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EARTHQUAKE ENGINEERING RESEARCH CENTER

PREDICTIVE DYNAMIC RESPONSE· OF PANEL TYPE STRUCTURES UNDER EARTHQUAKES

by J.P. KOLLEGGER J.G. BOUWKAMP

Report to the National Science Foundation

UNIVERSITY OF CALIFORNIA . Berkeley, California

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College of Engineering College of Engineering Department of Civil Engineering University of California Berkeley, California October 1980

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ABSTRACT

The potential coupling of translational and rotational motions of prefabricated panel systems under earthquake ground excitation is studied for several 12-story-high apartment buildings. Placement of apartments along the short end of these buildings and limiting the number of apartments along the long sides resulted in twelve different floor plans. The foundation flexibility was captured mathematically through introduction of a four-story-high "dummy story." Resonance and modal analyses were performed indicating considerable coupling of the longitudinal translational and torsional modal components. Under earthquake conditions both uncoupled and coupled translational and rotational motions were identified. The observed behavior was found to depend on both the degree of coupling of translational and rotational modal components of the buildings at the fundamental frequencies, as well as on the earthquake frequency response spectrum. A hypothesis regarding the anticipated behavior under earthquake excitation was developed and successfully tested against the analytical predicted structural response.

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1. INTRODUCTION·

1.1 General

Modern mul tistory apartment buildings are often an assembly of prefabricated wall and floor elements. Results of several forced and ambient vibration studies of such buildings indicate that these structures have quite different dynamic characteristics than earthquake codes would tend to imply [1,2]. Advanced computer techniques permit prediction of the earthquake response provided that the computer model formulation is accurate. In that respect, the formulation of the foundation stiffness is particularly critical. Experimental results have shown a potentially dangerous coupling of translational and torsional modes, a phenomenon that could lead to serious earthquake damages. Hence, the paper focuses on the influence of the floor plan layout on the basic dynamic characteristics of typical panel-type structures.

Considering the overall floor plan of panel type structures an often rectangular shape can be noted. Invariably, the apartment layout along the front and back of a building calls for structural walls and partitions oriented in the short direction of the building. Furthermore, outside walls along the length of the building are often non-structural. Longitudinal structural walls are typically located along the interior central corridor and also, as partitions between apartments, at either end of the building. With such wall layouts, the stiffness in the shorter transverse direction, contrary to normal expectations, is commonly found to be larger than the stiffness in the longitudinal direction. In addition, longitudinal motion seems to be particularly susceptible to rotational coupling. Hence, the transverse story deflections at the end of the

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building may become a predominant factor under earthquake excitation. This phenomenon becomes particularly pronounced when the longitudinal wall layout is non-symmetric with respect to the mass center of the typical floors.

In order to study the potential coupling of translational and rotational response of prefab systems as affected by the overall floor plan configuration, several floor plans will be considered. The selected variants will allow an assessment of the effect of the relative translational and torsional stiffnesses on the overall response of these structures under different earthquake ground excitations.

1.2 Acknowledgement

The authors gratefully acknowledge the financial support provided by the National Science Foundation under Grant PFR-7908257.

2. DESCRIPTION·OF THE ANALYZED STRUCTURES

Recently two apartment buildings, 12 and 8 stories in height, have been tested under forced and ambient vibrations [1,2]. The structures were of the "Forest City Dillon" prefab system. The vertical and horizontal load resistance was provided by reinforced concrete shear walls, oriented in both transverse and longitudinal directions. The wall dimensions were constant over the entire height of these buildings. Both structures were found on piles with lengths varying from 32 to 50 feet.

Incorporating the basic panel elements of the above prefab system, three structural variants, Al, B1, and Cl, with different floor plans, were formulated for this study (Fig. 2.1). The Al floor plan is very similar to the two experimentally tested buildings. Considering the A1 variant and rotating the two extreme apartments, facing south by 90 degrees, led to a floor plan with three apartments on either end of the building (variant B1). This arrangement results in an increase in the longitudinal stiffness and a reduction of the transverse and torsional stiffnesses. Adding one more unit on either end of the building resulted in variant Cl. This arrangement effectively increases, in comparison with Bl, both the torsional and longitudinal stiffness.

In order to further evaluate the effect of the longitudinal stiffness relative to the transverse and torsional stiffnesses, three more basic layouts were considered. Two of these variations were developed by eliminating transverse walls in the central portion of each of the three basic floor plans Al, B1, and Cl. Elimination of one set of transverse

FIG. 2.1. FLOOR PLANS STRUCTURES A1, B1 AND C1.

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FIG. 2.2. FLOOR PLANS STRUCTURES A2, B2 AND C2

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FIG. 2.3. FLOOR PLANS STRUCTURES A3, B3 AND C3

FIG. 2.4. FLOOR PLANS STRUCTURES Al-D, Bl-D, Cl-D

walls, or effectively removing one bay with two apartments, resulted in variants A2, B2, and C2 (Fig. 2.2). These structures were no longer symmetric with respect to the V-axis and thus would effectively exhibit torsional coupling under both x and y excitation. A further reduction of the transverse stiffness was introduced by eliminating a second set of transverse walls. This resulted in variants A3, B3, and C3 (Fig. 2.3).

A further variation in layout, resulting in a reduction of both the longitudinal and, because of the flange action in perpendicular oriented walls, the transverse stiffness, was achieved by deleting four walls along the interior corridor of structures Al, Bl, and Cl. Compared with structures Al, Bl, and Cl, the resulting torsional stiffness of the variants, identified as Al-O, Bl-O, Cl-O,and shown in Fig. 2.4, remained basically unchanged because the deleted walls were positioned closely to the center of rigidity of the floor layout.

Typically, all structures studied in this investigation were 12 stories. With heights of 9.67 feet for the first story and 8.67 feet for the other stories, the overall building height was 105 feet.

3. MODELING OF THE STRUCTURES

Analytic computer models of the twelve different structures shown in Figs. 2.1 through 2.4 were developed to determine their dynamic characteristics. The models'were formulated using both a rigid and an flexible base. TABS-77, a general purpose computer program [3J, was used to calculate frequencies and mode shapes, as well as the linear elastic time-history response under earthquake ground excitation.

The program considers the floors to act as rigid diaphragms with zero transverse stiffness. All elements are assembled initially into planar frames and then transformed, using the rigid-diaphragm assumption, to three degrees of freedom (2 translational and 1 rotational) at the center of rigidity of each story level. The assumption of a rigid floor diaphragm for the subject studies was fully supported by the experimental results of the forced vibration studies of two Forest Dillon type buildings.

The basic model of each building was formulated as a system of frames and shear-wall elements interconnected by floor diaphragms which were rigid in their own plane. All walls were treated as "wide columns." This required a reduction of properties (I, A) to the elastic centroid of each wall. Where a wall is met by a perpendicularly oriented wall, a portion of the latter wall is assumed acting as a flange and is thus included in the moment of inertia calculation. For a "half-flange" condition, where two panels form a single corner, the effective width is taken as 1/6 of the overall building height, or 17.5 feet. In the case of a "full flange" condition, the effective width is assumed to be 1/3 of the height, or 35 feet. The above assumption is based on the fact that

the walls are effectively interconnected at each floor level. The resulting dowel action over the height of the building seems to justify the assumed wall coupling, particularly for relatively small displacement conditions. A value of 4,000 ksi was used for the modulus of elasticity of the concrete. The reinforcing steel area was not included in calculating the moment of inertia of the shear walls; thus, the wall properties were the same for each of the 12 stories.

Wherever shear walls were positioned in one line, parallel to the direction of motion, it was assumed that those walls would be coupled by a portion of the floor slab with a width of 18 times the thickness of the floor. The effective span of the coupling girders was identical to the clear distance between the walls. Also, the effective height of the walls was taken as the clear height between two stories.

The masses, lumped at each story level, were calculated neglecting non-structural elements with a concrete weight of 0.15 kips/ft³. The locations of the center of mass and the center of resistance, which is calculated on the assumption that the wall panels are clamped at both ends, are shown in Figs. 2.1 through 2.4.

4. MODELING OF THE FOUNDATION

During the experimental building tests on the 12-story building, significant horizontal motion--up to 10% of the top story displacement- was recorded at the ground floor level. Therefore, it was considered necessary to develop analytical building models which would properly reflect the observed flexible base condition.

Combining the forced vibration test measurements of the horizontal ground displacements with the base overturning rotations, as estimated from the mode shapes, the following approach was used to model the base flexibility. The measured floor accelerations times the floor masses gave the elastic forces for each floor level, from which the base shear and the overturning moment could be computed. Comparing base shear and moment with the experimentally determined displacement and rotation at the ground floor allowed an evaluation of the translational and rotational stiffness of the foundation for both directions.

The lateral and rotational foundation stiffnesses for the two apartment buildings tested are presented in Table 4.1. In order to account for the foundation flexibility, the TABS program permits the introduction of a dummy story fixed at the base. The heights of these dummy stories as based on the different experimental stiffness values for the two test structures are also shown in Table 4.1. As the results were found to be rather similar for these structures, a representative height of approximately 32 feet was selected for the 12-story-high buildings under investigation, or, 30% of the structural height.

TABLE 4.1 ROTATIONAL AND LATERAL FOUNDATION STIFFNESSES

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5. FREQUENCY AND MODE SHAPE ANALYSES

In the first part of the dynamic analysis, frequencies and mode shapes for the twelve different structures were evaluated considering both a rigid and flexible foundation. Panel structures are quite rigid, and their seismic response is basically determined by the fundamental modal responses. Hence, only three fundamental resonant frequences were considered; namely, $f \times \theta_1$, $f \times \theta_2$, and fy. Of these three frequencies, two frequencies exhibit significant coupling between the translational x-motion and rotation (e) . The frequency at which the torsional effect is most pronounced has been termed the "torsional frequency."

A compilation of the mass and stiffness data for each of the twelve structures is presented in Table 5.1, where the lateral and rotational stiffnesses have been calculated for an 8.67-foot-high story on the assumption that the wall panels are clamped at both ends. The resonant frequencies for a flexible-base condition are also shown in Table 5.1. The "torsional frequencies" are specifically identified in this table. Also shown are the eccentricity distances e_x and e_y between the center of mass (C.M.) and the center of rigidity (C.R.). The e_v values are a direct indication of the potential coupling of the longitudinal x-motion and rotation. The small variations in the natural frequencies of the twelve structures seem to indicate that the effect of the different layouts is relatively small.

For each structure the three basic frequencies for both a rigid base condition, disregarding any soil-structure interaction, and a flexible base condition, are presented in Table 5.2. As expected, the frequencies

for the structures with a 32-foot-high dummy story, reflecting the flexible base, are smaller than the rigid-base values. For each of the structures the percentage change for the two fundamental $x - \theta$ coupled frequencies and the y-frequency are presented in the same table. In general, the frequencies for the flexible base condition are from 70% to 80% of those for the rigid base condition.

From these findings one can conclude that the effect of the dummy story on the frequencies can be captured by introducing the height of the dummy story as an addition to the total structural height of the building. Considering that the height of the dummy story is ³² ft., or basically four stories, the rigid and flexible base conditions represent structures with 12 and 16 stories, respectively. With experimental results from full-scale vibration studies carried out on prefabricated panel type buildings [1,2] indicating a proportionality between height and period, the fundamental frequencies of a 16-story structure would be only 75% of those of a 12-story structure with the same floor plan. This is in excellent agreement with the noted percentages in Table 5.1.

The previously noted $x-\theta$ coupling at resonance can be observed most clearly through normalized floor modes at the 12th floor level. The floor modes for the 12th floor and the resonant frequencies for both the rigid and flexible base conditions are presented in Tables 5.3, 5.4, and 5.5 for the x-, torsional-, and y-modes, respectively. Examples of such xand y-normalized mode shapes are shown in Fig. 5.1 for structures Al and C2. The results shown reflect the generally observed behavior of the several structures considered in this study.

Because of the y-axis symmetry of the floor plan in the ABC-l, ABC-3, andABC-l-D type structures (see Figs. 2.1,2.3,2.4), these structures

typically exhibit, as illustrated by structure Al in Fig. 5.1, a pure translational y-mode. However, for these structures, the other two frequencies typically show a significant coupling of the x and torsional modal components. In this respect, the results shown in Fig. 5.1, as well as the mode identification noted in Table 5.2, indicate that the base flexibility may change the torsional contribution in the two $x - \theta$ coupled modes. In certain instances (Al, Cl, A2. and C2), the flexible base condition alters the torsional contribution to the extent that the first fundamental frequency becomes the frequency with a predominant torsional modal component. In a few instances, such as for variants Cl, C2, and C3, the foundation flexibility also causes a reversal of the y and one $x-$ frequency. This behavior is illustrated by the floor-mode shapes for structure C2 as shown in Fig. 5.1. This structure also illustrates the torsional y-coupling effect typical for the ABC-2 structures. This phenomenon is a direct result of the non-symmetric layout of these structures with respect to both the x and y axes (see Fig. 2.2).

The relative magnitude of the rotation of the x-mode with respect to the rotation of the torsional mode at the 12th floor was computed for each building. The resulting percentage values of the relative degree of rotational coupling (C) for the twelve buildings studied on a flexible base are presented in Table 5.6. The same table also shows the results for the three buildings ABC-1 with an assumed rigid base condition. The percentages for the B-type structures, with consistently lower torsional stiffness (Table 5.1), are all smaller than 22%, whereas the A- and C-type variants have all higher values, ranging from 26% to 82%. These values

seem to correlate also with the degree of eccentricity; e.g., the distance between the center of mass and the center of rigidity.

The fundamental uncoupled y frequency and the lower frequency of the coupled $x-\theta$ mode for the different structures with flexible base, thus reflecting the appropriate foundation-structure interaction, are presented in Table 5.7. Also shown for comparison are the fundamental translational frequencies for by the x and y direction of these buildings using the period T as given by the Uniform Building Code (T = 0.05 h/ \sqrt{D}). The latter frequencies were calculated using the basic structural building height of 105 feet as specified by the UBC. Also indicated are the frequencies for a building with an effective height of 137 feet (structural height plus height of dummy story). The results show poor agreement between the analytical and UBC frequencies. In fact, in a total reversal of the UBC derived fundamental frequencies, the analytical frequencies are larger for resonance in the y-direction than for resonance in the xdirection.

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TABLE 5.1 STRUCTURE PROPERTIES AND RESONANT FREQUENCIES FOR FLEXIBLE BASE CONDITION

 $*$ = "torsional frequency" - maximum torsional contribution

TABLE 5.2 FOUNDATION EFFECT

y = translational frequency f_y * = "torsional frequency" f_{θ}
() = number between parentheses denotes % change

TABLE 5.3 RESONANT FREQUENCIES (f_x) AND
FLOOR MODES FOR THE X-MODE

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TABLE 5.4 RESONANT FREQUENCIES (f*) AND FLOOR MODES FOR THE TORSIONAL MODE

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TABLE 5.5 RESONANT FREQUENCIES (f_y) AND
FLOOR MODES FOR THE Y-MODE

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TABLE 5.6 DEGREE OF TORSIONAL COUPLING

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 $*$ C = ROTATIONAL COMPONENT OF THE X-MODE \times 100 ROTATIONAL COMPONENT OF THE 0-MODE X

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TABLE 5.7 ANALYTICAL AND UBC FREQUENCIES

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STRUCTURE A1

FIG. 5.1. MODE SHAPES 12th FLOOR - STRUCTURES A1 & C2

6. EARTHQUAKE TIME-HISTORY ANALYSIS

In order to gain information about the effect of longitudinal and torsional coupling of panel-type structures during seismic excitation, linear-elastic time-history analyses of the twelve structural variants were performed by submitting the buildings to longitudinal (E-W) directed ground excitation. In the first instance all structures were subjected to the N-S component of the 1940 El Centro earthquake with a maximum acceleration of 0.35 g. Subsequently, in order to study the effect of different ground excitations on the building response, structures ABC-l, with both flexible and rigid base conditions, were subjected to two additional earthquake ground-motion records; namely, the S69E component of the 1952 Kern County (Taft) earthquake with a peak acceleration of 0.18 g, and Pacoima Dam S14W record of the 1971 San Fernando earthquake with a scaled down peak acceleration of 0.35 g.

Selecting a linear-elastic time-history was considered to be justified as it will capture the important initial phase of the structural response. Another justification for the selected procedure was the notion that the principally localized nature of structural damages, short of collaose, will not alter the general building behavior from the analytically predicted response, particularly for the selected ground-motions. Admittedly, the non-linear soil-foundation characteristics can alter drastically the overall dynamic behavior.

The response of the structures for the first eight seconds of seismic excitation of the El Centro earthquake and for the first 12 seconds of the Taft and Pacoima Dam records resulting from an E-W excitation at the

dummy story base level, was evaluated. The ground motion was assumed to be constant over the length of the buildings, and no torsional earthquake components were considered. Under those conditions, a structure with coincident center of mass and center of resistance would not experience any torsional motion during such ground-motion. However, because of uncertainties in both the calculation of the mass and stiffness centers and the load distribution, as well as a result of structural imperfections, non-linear behavior, and other factors, it would be unreasonable to assume that torsional motion under earthquake excitation could be prevented.

Although the response to the three fundamental modes is predominant, . the contribution of the first fifteen modes was included in the analysis. The damping ratios for the three fundamental modes were based on the results of actual tests of a l2-story building; namely, 2% for the first mode and 1.4% for the second and third modes. The damping ratios for all other modes were taken at 2%.

The results of the time-history response studies under £1 Centro earthquake ground motion are presented in Figs. 6.1 through 6.4. These figures show for each of the variants the x and y displacements of the center of resistance at the 12th-floor level and the associated floor rotations versus time. Also indicated in these figures are the two basically coupled resonance frequencies and the frequencies of the translational and torsional response during the earthquake. These response frequencies were found by averaging the frequencies calculated from each half-cycle of structural response over the entire time-history.

Of the two coupled structural resonance frequencies, the torsional frequency f_A is defined as the translational resonance frequency with the highest degree of rotational coupling. Although also coupled, the other

frequency is labeled as the translational frequency $f_{\chi}.$ Fundamental and response frequencies for the structures with a flexible base subjected to the E1 Centro ground-motion are compared in Table 6.1. Under the x-directed excitation, the structures always responded in an x-motion with a frequency close to the fundamental x-mode frequency. This was true even for structures where the difference between the rotational contributions in the $x-$ and θ -mode was quite small (A2, C2, A3, and C3). However, the torsional response of the structures to seismic excitation occurred at a frequency close to either the fundamental torsional or the fundamental translational (f_x) frequency. In the first instance, the translational and rotational motions would, in fact, be uncoupled. However, in case the torsional motions occur at the fundamental translational frequency of the structure, the translational and torsional motions of the building are, in fact, coupled.

Reviewing the time-history results for the structures on flexible base subjected to the El Centro ground-motion, it can be observed that each building during the first few seconds of the earthquake responds in an uncoupled manner; i.e., the translational and torsional motions are 90° out of phase. For buildings Al, Cl, A2, and C2, this uncoupled response continues for most of the earthquake; only for a few cycles did a temporary in-phase response develop. Contrary to this favorable behavior, the initially uncoupled motion does not prevail for buildings Bl and B2. In those two cases, a virtually total in-phase response develops after a few seconds. However, fortunately the effect of the torsional response for these two structures is small in comparison to the translational response. This combined in-phase behavior is also supported by the two response frequencies $\bm{\mathsf{f}}_{\bm{\mathsf{X}}}$ and $\bm{\mathsf{f}}_{\bm{\mathsf{\Theta}}}$ of both buildings, as noted in the same

figures. It is obvious that the tuning of both response frequencies with the resonance frequency $f_{\sf X}$ causes this coupled effect. In fact, the uncoupled response frequencies for buildings Al, C1, A2, and C2, as noted also in Table 6.1, seem to support the previously noted out-of-phase response of the torsional and translational components of motion.

The above noted differences in response appear to be directly related to the degree of torsional coupling associated with the translational resonance frequency f_x , as compared with the maximum torsional coupling associated with the so-called rotational resonance frequency $\mathsf{f}_\theta^{\vphantom{1}}.$ For instance, for buildings AI, Cl, A2, and C2, which exhibit an out-ofphase response, the torsional coupling (C) for the $f_{\mathbf{x}}^{}$ frequencies amounted to, respectively, 31,43,77, and 82% of the torsional components of the f_Θ frequency (see Table 6.1). However, for buildings B1 and B2 these percentages were only 4 and 9%, respectively. Hence, it seems that significant torsional coupling at the translational resonance frequency results in an uncoupled response under earthquake excitation. On the other hand, a small degree of torsional coupling at resonance results in a combined in-phase translational and rotational response under earthquake conditions.

The above hypothesis is clearly supported by the in-phase response of buildings B3 and Bl-O for which the previously noted rotational coupling percentages were only 22 and 17 percent, respectively. Also, for buildings A3, C3, Al-O, and Cl-O, with rotational coupling percentages of 73, 80, 26, and 52 percent, respectively, the hypothesis seems to hold, as the response shows· a predominantly out-of-phase behavior.

In order to investigate the general validity of the above hypothesis, as it may be affected by the ground~rnotion input, buildings ABC-l on flexible

base were also subjected to the first 12 seconds of the Taft and Pacoima Dam ground motion records. The resulting x displacements and rotations at the center of the resistance at the 12th floor level are presented in Figs. 6.5 and 6.6. The associated structural and response frequencies are presented in Table 6.2. The uncoupled or coupled manner of response, as determined by the comparison of the fundamental frequencies of the structure with the response frequencies, as shown in this table, correlates favorably to the observed response as shown in Figs. 6.5 to 6.6.

The results indicate that for both the El Centro and Taft ground-motions, the buildings Al and Cl respond in an uncouoled fashion, while building Bl behaves in a coupled manner. However, in the case of the Pacoima Dam ground excitation, the three structures under study showed a coupled response, seemingly contradicting the above hypothesis. The reason for this different behavior, which reflects, in effect, a lack of excitation at the torsional resonance frequency, seems to be related to the energy of the earthquake record at this particular frequency.

The response spectra for the El Centro, Taft, and Pacoima Dam records are shown in Figs. 6.7 through 6.9, respectively. The fundamental x and θ frequencies of the ABC-1 structures are rather similar, averaging 2.1 cps for the translational and 1.70 cps for the torsional modes (Table 6.2). Considering the curves for 2% critical damping in each of the spectra for the corresponding averaged modal periods of 0.48 and 0.60 seconds, respectively, the soectral accelerations for these two modes are found to be approximately the same for the El Centro and Taft earthquakes. However, considering the Pacoima Dam spectrum, there is a distinct difference between the acceleration levels at these two fundamental periods. In fact, the spectral acceleration at about 0.48 sees, reflect-

ing the x resonance period, is quite large. On the other hand, the acceleration level at about 0.6 sees. or the fundamental torsional period is a distinct minimum. Hence, it seems reasonable to expect that this earthquake would fail to cause significant rotations in these structures. However, instead, a predominantly translational, x-resonance, response will result. As noted earlier, in such instances a building would respond in a coupled fashion, with the maximum fotation occurring at the instant of maximum translation. This behavior under the Pacoima dam record is clearly illustrated in Fig. 6.6.

Finally, Tables 6.3 and 6.4 summarize the maximum displacements and rotations at the roof level for the 18 different combinations of structures and earthquake records that were used in this analysis. Comparing the maximum rotations for the A and C structures with those for the B variants shows that the rotations developed in the B-type structures are generally lower.

TABLE 6.1 STRUCTURAL AND RESPONSE
FREQUENCIES FOR EL CENTRO RECORD

 $C = Torsional coupling percentage of f_x versus f_r$

TABLE 6.2 STRUCTURAL AND RESPONSE FREQUENCIES (FLEXIBLE BASE)

 $\sim 10^7$

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 $\mathcal{L}_{\mathcal{L}}$

TABLE 6.3 MAXIMUM DISPLACEMENTS AND ROTATIONS AT THE CENTER OF STIFFNESS OF THE ROOF

 $\mathcal{O}(\mathcal{L})$

 $\mathcal{L}^{\text{max}}_{\text{max}}$ and $\mathcal{L}^{\text{max}}_{\text{max}}$. The set of the $\mathcal{L}^{\text{max}}_{\text{max}}$

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TABLE 6.4 MAXIMUM DISPLACEMENTS AND ROTATIONS AT CENTER OF STIFFNESS OF THE ROOF

FIG. 6.1. EARTHQUAKE RESPONSE (EL CENTRO)

EARTHQUAKE RESPONSE (EL CENTRO) FIG. 6.2.

EARTHQUAKE RESPONSE (EL CENTRO) FIG. 6.3.

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EARTHQUAKE RESPONSE (EL CENTRO) FIG. 6.4.

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FIG. 6.5. EARTHQUAKE RESPONSE (TAFT)

FIG. 6.6. EARTHQUAKE RESPONSE (PACOIMA DAM)

FIG. 6.7. RESPONSE SPECTRA - EL CENTRO RECORD

IIIA004 52.002.0 TAFT LINCOLN SCHOOL TUNNEL COMP S69E DAMPING VALUES ARE 0. 2. 5. 10 AND 20 PERCENT OF CRITICAL

FIG. 6.8. RESPONSE SPECTRA - TAFT RECORD

SAN FERNANDO EARTHQUAKE FEB 9, 1971 - 0600 PST

IIICO41 71.001.0 PRCOIMA DAM. CAL. COMP S14W DAMPING VALUES ARE 0, 2, 5, 10 AND 20 PERCENT OF CRITICAL

FIG. 6.9. RESPONSE SPECTRA - PACOIMA DAM RECORD

7. CONCLUSIONS

Results of full-scale vibration studies of prefabricated panel-type buildings indicated a considerable translational and rotational coupling at resonance. Soil-pile-structure interaction effects were found to contribute significantly to the overall building response. This phenomenon required the introduction of a so-called "dummy story" in the computer model formulation of the structure.

In order to achieve an appropriate correlation between experimental and analytical results, a dummy story height of 30% of the overall structure height was required. To assess the general dynamic characteristics of panel type buildings, a total of twelve l2-story-high structures with different floor plans were studied in an analytical investigation. The dummy story height for all buildings was selected as 30% of the overall building height. The results of resonance frequency and modal analyses indicated considerable translational and rotational coupling at resonance. Despite markedly different floor plans, the three fundamental resonance frequencies were rather closely spaced. In general, the effect of the foundation flexibility needs to be considered, as it affects not only the resonance frequencies but also the extent of the modal coupling. Analytical results for both a rigid and flexible foundation constitution indicated that the fundamental periods were directly proportional to the overall structural height, including the dummy story. UBC derived periods were found to be grossly different from computer analyzed values. This discrepancy is a direct result of the code's inability to account for the actual wall layout and associated lateral stiffness of panel buildings.

Depending on the symmetry of the floor plan, rotational coupling was observed at two or possibly three fundamental resonant frequencies. Two of these frequencies were invariably associated with x-normalized modes. The resonance frequency exhibiting the most pronounced rotational, or torsional, coupling was termed the "torsional" frequency. The'other frequency, although exhibiting a smaller degree of rotational coupling, was termed the "translational" frequency. For the twelve structures studied, the degree of torsional coupling at resonance was found to have a direct bearing on the building response to earthquake excitation.

In case the torsional coupling at the translational resonance. frequency was at least 25% of the torsional component at torsional resonance, the translational and rotational motions of the building under earthquake excitation were found to be uncoupled, or 90° out of phase. In the case of a smaller rotational coupling percentage at resonance, the translational and rotational components of motion of the building under earthquake excitation showed an in-phase response. Fortunately, the basically limited torsional contribution at resonance, as reflected by a low rotational percentage value, will also limit the rotational excursions of the building under ground excitations.

The above observation seems to hold, in general, orovided that the earthquake acceleration at the fundamental structural periods is sufficient to excite the different structural modes. This energy dependent behavior was illustrated by the response of the buildings investigated under a Pacoima Dam excitation. In that case, both the translational and rotational motions occurred at the fundamental structural f_{x} -frequency, or in a coupled manner. The reason for this behavior was found in the frequency related energy of the Pacoima Dam earthquake, which lacks significant

acceleration pulses at a period close to the fundamental torsional period. Hence, excitation in an uncoupled fashion was not possible.

The latter observation is particularly important as it may reflect the dependence of earthquake induced excitation on the energy level of the earthquake at specific fundamental periods, be it either torsional or translational. Initial studies under rigid base conditions, even for the El Centro and Taft earthquakes, seem to support their potential behavior for at least low coupled systems.

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 $\mathcal{L}(\mathcal{L}(\mathcal{L}))$ and $\mathcal{L}(\mathcal{L}(\mathcal{L}))$ and $\mathcal{L}(\mathcal{L}(\mathcal{L}))$. Then $\mathcal{L}(\mathcal{L}(\mathcal{L}))$

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 $\bar{\mathbb{F}}$ $\bar{\rm I}$ $\label{eq:2.1} \frac{d}{dt} \int_{-\infty}^{\infty} \frac{d\mu}{dt} \left[\frac{d\mu}{dt} \right] \, d\mu = \frac{1}{2} \int_{-\infty}^{\infty} \frac{d\mu}{dt} \, d\mu$ $\mathcal{A}^{\mathcal{A}}$

 $\label{eq:2.1} \frac{1}{\sqrt{2}}\int_{\mathbb{R}^3} \frac{1}{\sqrt{2}}\left(\frac{1}{\sqrt{2}}\right)^2\left(\frac{1}{\sqrt{2}}\right)^2\left(\frac{1}{\sqrt{2}}\right)^2\left(\frac{1}{\sqrt{2}}\right)^2.$

 $\label{eq:2.1} \begin{split} \mathcal{L}_{\text{max}}(\mathbf{r},\mathbf{r}) = \mathcal{L}_{\text{max}}(\mathbf{r},\mathbf{r}) \mathcal{L}_{\text{max}}(\mathbf{r},\mathbf{r}) \mathcal{L}_{\text{max}}(\mathbf{r},\mathbf{r}) \mathcal{L}_{\text{max}}(\mathbf{r},\mathbf{r}) \mathcal{L}_{\text{max}}(\mathbf{r},\mathbf{r},\mathbf{r}) \mathcal{L}_{\text{max}}(\mathbf{r},\mathbf{r},\mathbf{r}) \mathcal{L}_{\text{max}}(\mathbf{r},\mathbf{r},\mathbf{r},\mathbf$

 $\label{eq:2.1} \frac{1}{\sqrt{2}}\int_{\mathbb{R}^3}\frac{1}{\sqrt{2}}\left(\frac{1}{\sqrt{2}}\right)^2\frac{1}{\sqrt{2}}\left(\frac{1}{\sqrt{2}}\right)^2\frac{1}{\sqrt{2}}\left(\frac{1}{\sqrt{2}}\right)^2.$

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 $\label{eq:2.1} \frac{1}{\sqrt{2}}\int_{0}^{\infty}\frac{1}{\sqrt{2\pi}}\left(\frac{1}{\sqrt{2\pi}}\right)^{2}d\mu\left(\frac{1}{\sqrt{2\pi}}\right)\frac{d\mu}{d\mu}d\mu\left(\frac{1}{\sqrt{2\pi}}\right).$ $\label{eq:2.1} \frac{1}{\sqrt{2}}\left(\frac{1}{\sqrt{2}}\right)^{2} \left(\frac{1}{\sqrt{2}}\right)^{2} \left(\$ $\label{eq:2.1} \frac{1}{\sqrt{2}}\int_{\mathbb{R}^3}\frac{1}{\sqrt{2}}\left(\frac{1}{\sqrt{2}}\right)^2\frac{1}{\sqrt{2}}\left(\frac{1}{\sqrt{2}}\right)^2\frac{1}{\sqrt{2}}\left(\frac{1}{\sqrt{2}}\right)^2\frac{1}{\sqrt{2}}\left(\frac{1}{\sqrt{2}}\right)^2\frac{1}{\sqrt{2}}\left(\frac{1}{\sqrt{2}}\right)^2\frac{1}{\sqrt{2}}\frac{1}{\sqrt{2}}\frac{1}{\sqrt{2}}\frac{1}{\sqrt{2}}\frac{1}{\sqrt{2}}\frac{1}{\sqrt{2}}$ $\label{eq:2.1} \frac{1}{\sqrt{2}}\sum_{i=1}^n\frac{1}{\sqrt{2}}\sum_{i=1}^n\frac{1}{\sqrt{2}}\sum_{i=1}^n\frac{1}{\sqrt{2}}\sum_{i=1}^n\frac{1}{\sqrt{2}}\sum_{i=1}^n\frac{1}{\sqrt{2}}\sum_{i=1}^n\frac{1}{\sqrt{2}}\sum_{i=1}^n\frac{1}{\sqrt{2}}\sum_{i=1}^n\frac{1}{\sqrt{2}}\sum_{i=1}^n\frac{1}{\sqrt{2}}\sum_{i=1}^n\frac{1}{\sqrt{2}}\sum_{i=1}^n\frac$ $\label{eq:2.1} \frac{1}{\sqrt{2\pi}}\sum_{i=1}^n\frac{1}{\sqrt{2\pi}}\int_{\mathbb{R}^n}\frac{1}{\sqrt{2\pi}}\int_{\mathbb{R}^n}\frac{1}{\sqrt{2\pi}}\int_{\mathbb{R}^n}\frac{1}{\sqrt{2\pi}}\int_{\mathbb{R}^n}\frac{1}{\sqrt{2\pi}}\int_{\mathbb{R}^n}\frac{1}{\sqrt{2\pi}}\int_{\mathbb{R}^n}\frac{1}{\sqrt{2\pi}}\int_{\mathbb{R}^n}\frac{1}{\sqrt{2\pi}}\int_{\mathbb{R}^n}\frac{1}{\$ $\label{eq:2.1} \mathcal{L}(\mathcal{L}^{\mathcal{L}}_{\mathcal{L}}(\mathcal{L}^{\mathcal{L}}_{\mathcal{L}})) \leq \mathcal{L}(\mathcal{L}^{\mathcal{L}}_{\mathcal{L}}(\mathcal{L}^{\mathcal{L}}_{\mathcal{L}})) \leq \mathcal{L}(\mathcal{L}^{\mathcal{L}}_{\mathcal{L}}(\mathcal{L}^{\mathcal{L}}_{\mathcal{L}}))$ $\label{eq:2.1} \frac{1}{2} \int_{\mathbb{R}^3} \left| \frac{d\mu}{d\mu} \right|^2 \, d\mu = \frac{1}{2} \int_{\mathbb{R}^3} \left| \frac{d\mu}{d\mu} \right|^2 \,$ $\label{eq:2.1} \frac{1}{2} \sum_{i=1}^n \frac{1}{2} \sum_{j=1}^n \frac{$ $\label{eq:2.1} \frac{1}{\sqrt{2\pi}}\int_{\mathbb{R}^3}\frac{1}{\sqrt{2\pi}}\int_{\mathbb{R}^3}\frac{1}{\sqrt{2\pi}}\int_{\mathbb{R}^3}\frac{1}{\sqrt{2\pi}}\int_{\mathbb{R}^3}\frac{1}{\sqrt{2\pi}}\int_{\mathbb{R}^3}\frac{1}{\sqrt{2\pi}}\int_{\mathbb{R}^3}\frac{1}{\sqrt{2\pi}}\int_{\mathbb{R}^3}\frac{1}{\sqrt{2\pi}}\int_{\mathbb{R}^3}\frac{1}{\sqrt{2\pi}}\int_{\mathbb{R}^3}\frac{1$ $\label{eq:2.1} \frac{1}{\sqrt{2}}\int_{\mathbb{R}^3}\frac{1}{\sqrt{2}}\left(\frac{1}{\sqrt{2}}\right)^2\frac{1}{\sqrt{2}}\left(\frac{1}{\sqrt{2}}\right)^2\frac{1}{\sqrt{2}}\left(\frac{1}{\sqrt{2}}\right)^2\frac{1}{\sqrt{2}}\left(\frac{1}{\sqrt{2}}\right)^2.$ $\label{eq:2.1} \frac{1}{\sqrt{2}}\int_{\mathbb{R}^3}\frac{1}{\sqrt{2}}\left(\frac{1}{\sqrt{2}}\right)^2\frac{1}{\sqrt{2}}\left(\frac{1}{\sqrt{2}}\right)^2\frac{1}{\sqrt{2}}\left(\frac{1}{\sqrt{2}}\right)^2\frac{1}{\sqrt{2}}\left(\frac{1}{\sqrt{2}}\right)^2.$ $\mathcal{L}(\mathcal{A})$ and $\mathcal{L}(\mathcal{A})$ $\hat{\mathcal{A}}$