectrum level. G1 and G2 are output from SHSPEC for a seismic moment of $1.0E+20$ dyne-cm since the area under $s_2(t)$ is unity. XMOM permits the use of another moment as well as the adjustment for focal mechanism. XMOM is the desired seismic moment times the terms in the square brackets of Equation 24. XMOM.LT.1 is interpreted as XMOM= $1.0E+20$

(More Card 1's are read until one with TL.LE.O is found, which causes program termination and closing of files). To generate Figure 19, TL=0.5 and XMOM=7.06E+22 were used (seismic moment of 3.53E+22 dynecm and a focal mechanism factor of 2.0).

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The printer output of SHVEL is mostly diagnostic. File 61 gives the values of TL, DT, and XMOM (DT is read from File 12). Under the system standard printer output (PRINT statement), YMAX and YMIN are the maximum and minimum amplitudes of each time plot; R, IOUT and TSHIFT are the parameters R, IOUT and TO written on File 12 by the program SHSPEC.

A description of the subroutines is given in Table B1. The program listing is given in Table B2.

Table Bl

Subroutine Description

Subroutine Name	Function
PULSE	Defines the source pulse of Equation 23. Other normalized source pulses can be used by rewriting this subroutine.
FOUR	Performs numerical approximation to the Fourier inte- gral by using a fast Fourier transform.
SEISPLT	Sets up a CALCOMP plot of ground motion time histories. Other plotters can be used by rewriting this subroutine.
SPPLT	Sets up log-log CALCOMP plot of Fourier amplitude spectra.
ALOGAXES	Sets up log-log axes for SPPLT.

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```
SHVEL PAGE 1
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```
Table B2
```

```
C
      PROGRAM SHVEL
      DIMENSION DATA(2048), X(1026), Y(1026), DATAS(1026)
      DIMENSION DATA1(2048)
      DIMENSION IBUF (1000)
С
      INPUT DATA
C
C
      CARD 1 TL. XMOM
      TL IS SOURCE PULSE PARAMETER, XMOM IS SEISMIC MOMENT
С
      IN DYNE-CM. IF XMOM=0 PROGRAM DEFAULTS TO 1.DE+20 D-CM
Ç
      .... MORE CARD 1 - USE TL.LT.O TO END CARD 1 SEQUENCE
C
      CALL PLOTS(IBUF,1000,10)
 9998 CONTINUE
      REWIND 12
      READ(12,1) DEPTH,FL,FU,DT,N,VRED
      NYQ = N/2 + 1
      NYQ2 = 2 * NYQ
      \tilde{D}\tilde{F} = 1./(N*D\tilde{T})
      N1 = FL/DF
      N2 = FU/DF
      READ(60,111) TL, XMOM
    1 FORMAT(4F10,5,15,F10,5)
   11 FORMAT(F10.5,215,2F10.5)
  111 FORMAT(F10,5,E10.3)
      NS = 2
      WRITE(20,11)TL, NS, N, DT, DEPTH
      IF(TL.LE.0.0) GO TO 9999
      WRITE(61,4) TL, DT, XMOM
    4 FORMAT(1H0,4HTL =,F10,5,5X,4HDT =,F10,5,5X,4HMOM=,
     1E10.3)
      XMOM = XMOM / 1.0E20
      IE(XMOM.LT.1.0E-20) XMOM = 1.0
      CALL PULSE(X,Y,N,DT,TL)
      CALL SEISPLT(X, Y, N, 0, 0, 0, 6HINPUT )
      PLOT SOURCE PULSE AND SPECTRA
С
      DO 200 I = 1,N
      J = 2 * I - 1
      K = 2 + I
      DATA(J) = Y(I)
  200 \text{ DATA(K)} = 0.0
      CALL FOUR(DATA, N, -1, DT, DF)
      D_0 205 I = 1, NYQ
      J = 2 * I - 1
      K = 2 * I
      IF(I.GE.N1.AND.I.LE.N2) GO TO 205
      DATA(J) = 0.0
```

SHVEL PAGE 2

```
DATA(K) = 0.0
  205 CONTINUE
      CALL SPPLT(DATA, X, Y, NYQ, DF, 6H SPEC )
      DO 206 I = 1, NYQ2
  206 DATAS(I) = XMOM + DATA(I)
      CALL FOUR (DATA, N, +1, DT, DF)
      D0 210 I = 1, N
      J = 2 * I - 1 
X(I) = (I+1) * DT
      Y(I) = DATA(J)
  210 CONTINUE
      PLOT FILTERED SOURCE PULSE
C
      CALL SEISPLT(X,Y,N,0.0,0,6H FILT )
 9997 CONTINUE
      READ(12,601)R, IOUT, TO
  601 FORMAT(E11.4, 15, E11.4)
      WRITE(20,601) R, IOUT, TO
      IF(R.LT.0.0) GO TO 9998
      PRINT 5, R, 10UT, TO
    5 FORMAT(1H0,4H R =,F8.2,8H IOUT =,I3,5X,10H TSHIFT =,
     1F8.2)
      READ(12,600) (DATA(1), I=1, NY02)
      READ(12,600)(DATA1(1),1=1,NY02)
  600 FORMAT(8E11.4)
      no 700 I = 1.NYQ
      J = 2*I - 1
      K = 2 + 1
      AR1 = DATA(J)
      \tilde{A}11 = DATA(K)
      AR2 = DATA1(J)
      \dot{A}I2 = DATA1(K)
      DATA(J) = DATAS(J)+AR1 - DATAS(K)+AI1
      DATA(K) = DATAS(K) + AR1 + DATAS(J) + AI1
      DATA1(J) = DATAS(J)+AR2 - DATAS(K)+A12
      DATA1(K) = DATAS(K)+AR2 + DATAS(J)+A12
      IF(I.EQ.1) GO TO 700
      \bar{1}\bar{1} = N + 2 - 1
      JJ = 2 * II - 1
      KK = 2 * 11
      DATA(JJ) = DATA(J)
      DATA(KK) = - DATA(K)
      DATA1(JJ) = DATA1(J)
      DATA1(KK) = - DATA1(K)
  700 CONTINUE
  303 CONTINUE
```

```
CALL FOUR(DATA, N, +1, DT, DF)
      CALL FOUR(DATA1,N,+1,DT,DF)
      DO 400 I = 1.N
      J = 2 + 1 - 1
      X(I) = DATA(J)
      Y(I) = DATA1(J)
  400 CONTINUE
      WRITE(20,600)(X(I),I=1,N)
      WRITE(20,600)(Y(I),1=1,N)
      GO TO 9997
 9999 CONTINUE
      CALL PLOT(12.0,0.0,999)
      STOP
      END
      SUBROUTINE PULSE(T, F, N, DT, TL)
      DIMENSION T(1), F(1)
      T1 = 0.0
      \tilde{T}2 = T1 + TL
      T3 = T2 + TL
      T4 = T3 + TL
      T5 = T4 + TL
      DO 100 I = 1.N
      T(1) = (1-1) + DT
      Y = T(I)
      Z = Y - T1
      F(I) = 0.0
      IF(Y.GT.T1) GO TO 101
      GO TO 100
  101 (F(Y.GT.T2) G0 T0 102
      F(I) = (Z/TL)*(Z/TL)*0.5
      GO TO 100
  102 IF(Y.GT.T3) GO TO 103
      F(I) = -(Z/TL)*(Z/TL)*0.5 + 2.0*(Z/TL) - 1.0
      GO TO 100
  103 IF(Y.GT.T4) GO TO 104
      F(I) = - (Z/TL)*(Z/TL)*0.5 + 2.0*(Z/TL) - 1.
      GO TO 100
  104 IF(Y.GT.T5) GO TO 105
      F(I) = (Z/TL)*(Z/TL) * 0.5 -4.0 * (Z/TL) + 8.0
      GO TO 100
  105 F(I) = 0.0
  100 CONTINUE
      AREA OF PULSE NORMALIZED TO UNITY
C
      DO 200 I = 1, N
```

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200 F(I) = F(I) /(2.*TL)
RETURN
END
```

4

SUBROUTINE FOUR (DATA, NN, ISIGN, DT, DF) THE COOLEY_TOOKEY FAST FOURIER TRANSFORM IN USASI BASIC FORTRAN TRANSFORM(J)=SUM(DATA(1)+W++(I-1)(J-1)). WHERE I AND J RUN FROM 1 TO NN AND W=EXP(ISIGN+2+PI+ SQRT(-1)/NN). DATA IS A ONE-DIMENSION AL GOMPLEX ARRAY (I.E., THE REAL AND IMAGINARY PARTS OF DATA ARE LOCATED IMMEDIATELY ADJACENT IN STORAGE, SUCH AS FORTRAN IV PLACES THEM) WHOSE LENGTH NN IS A POWER OF TWO, ISIGN IS +1 OR -1, GIVING THE SIGN OF THE TRANSFORM VALUES ARE RETURNED IN ARRAY TRANSFORM, DATA, REPLACING THE INPUT DATA. THE TIME IS PROPOR-TIONAL TO NOLOG²(N), RATHER THAN THE USUAL Nov2 RMS RESOLUTION ERROR BEING BOUNDED BY 6*SORT(1)* LOG2(NN)+2++(-B), WHERE B IS THE NUMBER OF BITS IN THE FLOATING POINT FRACTION. PROGRAM AUTOMATIGALLY TAKES INTO ACCOUNT DIMENSIONALITY DIMENSION DATA(1) N = 2 * NNIF(DT, EQ.0.0) DT = 1./(NN*DF)IF(DF, EQ.0.0) DF = 1./(NN+DT) $\tilde{I}\tilde{F}(DT,NE.(NN+DF))$ DF = 1./(NN+DT) J = 1no 5 I=1,N,2 IF(I-J)1,2,2 1 TEMPR = DATA(J)TEMPI = DATA(J+1) $\tilde{D}ATA(J) = DATA(I)$ DATA(J+1) = DATA(I+1)DATA(1) = TEMPRDATA(I+1) = TEMPI2 M = N/23 IF(J-M) 5,5,4 4 J = J = MM = M/2İF(M-2)5,3,3 5 J=J+M MMAX = 26 IF (MMAX-N) 7,10,10 7 ISTEP= 2 *MMAX THETA = 6.283185307/FLOAT(ISIGN+MMAX) SINTH#SIN(THETA/2.)

```
WSTPR=-2.*SINTH*SINTH
      WSTPI=SIN(THETA)
      WR=1.0
      W1=0.0
      DO 9 M=1, MMAX, 2
      DO 8 I=M,N,ISTEP
      J=I+MMAX
      TEMPROWRODATA(J)-WIODATA(J+1)
      TEMPI=WR*DATA(J+1)+WI*DATA(J)
      DATA(J)=DATA(I)-TEMPR
      DATA(J+1)=DATA(I+1)-TEMPI
      DATA(I)=DATA(I)+TEMPR
    8 DATA(I+1) = DATA(I+1) + TEMPI
      TEMPR = WR
      WR = WR*WSTPR-WI*WSTPI + WR
    9 WI = WI*WSTPR+TEMPR*WSTPI + WI
      MMAX = ISTEP
      GO TO 6
   10 CONTINUE
      IF(ISIGN.LT.0) GO TO 1002
C
      FREQUENCY TO TIME DOMAIN
      DO 1001 IIII = 1, N
 1001 DATA(IIII) = DATA(IIII) + DF
      RETURN
 1002 CONTINUE
      TIME TO FREQUENCY DOMAIN
C
      DO 1003 IIII = 1.N
 1003 DATA(IIII) = DATA(IIII) + DT
      RETURN
      END
      SUBROUTINE SEISPLT(X,Y,N,DIST, ID, SYM)
      CHARACTER SYM
      DIMENSION X(1),Y(1)
      CALL PLOT(0,0,-11,0,-3)
      CALL PLOT(0,0,2.0,-3)
      YMIN = 1.0E+38
      Y_{MAX} = -1.0E + 38
      DO 100 I = 1.N
      IF(Y(I),GT,YMAX) YMAX = Y(I)
      IF(Y(I).LT.YMIN) YMIN = Y(I)
 100 CONTINUE
      IF(ID.GT.O) PRINT 1,YMAX,YMIN,DIST
IF(ID,EQ.O) PRINT 2,YMAX,YMIN
    1 FORMAT(1H ,6HYMAX =,E10,3,10H
                                          YMIN = , E10.3, 3X
```

```
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```

```
16HDIST = ,F6,1)
   2 FORMAT(1H ,6HYMAX =, E10, 3, 10H YMIN = , E10.3)
     IF (ABS(YMIN).GT.YMAX) YMAX = ABS(YMIN)
     X(N+1) = +5.0
     X(N+2) = 15.
     Y(N+1) = - YMAX
     Y(N+2) = 2, \# YMAX
     CALL AXIS(0,25,0.0,10HT - X/4,67 ,-10,5,0,90,0,X(N+1)
    1, x(N+2)
                                 ,1,1,0,180,0,Y(N+1),Y(N+2))
     CALL AXIS(0,0,-0.25,1H
     Y(N+2) = - Y(N+2)
     CALL LINE(Y,X,N,1,0,0)
     IF(ID,GT.0) CALL NUMBER(-0,75,4,5,0,14,DIST,90.0,-1)
     CALL SYMBOL(-1.0,-1.5,0.14,SYM,0.0,+6)
     CALL PLOT(3.0,0,0,-3)
     RETURN
     END
     SUBROUTINE SPPLT(DATA, X, Y, NP, DF, SYM)
     THIS PLOTS AMPLITUDE SPECTRA ON 2 X 3 CYCLE LOG-LOG
     SCALE
     DIMENSION DATA(1), Y(1), X(1)
     CHARACTER TTLX(2), TTLY(2)
     CHARACTER SYM
     CALL PLOT(0,0,-11,0,-3)
     CALL PLOT(0.0,2.0,-3)
     XMIN = 0.1
     XMAX = 10.
     YMAX = 1.0E - 38
     j = 0
     THE ZERO FREQUENCY POINT IS NOT PLOTTED
     DO 5700 I = 2.NP
     <u>j</u> = J + 1
     X(J) = (I-1) + DF
     IF(X(J),LT,XMIN) X(J) = XMIN
     \overline{IF}(X(J).GT, XMAX) X(J) = XMAX
     K = 2 + I - 1
      = 2 + 1
     Y(J) = SORT(ABS(DATA(K)*DATA(K) + DATA(L)*DATA(L)))
     IF(Y(J),GT,YMAX) YMAX = Y(J)
5700 CONTINUE
     \dot{Y}Y = ALOGIO(YMAX)
     L\tilde{Y} = YY
     YY=LY
     IF(YY,GT,LY) YY = LY + 1
```

C C

C

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```
YMIN = 10.**(YY - 3.)
      YMAX = 10. ++YY
     N = J
     DO 5701 I = 1.N
     IF(Y(I).LT.YMIN) Y(I) = YMIN
5701 CONTINUE
     XAXLEN = 3.732
     \tilde{Y}_{A}XLEN = 5.598
     DELTAX = 2./XAXLEN
     DELTAY = 3./YAXLEN
     X1 = ALOG10(XMIN)
     NOCX = 2
     NOCY = 3
     \dot{Y}_1 = \dot{Y}\dot{Y} - NOC\dot{Y}
     TTLX(1)=6HFREQ (
     TTLX(2) = 6HHZ)
     TTLY(1) = 6HAMP (C
     TTLY(2) = 6HM-SEC)
     MTX = 12
     MTY = 12
     CALL ALOGAXES (XAXLEN, YAXLEN, NOCX, NOCY, TTLX, TTLY, MTX,
    IMTY (X1, Y1, DELTAX, DELTAY)
     DO 5703 I = 1, N
     Y(I) = ALOG10(Y(I))
5703 X(I) = ALOG10(X(I))
     X(N+1) = X1
     X(N+2) = DELTAX
     Y(N+1) = Y1
     Y(N+2) = DELTAY
     CALL LINE (X.Y.N.1,0.0)
     CALL SYMBOL (0.0,-1.0,0.14, SYM,0.0,+6)
     CALL PLOT(10.0,0.0,-3)
     RETURN
     END
     SUBROUTINE ALOGAXES(XAXLEN,YAXLEN,NOCX,NOCY,TTLX,TTLY,
    1MTX, MTY, X1, Y1, DELTAX, DELTAY)
     CHARACTER TTLX(1), TTLY(1)
     SLT = 0.02+YAXLEN
     SST = 0.01 + YAXLEN
     SP = -0.06 + YAXLEN
     SS = 0.035 + YAXLEN
     SSP = SP + SS - 0.06
     TTLP = -0.11 + YAXLEN - 0.1
     STTL = 0.035+YAXLEN
```

B-10

```
XNUM = 1
  Y_1 = Y_1
  YU = Y1 + ANDCY
  IF (ABS(YL).GE.10. .OR. ABS(YU).GE.10. )XNUM = XNUM +1.
  IF(ABS(YL).GE.100..OR. ABS(YU).GE.100.)XNUM = XNUM +1.
  IF(Y1,LT,O) XNUM = XNUM + 1.0
  CALL PLOT(-SLT,0.0,2)
  CALL PLOT(0.0,-SLT,3)
  CALL PLOT(0.0.0.0.2)
  XPO = X1
  YPO = Y1
  FE (NOCX.EQ.0) GO TO 4
  ANOCX = NOCX
  FACTX = XAXLEN/ANOCX
  CALL SYMBOL (-, 6*SS, SP, SS, 2H10, 0, 0, 2)
  CALL NUMBER(999., SSP, 0.6*SS, X1, 0.0, -1)
  CALL PLOT(0.0.0.0.3)
  DO 3 J = 1, NOCX
  DO 2 I = 1.10
  \mathbf{X} = \mathbf{I}
  X = ALOG10(X) *FACTX + (J-1)*FACTX
  IF(I.EQ.1)G0 TO 2
  CALL PLOT(X:0.0.2)
  CALL PLOT(X,-SST,2)
2 CALL PLOT(X,0.0,3)
  CALL PLOT(X,-SLT,2)
  CALL SYMBOL(X-.6+SS, SP, SS, 2H10, 0.0;2)
  XP0 = XP0 + 1.0
  CALL NUMBER(999,,SSP,0,6*SS,XP0,0,0,-1)
3 CALL PLOT(X,0.0,3)
  XTL = MTX
  XTL = (XAXLEN-XTL*STTL)/2.0
  CALL SYMBOL (XTL, TTLP, STTL, TTLX, 0.0, MTX)
  GO TO 6
4 CALL AXIS(0,0,0,0,TTLX,-MTX,XAXLEN;0.0,X1;DELTAX)
6 CALL PLOT(0,0,0,0,3)
  IF (NOCY.EQ.0) GO TO 10
  ANOCY = NOCY
  SP = SP - (XNUM - 1.5) * 0.5 * SS
  TTLP = TTLP - (XNUM-1.) +0.5+SS
  FACTY = YAXLEN/ANOCY
  CALL SYMBOL(SP-0.4,-0.5*SS,SS,2H10,0.0,2)
  CALL NUMBER(999,,,5*SS-.06,,6*SS,Y1,0.0,-1)
  CALL PLOT(0,0,0,0,3)
  DO 9 J = 1, NOCY
```

SHVEL PAGE 9

```
DO 8 I = 1,10
   Ϋ́= Ι
   Y = ALOG1O(Y) * FACTY + (J-1)*FACTY
   IF(I.EQ.1)60 TO 8
   CALL PLOT(0,0,Y,2)
   CALL PLOT(-SST, Y, 2)
 8 CALL PLOT(0.0, Y.3)
   CALL PLOT(-SLT, Y, 2)
   CALL SYMBOL (SP-.4, Y-.5+SS, SS, 2H10,0,0,2)
   YPO = YPO + 1
   CALL NUMBER(999., Y+., 5*SS-, 06,, 6*SS, YP0, 0.0, +1)
 9 CALL PLOT(0,0,Y,3)
   YTL=MTY
   YTL = (YAXLEN-YTL+STTL)/2.0
   CALL SYMBOL (TTLP-,2,YTL, STTL, TTLY, 90., MTY)
   RETURN
10 CALL AXIS(0.0,0,0,TTLY,MTY,YAXLEN,90.,Y1,DELTAY)
   RETURN
```

END

APPENDIX C: COMPUTER PROGRAM DSVLAC

Function

This self-contained program takes the velocity time series computed by the program SHVEL, plots the displacement, velocity and acceleration time histories and also prepares an output file for use by the program SDSVSA. Input is from File 20, generated by SHVEL. CALCOMP output for off-line plotting is on File 10. File 21 contains data for use by the program SDSVSA. Printer output is through the PRINT statement and consists of the following for each source pulse:

Line 1 TL,NS,N,DT,DEPTH where the variables are as described for SHSPEC and SHVEL, except that NS indicates the number of focal mechanisms for each distance (NS=2 here since G1 and G2 traces are plotted)

Line 2 R, IOUT, TO

Line 3 SYM, YMAX, YMIN, R (tabulation of trace extrema. D1 is G1 displacement, D2 is G2 displacement, V1 is G1 velocity, A1 is G1 acceleration history, etc.)

Line 3 repeats 3*NS times.

The subroutines are only three: SEISPLT plots the time traces; DISP calculates displacement time histories by trapezoidal rule; and ACCL calculates acceleration time histories by assuming linear velocity segments.

The program DSVLAC is given in Table C1.

C-1

Table Cl

DSVLAC PAGE 1

C C C	PROGRAM DSVLAC THIS TAKES VELOCITIES GENERATED BY AND PLOTS ALL THREE DIMENSION IBUF(1000)	SHVEL	AND	COMPUTES	
	DIMENSION V(1026),D(2050),T(2050) CHARACTER ID(2),IV(2),IA(2) ID(1) = 6H D1 ID(2) = 6H D2				
	V(1) = 6H V1 V(2) = 6H V2 IA(1) = 6H A1				
	IA(2) = 6H A2 REWIND 20 REWIND 21				
1 600	CALL PLOTS(IBUF,1000,10) FORMAT(F10.5,215,2F10,5) FORMAT(8E11,4)				
9998	CONTINUE READ(20,1)TL,NS,N,DT,DEPTH WRITE(21.1) TL,NS,N,DT,DEPTH				
9997	IF(TL,LE.0.0) GO TO 9999 PRINT 1,TL,NS,N,DT,DEPTH CONTINUE				
	READ(20,601) R,IOUT,TO WRITE(21,601)R,IOUT,TO IF(R.LT,0.0) GO TO 9998 PRINT 601, R,IOUT,TO DO 9996 L = 1.NS				
	READ(20,600) (V(I),I=1,N) CALL DISP(V ,DT,N,T,D) CALL SEISPLT(T,D,N,R,1,ID(L),DMAX)				
	CALL SEISPLT(T,V,N,R,1,IV(L),VMAX) CALL ACCL(V,DT,N,M,T,D) CALL SEISPLT(T,D,M,R,1,IA(L),AMAX) WRITE(21,604) AMAX,VMAX,DMAX				
604	FORMAT(3E11,4) WRITE(21,600)(V(I),I=1,N)				
9996	CONTINUE GD TO 9997				
9999	CONTINUE CALL PLOT(1 ² .0,0.0,999) STOP END				
	SUBROUTINE SEISPIT(X.Y.N.DIST.ID.S	YM.YMAX	()		

C-2
```
CHARACTER SYM
    DIMENSION X(1), Y(1)
    CALL PLOT(0.0,-11.0,-3)
    CALL PLOT(0,0,2.5,-3)
    YMIN = 1.0E + 38
    YMAX = -1.0E+38
    DO 100 I = 1.N
    IF(Y(I),GT,YMAX) YMAX = Y(I)
    \dot{I}\dot{F}(Y(I),L\dot{T},YMIN) YMIN = Y(I)
100 CONTINUE
    IF(ID.GT.D) PRINT 1, SYM, YMAX, YMIN, DIST
    IF(ID, EQ. 0) PRINT 2, YMAX, YMIN
  1 FORMAT(1H , A6, 6HYMAX =, E10.3, 10H
                                          YMIN = E10.3.3X,
   16HDIST =, F6.1)
  2 FORMAT(1H ,6HYMAX =, E10,3,10H
                                       YMIN = E10.3
    IF (ABS (YMIN). GT. YMAX) YMAX = ABS (YMIN)
    X(N+1) = -5.0
    X(N+2) = 15.
    Y(N+1) = - YMAX
    Y(N+2) = 2. + YMAX
    CALL AXIS(0,25,0,0,10HT - X/4,67 ,-10,5.0,90.0,X(N+1)
   1, X(N+2))
                                ,1,1,0,180:0,Y(N+1),Y(N+2))
    CALL AXIS(0,0,-0.25,1H
    Y(N+2) = -Y(N+2)
    CALL LINE(Y, X, N, 1, 0, 0)
    IF(ID.GT.0) CALL NUMBER(-0.75,4,5,0,14,DIST,90.0,-1)
    CALL SYMBOL(-1.0,-1.5,0.14, SYM,0.0,+6)
    CALL PLOT(3,0,0,0,-3)
    RETURN
    END
    SUBROUTINE DISP(V, DT, N, T, D)
    DIMENSION V(1), T(1), D(1)
    D(1) = 0.0
    SUM=0.0
    DO 100 I = 2, N
    T(I) = (I-1) + DT
    SUM = SUM + 0.5 + DT + (V(I)+V(I-1))
    D(1) = SUM
100 CONTINUE
    RETURN
    END
    SUBROUTINE ACCL (V, DT, N, M, T, A)
    DIMENSION V(1), T(1), A(1)
```

DSVLAC PAGE 3

```
M = 2#N
    NM1 = N - 1
    DO 100 I = 1,NM1
    DIF = (V(I+1)-V(I))/DT
    J = 2*I - 1
    K = 2 * I
    T(J) = (1-1) * DT
    T(K) = I + DT
    A(J) = DIF
    A(K) = DIF
100 CONTINUE
    DIF = (V(1) - V(N))/DT
    J = 2*N - 1
    K = 2^{*}N
    T(J) = (N-1) + DT
    T(K) = N + DT
    A(J) = DIF
A(K) = DIF
    RETURN
    END
```

APPENDIX D; COMPUTER PROGRAM SDSYSA

Function

This program used the output of DSVLAC to compute the response spectra of each trace using Equations 30 and 31. The input is on File 21 generated by the program DSVLAC. Off-line CALCOMP graphic output is on File 10. Printer output is through the use of the PRINT statement. The output consists of a plot of the response spectrum as well as a listing of the response spectrum values, including SD, SV, SA, PSV and the Fourier spectrum FS, for damping values of 0, 2, 5 and 10 percent critical and oscillator periods from DT to 100 sec (it is meaningless to compute the response for periods less than the sampling interval).

The subroutines are MOTION which performs the computations for each input time history, SVLOG which performs the logarithmic plot and AMATRIX which computes the matrix elements of Equation 30.

The program listing is given in Table D1.

Table D1

```
C
      PROGRAM SD, SV, SA, PSV, FS
      DIMENSION VEL (1024), TMAX(3)
      DIMENSION IBUF(1000)
      CHARACTER SYM(2)
      CALL PLOTS(IBUF, 1000, 10)
      REWIND 21
      SYM(1) = 6HG1
      SYM(2) = 6HG2
  100 READ(21,1000) TL,NS,N,DT,DEPTH
      IF( TL.LE.0.0 ) GO TO 300
      CALL AMATRIX(N,DT)
  105 CONTINUE
      READ(21,1100) R, IOUT, TO
      IF( R.LT.0.0 ) GO TO 100
      Do 200 I1=1.NS
      READ(21,1200) (TMAX(1),1=1,3)
      READ(21,1300) (VEL(I), 1=1,N)
      CALL MOTION(VEL, TMAX, SYM(11), R, DEPTH)
  200 CONTINUE
      GO TO 105
  300 CALL PLOT(10,0,0,0,999)
 1000 FORMAT(F10,5,215,2F10.5)
 1100 FORMAT(E11.4, 15, E11,4)
 1200 FORMAT(3E11,4)
 1300 FORMAT(8E11,4)
      STOP
      END
      SUBROUTINE MOTION(VEL, TMAX, SYM, R, DEPTH)
C
   THIS PROGRAM TAKES THE VELOCITY GENERATED AND FINDS
C
   SD, SV, SA, PSV, FS BY THE MODIFIED NIGAM-JENNINGS METHOD
C
   THE INBUT VELOCITY GRID POINTS ARE CONNECTED BY LINEAR
C
C
      SEGMENT
С
       VEL = VELOCITY GENERATED, USED AS INPUT
C
Ċ
       SYM = NAME OF THE INPUT VELOCITY
C
         R = EPICENTER DISTANT
     DEPTH = SOURCE DEPTH
C
C
      DIMENSION VEL(1), TMAX(1)
      DIMENSION SD(49,4), SV(49,4), SA(49,4), PSV(49,4), FS(49)
      COMMON/ABCOEF/A11(49,4),A12(49,4),A21(49,4),A22(49,4)
                       ,B1(49,4),B2(49,4),PERIOD(49),KNDT(49)
     끃
                       ,KN1(49),DAMP(4),L
     45
```

С

```
CHARACTER SYM, E*153, F(102), G(3)
    DO 200 11=L.49
    NDT = KNDT(I1)
    N1
         = KN1(11)
    FREQ = 6.283185/PERIOD(11)
    14
          FREQ#FREQ
    DO 200 I2=1,4
          = 2.#FREQ#DAMP(12)
    15
    DMAX = 0.
    VMAX = 0.
    AMAX = 0.
    X1
          # 0.
          = 0.
    ۷1
 THE MAIN DO LOOP
    DO 100 I=1,N1
    \mathbf{J} = (\mathbf{I} + \mathbf{N}\mathbf{D}\mathbf{T} - \mathbf{1}) / \mathbf{N}\mathbf{D}\mathbf{T}
    DVEL = (VEL(J+1)-VEL(J))/NDT
    X = A11(I1,I2) *X1+A12(I1,I2) *V1+B1(I1,I2) *DVEL
    V = A21(11,12) * X1 + A22(11,12) * V1 * B2(11,12) * DVEL
    X1 = X
    V1 = V
    A = T4 + X + T5 + V
    XABS = ABS(X)
    VABS = ABS(V)
    AABS = ABS(A)
                           DMAX = XABS
    IF( DMAX.LT, XABS )
    IF( VMAX.LT.VABS )
                          VMAX = VABS
    IF( AMAX.LT.AABS ) AMAX = AABS
100 CONTINUE
    IF(I2,E0,1) FS(I1) = SQRT(T4*X*X*V*V)
     SD(11,12) = DMAX
     SV(11, 12) = VMAX
     SA(I1,I2) = AMAX
    PSV(I1, I2) = FREQ+DMAX
200 CONTINUE
    CALL SVLOG(PSV, SYM, R)
    G(1) = 6H AMAX=
    G(2) = 6H VMAX=
    G(3) = 6H DMAX=
    PRINT 1000, SYM, R, DEPTH, ((G(1), TMAX(1)), I=1,3)
    PRINT 1080, (DAMP(I), I=1,4)
    DO 300 I=L,49
    ENCODE(E,1100) FS(I),SD(I,1),SV(I,1),SA(I,1),PSV(I,1)
                            ,SD(1,2),SV(1,2),SA(1,2),PSV(1,2)
   4
                            ,SD(1,3),SV(1,3),SA(1,3),PSV(1,3)
   4
```

```
,SD(1,4),SV(1,4),SA(1,4),PSV(1,4)
      DECODE( E.1200 ) F
      PRINT 1300, (PERIOD(I),F)
  300 CONTINUE
 1000 FORMAT(1H1,////51X,A6,2X,3H(R=,F7,2,3H KM,8H DEPTH=
            , F6.2.4H KM)//49X.3(A6, E9.2.1X))
     1
 1080 FORMAT(/34X,4(5HDAMP=+F4,2,15X)/14X,6HPER10D,3X,2HFS,
              4(4X,2HSD,4X,2HSV,4X,2HSA,3X,3HPSV))
     ĕ
 1100 FORMAT(17E9,2)
 1200 FORMAT(17(A1,1X,3A1,1X,A1,1X,A1))
 1300 FORMAT(13X, F6, 2, 1X, 102A1)
      RETURN
      END
      SUBROUTINE SVLOG(SVP, SYM, R)
C
   PLOT PSV-PERIOD ON LOG-LOG SCALE
C
C.
      DIMENSION SVP(49,4)
      DIMENSION PSV(49,4), FS(51), FP(51)
      CHARACTER SYM
      COMMON/ PERLOG / PERIOD1(51).L
      CYCLE = 1.84
           = 3
      NOCX
      NOCY
            = 4
      CALL PLOT(0,,-11.,-3)
      CALL PLOT(0,,2.,-3)
      YMIN = 1.E+38
      DO 400 11=L.49
      DO 400 I2=1:4
      T = SVP(I1, I2)
      PSV(11, 12) = ALOG1O(T)
      \tilde{T} = PSV(11, I2)
      IF( T.LT.YMIN ) YMIN = T
  400 CONTINUE
      DO 450 1=2,9
      Ť = I
  450 FS(I) = ALOG10(T) * CYCLE
      XLEN = NOCX+CYCLE
      YLEN = NOCY+CYCLE
            = 0.01*XLEN
      SEG
      SIZE
           = 0.027+XLEN
      SIZE1 = 0.6*SIZE
      LYMIN = YMIN-1.
      IF ( YMIN, GT. 0. ) LYMIN = LYMIN+1
```

D-4

```
DO 800 I1=1,2
                      GO TO 490
    IF( 11.EQ.2 )
    Ť1
           = 1.
            = 0.
    12
            = 0.09
    13
    T4
            = 0.015
    NOC
            = NOCY
    POWER = LYMIN-1
    GO TO 500
490 71
           = 0,
            = 1.
    12
            = 0.022
    Ť3
           = 0,04
    74
           = NOCX
    NOC
    POWER = -2.
            = -T3*XLEN
500 X0
    YO
            = -T4 * XLEN
           = Y0+0.62*SIZE
    Y01
    NOC1 = NOC+1
    no 600 I=1,NOC1
    X_1 = T_{2*}(I_{-1}) * CYCLE
    Y\overline{1} = T1*(I-1)*CYCLE
    CALL PLOT(X1, Y1,3)
    x_2 = x_1 + x_0
    Y_2 = Y_1 + Y_0
    CALL NUMBER (X2, Y2, SIZE, 10,, 0,,-1)
    POWER = POWER+1.
    Y_2 = Y_1 + Y_0 1
    CALL NUMBER (999,, Y2, SIZE1, POWER, 0,, -1)
    CALL PLOT(X1,Y1,3)
    X_2 = T_2 X_1 + T_1 X LEN
    Y2 = T1+Y1+T2+YLEN
    CALL PLOT(X2, Y2, 2)
600 CONTINUE
    CALL PLOT(0.,0.,3)
    DO 700 12=1,2
    S1 = (12-1)*(T1*XLEN+T2*YLEN)
    S_2 = (3, -2, +12) + SEG
    DO 700 I=1,NOC
    S3 = (I-1) * CYCLE
    DO 700 J=2,9
    X_1 = T_1 * S_1 + T_2 * (F_S(J) + S_3)
    Y_1 = T_2 * S_1 + T_1 * (F_S(J) + S_3)
    CALL PLOT(X1, Y1,3)
    X_2 = X_1 + T_1 + S_2
```

```
Y_2 = Y_1 + T_2 + S_2
      CALL PLOT(X2,Y2,2)
  700 CONTINUE
      CALL PLOT(0.,0.,3)
  800 CONTINUE
      SIZE # 0.035+XLEN
      CALL SYMBOL(0.30*XLEN, -0.11*XLEN, SIZE, 12HPERIOD (SEC),
     10.0.12)
      CALL PLOT(0.0,0.0,3)
      CALL SYMBOL(-0.13+XLEN,0.45+XLEN,SIZE,12HPSV (CM/SEC),
     190.0,12)
      CALL PLOT(0,0,0,0,3)
      X1 = 0.30 + XLEN
      Y1 = -0.23+XLEN
      CALL SYMBOL (X1, Y1, SIZE, SYM, 0., 6)
      CALL SYMBOL(999,, Y1, SIZE, 2HR=, 0,, 2)
      CALL NUMBER (999., Y1, SIZE, R, 0, ,-1)
      CALL SYMBOL (999., Y1, SIZE, 2HKM, 0., 2)
      CALL PLOT(0,,0.,3)
      K1 = 50-L
      FP(K1+1) = -1.
      FP(K1+2) = 1./CYCLE
      FS(K1+1) = LYMIN
      FS(K1+2) = 1./CYCLE
      DO 900 J=1,4
      DO 890 I=L,49
      K = I+1-L
      FP(K) = PERIOD1(I)
      \dot{F}S(K) = PSV(I_J)
  890 CONTINUE
  900 CALL LINE(FP, FS, K1, 1, 0, 0)
      ČALL PLOT(10.,0.,-3)
      RETURN
      END
      SUBROUTINE AMATRIX(NO,DTO)
Ĉ
C
        NO = NUMBER OF GRID POINTS
       TTO = TIME INTERNAL USED IN SAMPLING THE INPUT VEL
C
С
      COMMON/ABCOEF/A11(49,4),A12(49,4),A21(49,4),A22(49,4)
                        ,B1(49,4),B2(49,4),PERIOD(49),KNDT(49)
     8
                        ,KN1(49),DAMP(4),L
      COMMON/ PERLOG / PERIOD1(51),L1
      DAMP(1) = 0.
```

```
DAMP(2) = 0.02
      DAMP(3) = 0.05
      DAMP(4) = 0.1
      J≡0
      PERIOD(1) = 0.1
      DO 90 I1=1,3
      ADD = 0.02 \times 10. \times \times (11 - 1.)
      DO 80 12=1,5
      J = J + 1
   80 PERIOD(J+1) = PERIOD(J)+ADD
      ADD = 2,5 + ADD
      DO 85 12=6,11
      J = J + 1
   85 PERIOD(J+1) = PERIOD(J)+ADD
      ADD = 2.*ADD
      DO 90 12=12,16
      J = J^*1
   90 PERIOD(J+1) = PERIOD(J)+ADD
      TNYG = 2. +DTO
      DO 92 1=1,49
      \dot{\tau} = PERIOD(I)
      F(T.GE.TNYG) GO TO 94
   92 CONTINUE
   94 L = 1
      L1 = L
      DO 95 I=L.49
      \dot{T} = PERIOD(I)
   95 PERIOD1(I) = ALOG10(T)
      DO 100 I1=L,49
С
   FIND THE PROPER TIME INTERVEL
      DT1 = PERIOD(11)/10.
      NDT = DTO/DT1+1.
      DT = DTO/NDT
           = (NO-1) + NDT+1
      N
           = N - 1
      N1
      FREQ = 6.283185/PERIOD(I1)
      KN1(11) = N1
      KNDT(I1) = NDT
      DO 100 12=1.4
   FIND THE MATRIX A, B USED IN CALCULATING X,V
С
      SORT1= SORT(1.-DAMP(12)+DAMP(12))
            = FREQ#SORT1
      WD :
      WDT
            # WD+DT
      11
            = -FREQ+DAMP(12)+DT
      Ť2
            = DAMP(12)/SQRT1
```

```
EXP1 # EXP(T1)
SIN1 # SIN(WDT)
COS1 # COS(WDT)
T3 # -1.+EXP1*(COS1+T2*SIN1)
T4 # FREQ*FREQ
A11(I1,I2) # EXP1*(T2*SIN1+COS1)
A12(I1,I2) # EXP1*SIN1/WD
A21(I1,I2) # CREQ*EXP1*SIN1/SORT1
A22(I1,I2) # CREQ*EXP1*SIN1/SORT1
B1(I1:I2) # T3/(T4*DT)
B2(I1:I2) # T3/(T4*DT)
B2(I1:I2) # CREQT
RETURN
END
```

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- "Analysis of Strong Motion Data from the New Madrid Seismic Zone: 1975-1976," by Robert B. Herrmann, August 1977. (NTIS PB 280 148/AS).
- "A Time Domain Study of the Attenuation of 10-Hz Waves in the New Madrid Seismic Zone," by Otto W. Nuttli, <u>Bulletin</u>, Seismological Society of America, Vol. 68, April 1978, pp. 343-356.
- 3. "SH Wave Generation by Dislocation Sources A Numerical Study," by Robert B. Herrmann (submitted to <u>Bulletin</u>, <u>Seismological Society</u> of America), 1978.
- 4. "On the Relation Between MM Intensity and Body-Wave Magnitude," by Otto W. Nuttli, G.A. Bollinger, and Donald W. Griffiths (submitted to Bulletin, Seismological Society of America), 1978.
- 5. "Computer Programs in Earthquake Seismology, Volume 1: General Programs," edited by Robert B. Herrmann, Department of Earth and Atmospheric Sciences, Saint Louis University, October 1978.
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E-1

· 1 I. I. ł. ł. ł. ł. I. i i 1 1 ł. ł.