# PRELIMINARY REPORT ON <br> THE SMART 1 STRONG MOTION ARRAY IN TAIWAN 

by
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Report to the National Science Foundation

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15. Suppiomentary Notes
16. Abstract (Limit: 200 worts)

The first large digital array, called SMART 1 (with radius 2 km and 37 accelerometers), to record substantial ground motion (up to 0.24 g horizontal acceleration) became operational in September 1980 in a highly seismic region of Taiwan. During the first year of operation, SMART 1 recorded fifteen earthquakes with local magnitudes ranging from 3.4 to 6.9.

Installational and operational details and likely errors in the data processing are presented.

For this major preliminary study, recorded wave forms across the array were analyzed for two earthquakes. The correlation coefficient between the acceleration wave forms of the same component recorded at any two array sites was studied. Representative measurements were made of seismic wave coherency, Fourier wave number, and response spectra. Comparisons of power spectra as a function of wave number, frequency, azimuth of propagation, and wave type were made.

The engineering analysis included (1) transformations to principar axes, (2) development of generalized response spectrum ratios for characterizing multi-support excitations, and (3) moving window analysis in the time and frequency domains for studying spectral variations of recorded ground motions. The dynamic properties of site conditions and spatial correlations of earthquake motions were studied. A technique using. the principal variance ratio was developed to identify the wave direction and type of waves.

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Report to the National Science Foundation

Report No. UCB/EERC-82/13
Earthquake Engineering Research Center
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## ABSTRACT

Specially designed arrays of strong-motion seismographs near to the earthquake source are required for seismological and engineering studies of the generation and near-field properties of seismic waves. The first such large digital array, called SMART 1 (with radius 2 km and 37 accelerometers), to record substantial ground motion (up to 0.24 g horizontal acceleration) became operational in September 1980 in a highly seismic region of Taiwan. During the first year of operation, SMART 1 recorded fifteen earthquakes with local magnitudes ( $M_{L}$ ) ranging from 3.4 to 6.9. Three were located directly below the array at focal depths of 59 to 76 km . The remaining twelve had shallow depths with epicentral distances from 1.8 to 76 km . Digital records from 27 three-component accelerographs were obtained from a magnitude $6.9\left(\mathrm{M}_{\mathrm{L}}\right)$ local earthquake on January 29, 1981.

The digital accelerographs were tested on the shaking table at U.C. Berkeley before they were sent to the field. Calculated instrumental transfer functions show that the calibration up to 20 Hz is known sufficiently well for normal wave analysis. Installational and operational details and likely errors in the data processing are also presented.

For the major preliminary study, recorded wave forms across the array were analyzed for the January 29, 1981 and November 14, 1980 earthquakes. The correlation coefficient between the acceleration wave forms of the same component recorded at any two array sites was studied. Representative measurements were made of seismic wave coherency, Fourier wave number, and response spectra. Comparisons of power spectra as a function of wave number, frequency, azimuth of propagation, and wave type show that wave forms and local magnitude varied significantly across the array for each event. On average, peak accelerations of horizontal components were about three
times that of the vertical component. Relative spectral changes from earthquake to earthquake were large.

The preliminary engineering analysis included (1) transformations to principal axes, (2) development of generalized response spectrum ratios for characterizing multi-support excitations, and (3) moving window analysis in the time and frequency domains for studying the spectral variations of recorded ground motions. The dynamic properties of site conditions and, following ideas of Newmark, spatial correlations of earthquake motions were also studied. A technique using the principal variance ratio was developed to identify the wave direction and type of waves.

## ACKNOWLEDGMENTS

Operation of SMART 1 is a joint effort between the University of California, Berkeley, and the Academia Sinica, Taỉan, R.O.C. Financial support is provided by the National Science Foundation under the grant No. CEE-7908982 and by the National Science Council under the grant No. 70-0202-M0001-03.

The authors wish to express their appreciation to Norman Abrahamson, Russell Sell, M. K. Hsu, C. C. Liu and J. Marrone for essential contributions. Requests for digital tape copies of the SMART 1 records in standard ASCII format should be made to the first author.

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## 1. GENERAL INTRODUCTION

### 1.1 Objectives

Installation of specially designed arrays of strong-motion seismographs in highly seismic areas of the world was recommended at an international workshop ${ }^{1}$ in Hawaii in 1978. Since that time, a number of large-scale arrays have been designed for siting in California, Japan, Assam (India), Mexico, People's Republic of China, Turkey, and in Taiwan, R.O.C., among other places. In addition, an International Strong-Motion Array Council (ISMAC) has been formed and has held two meetings to assist development and recommend future international meetings, data standardization and dissemination, instrumental comparisons, and so on.

Array measurements of seismic waves near to the source of a great earthquake are needed for two main reasons: first, such data provide a fuller understanding of both the generation of seismic waves from the moving dislocation along the causative fault and the effect of the intervening geology on the wave propagation. Secondly, such data supply essential knowledge about the spatio-temporal variations of seismic ground motions for engineering design of structures with large base dimensions, such as dams and bridges. With these objectives, the International Workshop on Strong Motion in Hawaii in May, 1978, recognized the need for groups of broadband accelerometers within a specified seismic area and with a specified site geometry and common time base. The first such digital array to become operational is located at the town of Lotung in the northeast corner of Taiwan, a particularly seismic area. ${ }^{2}$

For engineering purposes, the prediction of strong ground motion and of the response of engineered structures in earthquakes ${ }^{3}$ depends upon measurements of the spatial variability of earthquake intensities. Pioneering work of this
kind for small ground motions was first carried out in Japan ${ }^{4}$ using a small array of seismographs and correlational analysis. In this report, we describe more extensive measurements of seismic waves from strong earthquakes near to their sources, from a dense multiple-element array of digital strong-motion seismographs, and summarize the basic strong-motion data recorded by the array in its first 12 months of operation. An indication of preliminary research with some of the data is also given.

The SMART 1 research project is conducted jointly by the Seismographic Station, University of California, Berkeley, and the Institute of Earth Sciences, Academia Sinica, Taipei.

### 1.2 Strong Motion Array Configuration and Site Conditions

The strong-motion array, called SMART 1, installed at Lotung in Taiwan, is a two-dimensional surface array and consists of a center element $C 00$ and three concentric circles (inner $I$, middle $M$, and outer 0 ), each with 12 strong-motion seismographs having a common time base, and radii of 200 meters, 1 km , and 2 km , respectively (see Figs. 1.1 and 1.2 ). The inner ring controls the spatial aliasing since, for a wave velocity of $1 \mathrm{~km} / \mathrm{sec}$ and element spacing of 100 m , say, the aliasing frequency is 5 Hz . Only one instrument in the I-ring is located more than 10 m from the position of perfect symmetry. The coordinates of SMART 1 are shown in Table 1.1 . Details of the Lotung area and the soil conditions are shown in Figs. 1.3 and 1.4 ; for the upper 500 meters depth, the $P$ wave velocity is about 0.5 to $1.0 \mathrm{~km} / \mathrm{sec}$.

Installation began in September, 1980, and by January, 1981, 27 instruments were in place. By September, 1981, 15 earthquakes of local magnitude $3.4 \leq M_{L} \leq 6.9$ had triggered array elements (see Table 1.2).

The largest, on January 29 , 1981, was a strong earthquake centered 30 km from the center of the array and felt all over Taiwan. Its focal depth was approximately 11 km . The (Richter) magnitude calculated locally by the Institute of Earth Sciences (Taipei) was 6.9. The world-wide average $m_{b}$ magnitude (NEIS) was 5.6. In this case, the seismic waves triggered all the 27 operational digital accelerometers, thereby providing the largest comprehensive multi-dimensional recording of strong ground motion near a significant fault rupture yet obtained. This set of accelerograms can now be compared with important strong motions measured with other arrays such as in the 1979 Imperial Valley earthquake ${ }^{5}$ and the 1975 Oroville aftershocks. ${ }^{6}$ In the 1981 Taiwan earthquake, the maximum horizontal and vertical accelerations recorded were 0.24 g and 0.09 g , respectively. (A number of strong-motion accelerometers of conventional analog type also triggered in the vicinity of SMART 1 , allowing crucial comparison between the two types of measurements ${ }^{7}$; see Figs. 3.4 a and 3.4b.)

Large aperture seismic arrays (linear dimension of order 100 km ) have been used for over 15 years to discriminate between underground nuclear explosions and earthquakes by enhancing the signal-to-noise ratio. ${ }^{8,} 9$ In contrast, a strong-motion array of aperture 2 km is not designed to enhance small signals, but rather to determinewave speed, direction of propagation, type of wave component, and spatial variations and phase relations. As in an array of radio telescopes, a seismic array, like SMART 1, allows wave correlations for consecutive time and frequency intervals. Also, a computer algorithm can be used to insert appropriate time lags in the signals at each element, thereby steering the array response towards a known azimuth. One seismological objective is to follow the seismic dislocation as it moves
along the rupturing fault. On the engineering side, the measurements are designed to address such key questions as how the intensity of seismic waves varies over short distances, what is the contribution of seismic surface waves to shaking at a given site and, in particular, to provide information on out-of-phase wave components over distances comparable to the base dimensions of large engineered structures. Accelerograms from individual strongmotion seismographs cannot, in general, provide the resolution needed to resolve such questions.

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TABIE 1.1

* From 10/18/80 to 5/30/81:
SMART 1 Site Coordinates (from June 1, 1982)

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24 & 40 & 57.05 \\
24 & 40 & 53.09
\end{array}
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\begin{aligned}
& 11.24 \\
& 39.31
\end{aligned}
$$

$$
\begin{aligned}
& 5.5 \\
& 4.4
\end{aligned}
$$

| Site | X(meters) | Y(meters) | Longitude ( E ) |  |  | Latitude (N) |  |  | R(meters) | $\begin{aligned} & \text { Azimuth } \\ & \text { (degrees) } \end{aligned}$ | Level (meters) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | deg. | min. | sec. | deg. | min. | sec . |  |  |  |
| C00 | 0.0 | 0.0 | 121 | 45 | 53.23 | 24 | 40 | 25.55 |  |  | 6.1 |
| 101 | 30.5 | 190.9 | 121 | 45 | 54.33 | 24 | 40 | 31.76 | 193.3 | 9.07 | 5.9 |
| I02 | 132.5 | 141.6 | 121 | 45 | 57.93 | 24 | 40 | 30.15 | 193.9 | 43.10 | 5.5 |
| 103 | 193.6 | 65.1 | 121 | 46 | 00.09 | 24 | 40 | 27.67 | 204.2 | 71.41 | 6.1 |
| IO4 | 202.2 | -43.2 | 121 | 46 | 00.40 | 24 | 40 | 24.15 | 206.8 | 102.05 | 6.1 |
| 105 | 150.9 | -134.0 | 121 | 45 | 58.58 | 24 | 40 | 21.20 | 201.8 | 131.60 | 6.3 |
| 106 | 45.5 | -188.2 | 121 | 45 | 54.84 | 24 | 40 | 18.46 | 193.6 | 166.42 | 6.6 |
| I07 | -51.8 | -193.8 | 121 | 45 | 51.39 | 24 | 40 | 19.22 | 200.6 | 194.98 | 6.3 |
| 108 | -122.3 | -142.4 | 121 | 45 | 48.89 | 24 | 40 | 20.92 | 187.7 | 220.65 | 6.2 |
| I09 | -196.7 | -64.2 | 121 | 45 | 46.25 | 24 | 40 | 23.46 | 206.9 | 251.93 | 7.0 |
| I10 | -196.3 | 36.5 | 121 | 45 | 46.30 | 24 | 40 | 26.74 | 199.7 | 280.53 | 7.0 |
| I11 | -136.1 | 120.3 | 121 | 45 | 48.40 | 24 | 40 | 29.46 | 181.6 | 311.46 | 6.8 |
| I12 | -59.2 | 192.5 | 121 | 45 | 51.13 | 24 | 40 | 31.81 | 201.4 | 342.90 | 6.4 |
| MO1* | 186.6 | 938.6 | 121 | 45 | 59.87 | 24 | 40 | 56.05 | 956.9. | 11.24 | 5.0 |
| MO2** | 696.9 | 850.9 | 121 | 46 | 18.00 | 24 | 40 | 53.21 | 1099.9 | 39.32 | 4.4 |
| M03 | 879.6 | 348.4 | 121 | 46 | 24.45 | 24 | 40 | 36.87 | 946.1 | 68.39 | 4.0 |
| MO4 | 988.3 | -219.9 | 121 | 46 | 28.26 | 24 | 40 | 18.40 | 1012.5 | 102.55 | 4.5 |
| * From 10/18/80 to 5/30/81: |  |  |  |  |  |  |  |  |  |  |  |
| MO1 | 193.3 | 972.9 | 121 | 46 | 00.12 | 24 | 40 | 57.05 | 991.5 | 11.24 | 5.5 |
| ** From 10/18/80 to 1/1/81: |  |  |  |  |  |  |  |  |  |  |  |
| MO2 | 696.6 | 850.6 | 121 | 46 | 18.05 | 24 | 40 | 53.09 | 1099.4 | 39.31 | 4.4 |

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table 1.1
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| $\begin{gathered} \stackrel{y}{4} \\ \underset{\sim}{u} \end{gathered}$ |  |

TABLE 1. 2

| Event <br> No. | Origin Time (GMT) |  | Epicenter |  |  |  | $\begin{gathered} \text { Depth } \\ (\mathrm{km}) \end{gathered}$ | Mag. | $\begin{aligned} & \text { Azim. } \\ & (\operatorname{deg} .) \end{aligned}$ | $\begin{gathered} \Delta \\ (\mathrm{km}) \end{gathered}$ | $\mathrm{T} / \mathrm{I}^{*}$ | Max. Acc. (gal) |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Longitude (E) |  | Latitude (N) |  |  |  |  |  |  |  |  |  |
|  |  |  | deg. | min. | deg. | min. |  |  |  |  |  | V | ETV | NS |
| 1 | 1980.10.18 | 00:08:22.9 | 121 | 52 | 24 | 17 | 8 | 5.8 | 166.5 | 45.0 | 16/21 | 14.8 | 21.1 | 23.7 |
| 2 | 1980.11.14 | 13:37: 4.0 | 121 | 47 | 24 | 35 | 62 | 5.9 | 164.2 | 10.0 | 16/21 | 29.7 | 69.7 | 78.7 |
| 3 | 1980.11.14 | 13:38:15.8 | 121 | 49 | 24 | 34 | 59 | 5.6 | 152.1 | 12.5 | 13/21. | 10.7 | 22.9 | 24.6 |
| 4 | 1981. 1. 24 | 14:10:31.7 | 1.21 | 44 | 23 | 53 | 43 | 5.8 | 181.7 | 87.5 | $2 / 27$ | 2.4 | 8.1 | 9.0 |
| 5 | 1981. 1.29 | 04:51:36.0 | 121 | 53 | 24 | 26 | 11 | 6.9 | 153.8 | 30.0 | 27/27 | 64.5 | 158.2 | 244.1 |
| 6 | 1981. 2.27 | 02:27:33.9 | 121 | 52 | 24 | 33 | 76 | 5.8 | 140.4 | 17.2 | 10/27 | 4.4 | 13.6 | 12.2 |
| 7 | 1981. 3. 2 | 12:13:46.5 | 121 | 25 | 22 | 57 | 9 | 6.9 | 190.6 | 192.6 | $3 / 27$ | 2.7 | 6.4 | 10.5 |
| 8 | 1981. 3.10 | 08:24:51.2 | 121 | 47 | 24 | 44 | 7 | 4.4 | 15.4 | 7.0 | 19/27 | 16.0 | 23.5 | 34.5 |
| 9 | 1981. 3.22 | 21:25:32.5 | 121 | 49 | 24 | 45 | 11 | 3.8 | 30.9 | 9.7 | 12/28 | 13.1 | 22.8 | $19.1$ |
| 10 | 1981. 5. 3 | 19:19:51.3 | 121 | 59 | 24 | 42 | 68 | 5.3 | 82.4 | 21.5 | $10 / 28$ | 16.6 | 21.0 | 18.3 |
| 11 | 1981.6.1 | 11:53:44.2 | 121 | 50 | 24 | 23 | 2 | 5.3 | 165.5 | 32.5 | 8/28 | 10.1 | 13.2 | 15.0 |
| 12 | 1981. 8.20 | 19:03:28.1 | 121 | 45 | 24 | 41 | 0.1 | 4.7 | 286.7 | 1.8 | 18/36 | 22.9 | 23.3 | 35.5 |
| 13 | 1981. 8.20 | $20: 55: 6.6$ | 121 | 46 | 24 | 43 | 0.3 | 3.9 | 23.1 | 4.3 | 14/36 | 13.4 | 25.8 | 35.5 |
| 14 | 1981. 8.30 | 18:54:53.6 | 121 | 45 | 24 | 28 | 0.2 | 5.0 | 180.0 | 23.0 | 31/36 | 17.7 | 31.6 | 43.5 |
| 15 | 1981.10. 5 | 13:24:30.5 | 121 | 45 | 24 | 39 | 3.6 | 3.4 | 219.2 | 2.7 | 29/37 | 40.5 | 95.5 | $55.7$ |

[^0]
Fig. 1.1 Location of SMART 1


Fig. 1.2 The SMART 1 array


Fig. 1. 3 Geological map of Lotung area

Fig. 1.4 Profile of array site

## 2. INSTRUMENTATION

### 2.1 Introduction

A11 the instruments selected for the SMART 1 array were extensively tested at the University of California, Berkeley, before they were shipped to Taiwan where they were again checked before final installation. Installation of the SMART 1 instruments in the field in Taiwan began in September 1980 by engineers from the Institute of Earth Sciences, Taiwan, initially jointly with the staff of the Seismographic Station of the University of California at Berkeley. By October 1980, twenty-one elements of the array were operational and the remaining elements were added in the following months (Table 1.1). All thirty-seven elements were installed by September 1981. A second-order traverse was made in January 1981 to determine the exact location of each element. The coordinates are given in Table 1.1. The deviations of the actual site locations from the planned configuration are 1isted in Table 2.1.

By June 1981, eleven earthquakes had been recorded by SMART 1, with excellent performance in that most instruments triggered and the digital records were of high quality.

In this section some of the technical insights gained from the installation and operation of SMART 1 during its first year are presented.

### 2.2 Instrument Specification

The array elements at the field stations are triaxial strong-motion accelerographs which include digital cassette recorders with precision timing capability. A detailed description of the instrumental components is given below.

## (i) Accelerographs

There are 37 self-contained digital accelerographs having low power dissipation. Tie-down bolts anchor the unit to a surface pad. The three-component accelerometers (SA-3000) are selftriggering when the vertical acceleration exceeds 0.01 g (adjustable). The accelerometer is connected to a Sprengnether DR 100 recorder (shown in Fig. 2.1) in which data are filtered to prevent aliasing. The signal sampling at 100 sps per channel is converted to 12 bit binary. The digital delay memory has a capacity of 2.5 seconds. Digital data are recorded on magnetic tape cassettes which have a high signal-to-noise ratio. An automatic time-code generator records on tape such time information as day of year, hour, minute, second. The accelerograph also is capable of recording externally generated reference time signals on the cassette tape.

The sensitivity of the SA- 3000 is $3.75 \mathrm{~V} / \mathrm{g}$ with $\pm 2.0 \mathrm{~g}$ full scale; its resolution is 0.001 percent of full scale or $2.0 \times 10^{-3} \mathrm{~g}$. Arrows on the case of the sensor indicate the positive directions of the motions as shown in Fig. 4.8. The SA-3000 consists of three force-balanced accelerometers oriented so that their sensitive axes are orthogonal. Their full-scale output is $\pm 7.5 \mathrm{~V}$. A bubble is provided in the lid of the SA-3000 to ensure level installation of the sensor. Calibration data for level output voltage are provided with each unit so that an absolute level can be achieved for the horizontal sensors to approximately +3 minutes of arc. The AC/DC converter, calibration, circuit, and three-channel, ...
five-pole Butterworth low-pass anti-aliasing filter are incorporated within the unit. The calibration indut injects current into each sensor so as to provide approximately a 1 g bias of the sensor. Specifications of the SA-3000 are shown in Table 2.2.
(ii) Power Units

Each of the 37 elements of the array is powered by lead-acid batteries, charged regularly from the local electricity supply.
(iii) Portable Comparator

A portable field clock and comparator unit that can be taken from station to station is used to compute and display accumulated time corrections for the internal station clock to an accuracy of 1 millisecond. A comparator reference clock is also displayed. Manual adjustments of the comparator clock to GMT from radio timesignals are necessary.
(iv) Portable Playback Unit

The portable playback unit has the capacity to play the accelerograph digital tape cassettes onto strip charts with variable gain. The analog signals are displayed in parallel with the coded time data.
(v) Laboratory Playback System

The laboratory playback system selected was the Sprengnether DP-200 (shown in Fig. 4.1) which has the capability to play cassette tapes into a recorder that displays the signals on three-
channel paper with time annotation. The system can also transfer the digital data from cassettes to nine-track tape (10-1/2 inch reels) in ASCII-coded 800 bpi records with character representation. The length of the record is 5120 characters.

During the initial testing, if any malfunction was noted in an instrument, all other instruments were checked particularly with regard to this function. Most difficulties occurred with individual accelerometers which are easily damaged by rough handing since they are of the pivot and jewel type. One symptom of damage was variation of the base line, called DC drift or DC offset. In all, 24 of the 111 SA- 3000 accelerometers were returned to the manufacturer, Columbia Research Laboratories, Inc., for repairs.

Some available strong motion instrumentation was rejected for a variety of reasons. For example, some nine-track tape recorders were not acceptable since they used binary format, not ASCII. The latter code was selected because it was decided that the system must be independent of a particular computer from the outset; the project is an international one and could not be tied to a specific data processing system.

In particular, the instruments selected have the following features: the crystal oscillator specifications of the clock-comparator are very precise; the anti-aliasing filter for the seismic data has sharp attenuation; the annotation on the paper recorder playout is quite complete, and includes a simultaneous time information unit, serial number, and accurate reference time. Furthermore, the cassette playback system is convenient in that it displays time of event and event number while the tape is read, and the tape automatically stops between events. It would be even more satisfactory, however, if the start-up time were slightly faster and the tape recording time longer.

### 2.3 Shaking Table Test

Finally, before they were shipped to Taiwan, all accelerometers and digital recorders were tested on the earthquake simulator (shaking table) at the Earthquake Engineering Research Center of the University of California, Berkeley (Fig. 2.2). Recorded strong ground motions from California earthquakes scaled to various acceleration levels were used to drive the shaking table to which both the accelerometers and recorders were rigidly attached.

This laboratory test for defects in the instrumentation also provided an opportunity to check the specified responses of the accelerometers against the known response of the shaking table. A time-history of the shaking table input and the corresponding response of one of the instruments is shown in Fig. 2.3. The response of the shaking table is measured by an accelerometer placed at the center of the table. Tests were also done at low acceleration levels to test the trigger circuitry.

On subsequent evaluation, the shaking table tests proved to be of great value. Undoubtedly, malfunctions in the field in Taiwan were minimized by this procedure.

The following shaking table inputs based on accelerograms recorded at E1 Centro, Taft, and Pacoima Dam during the earthquakes of May 1940, June 1952, and February 1971, respectively, were used.

| (1) El Centro | vertical |
| :--- | :--- |
| (2) El Centro | NS horizontal - max. accel. 0.33 g |
| (3) (1) and (2) combined |  |
| (4) Pacoima | horizontal and vertical combined |
| (5) Taft | horizontal S69E (max. accel. 0.18 g$)$ and <br>  |

A comparison of El Centro (2) with the response of one of the instruments in Fig. 2.3 shows no significant differences in the time domain. The relation between the driving force and the transfer functions of the shaking table and instrument are illustrated in Fig. 2.4. When all the systems are assumed to be linear, the instrument transfer function is defined as

$$
H(\omega)=\frac{Y(\omega)}{F(\omega)}
$$

where $Y(\omega)$ and $F(\omega)$ are the Fourier transforms of the responses of the instrument, $y(t)$, and shaking table, $f(t)$, respectively.

Figures 2.5 and 2.6 show the transfer functions of instruments 290 and 300, for the different driving forces, E1 Centro (1) and (2). The curves show that at frequencies below $16 \mathrm{~Hz},|\mathrm{H}(\omega)|$ is approximately equal to one. This means that below 16 Hz the signal recorded by the instrument is essentially the same as the movement of the shaking table. Comparison of the recorded response of the instrument with the input motion indicates close agreement.

### 2.4 Field Adjustments

A typical field installation is shown in Fig. 2.7. The elements of the array are routinely checked every 2 to 3 days in accordance with the following directions to the local operator:

1. Before visiting station, observe clock error of $T S-500$ on scope. Adjust clock to zero error once every two weeks.
2. On entry to station, take a general look at the system. The "clock" lamp on DR-100 should flash once per second. Turn on "display" switch to make sure that the clock works in normal conditions.
3. Read event number and record it on operational $\log$.
4. Check the time error between $T S-500$ and $D R-100$. Enter the time and time error on this operational log. On giving a "step" calibration
or writing a time error from the $T S-500$, make a note on the operational $\log$ and observe the tape movement. Adjust DR-100 clock to zero error once every two weeks (after TS-500 adjustment).
5. Use a digital voltage meter to check external battery voltage and record on operational $10 g$.
6. Replace external battery at each station once a week.
7. Measure output signal of each channel of the SA-3000 accelerometer and record on the operational log.
8. Do not change sample rate and time duration switch.
9. If a change in trigger level is made or the tape is replaced, make a note on the operational log.
10. Before leaving the station, observe event number again and turn display off.
11. Immediately following an earthquake, each station should be visited. Write time error on the tape and operational log, then replace the tape. Send data back to the Institute as soon as possible.

TABLE 2.1

Deviation of Actual Site Locations from the Planned Configuration

| Station | Distance <br> Error <br> (meters) | Azimuth <br> Error <br> (degrees) | Station | Distance <br> Error <br> (meters) | Azimuth <br> Error <br> (degrees) |
| :--- | :---: | :---: | :---: | :---: | :---: |
| I01 | -6.7 | -3.29 | M07 | +22.9 | +2.65 |
| I02 | -6.1 | +0.74 | M08 | -16.3 | -1.84 |
| I03 | +4.2 | -0.95 | M09 | +33.9 | -3.87 |
| I04 | +6.8 | -0.31 | M10 | -77.0 | -3.9 |
| I05 | +1.8 | -0.76 | M11 | +2.0 | $0 \%$ |
| I06 | -6.4 | +4.06 | M12 | +3.5 | +0.57 |
| I07 | +0.6 | +2.62 | 001 | +26.4 | -1.27 |
| I08 | -12.3 | -1.71 | 002 | +8.2 | -0.17 |
| I09 | +6.9 | -0.43 | 003 | +40.7 | +0.31 |
| I10 | -0.3 | -1.83 | 004 | -15.7 | -1.59 |
| I11 | -18.4 | -0.90 | 005 | -1.0 | -2.68 |
| I12 | +1.4 | +0.54 | 006 | +10.2 | -0.55 |
| M01 | -8.1 | -1.12 | 007 | +0.8 | -1.38 |
| M02 | +99.9 | -3.04 | 008 | +56.4 | -3.19 |
| M03 | -53.9 | -3.97 | 009 | +45.2 | -2.44 |
| M04 | +12.5 | +0.19 | 010 | +2.9 | +0.40 |
| M05 | -39.9 | -3.06 | 011 | -51.2 | -0.03 |
| M06 | +2.7 | -0.21 | 012 | -3.6 | +0.17 |

RANGE: $\pm 2.0 \mathrm{~g}$
SCALE FACTOR: $3.75 \mathrm{v} / \mathrm{g}$
INPUT POWER: + 12 vdc @ 165 ma
RESOLUTION: $0.001 \%$ of full scale
NON-LINEARITY: Less than $0.2 \%$ of full scale
HYSTERESIS: Less than $0.05 \%$ of full scale
CROSS-AXIS SENSITIVITY: Less than $1 \%$
TEMPERATURE SENSITIVITY: Less than $0.01 \%$ per degree $F$
NATURAL FREQUENCY: $>50 \mathrm{~Hz}$
DAMPING RATIO: $0.7 \pm 0.2$
ZERO OUTPUT: Less than 0.50\%
TEMPERATURE RANGE:

$$
\begin{array}{ll}
65^{\circ} \mathrm{F} \text { to } 200^{\circ} \mathrm{F} & \text { storage } \\
0^{\circ} \mathrm{F} \text { to } 150^{\circ} \mathrm{F} & \text { operation }
\end{array}
$$





Fig. 2.3 Comparison between input acceleration and instrument response from shaking table test

Fig. 2.4 Diagrammatic representation of shaking table test



[^1]Instrument No. 290
Input: El Centro, Horizontal(NS Component)

Fig. 2.6 Instrument transfer function for El Centro horizontal input


Fig. 2.7 Typical field installation

## 3. A PRELIMINARY STUDY OF THE TAIWAN STRONG MOTION ARRAY DATA

### 3.1 Description of Available SMART 1 Data

During the first six-month period of operation, from October 1980 to March 1981, SMART I was triggered partially or wholly by nine earthquakes. Most analysis to date has been given to this early data set. The parameters of these earthquakes are listed in Table 1.2 , together with preliminary results for six subsequent earthquakes up till October 1981. The earthquakes in the total set are referred to as Event 1 through Event 15. The recorded maximum peak accelerations of the vertical, EW, and NS components of each earthquake are also included in Table 1.2. The epicenters of the first nine earthquakes are shown in Fig. 3.1. Table 1.2 and Fig. 3.1 show that three earthquakes with $M_{L}$ in the range $5.6-5.9$ were located almost directly below SMART 1 at depths ranging from 59 to 76 km . The remaining six earthquakes with $M_{L}$ in the range 3.8 to 6.9 were all shallow, with depths ranging from 7 to 43 km . The epicentral distance ranges from 7 to 193 km . The ratio of triggered instruments to operational instruments ranges from $2 / 27$ to $27 / 27$ for the first nine earthquakes. With only few exceptions, failure to trigger was simply because actual ground accelerations did not reach the preset trigger levels of $10-15$ gals. The highest acceleration recorded during the initial twelve-month period was 244 gals.

Following each event, the triggered tape cassettes were retrieved from the field and returned to the Institute of Earth Sciences, Taipei, where their contents were transferred onto a regular 9-track magnetic tape (see Section 2.2). The data on this regular tape were then read into a computer for decoding, checking, editing and correction for $D C$ offsets before they were stored onto a data tape for further processing. Time corrections of individual records were included in the event header.

Figures 3.2a, b, and chow recorded waveforms of the vertical, EW and NS components, respectively, for Event 2 , the $M_{L}=5.9$ earthquake of November 14, 1980. This earthquake at 62 km depth was only 10 km from SMART 1 , so that it was located almost right under the array; 16 out of the 21 operating instruments were triggered. Both P and S waves were recorded, showing an S-P time of about 9 sec. A small delay of $P$ waves as well as of $S$ waves across the array was observed, consistent with the near-vertical incidence of these waves. The signal levels of the vertical component (primarily P waves) were significantly lower than those of both the EW component (primarily SH waves) and the NS component (primarily SV waves). The two horizontal components had about the same strength. The waveforms of individual components varied considerably across the array. Figures 3.3a, b and c show recorded waveforms for Event 5.

Tables 3.1 and 3.2 list the peak accelerations of the vertical, EW and NS components and their occurrence times recorded by SMART 1 for Events 2 and 5 , respectively. The values range from 9.3 to 29.7 gal, 19.9 to 69.7 gal and 29.0 to 78.7 gal for the vertical, EW and NS components, respectively, so that the peak accelerations vary by a factor of 2 to 4 across the array. The following two observations can be made from these results. First, variations in both vertical and horizontal peak accelerations by a factor of 2 to 3 were not uncommon over a circular area having a radius of only 2 km . Secondly, the peak accelerations of the horizontal components were about 3 times greater than those of the vertical component.

A comparison between the free-field motion and the motion recorded by an analog-recording SMA-1 instrument at the Lotung Town Hall in the SMART 1 area can be seen from Figs. 3.4a and b.
3.2 Correlation Coefficients of Acceleration Waveforms Across SMART 1

An important consideration in the design of a long-base structure concerns the coherency of input acceleration functions at different points of its base. The SMART 1 data provide valuable information for this problem. The correlation coefficients $\rho_{i j}$ (see Chapter 7) between the acceleration waveforms of the same component recorded at two array sites were computed. The results are plotted as a function of site separation for the largest intermediate-depth earthquake, Event 2, whose waves arrive at the array in a nearly vertical direction, and for the largest shallow earthquake, Event 5, whose waves arrive at the array in a more horizontal direction.

Figure 3.5 shows the correlation coefficient $\rho_{i j}$ for the vertical, $E W$, and NS components for Event 5 to be about $0.5,0.6$, and 0.7 , respectively, at site separation about 0.2 km . For larger site separations, $\rho_{i j}$ drops to within $\pm 0.2, \pm 0.3$, and $\pm 0.4$ for the vertical, $E W$, and NS components, respectively. Thus, the waveforms are better correlated for the NS component than for the EW component. The vertical component has the poorest correlation.

TABLE 3.1
Maximum Acceleration: Event 2

EARTHQUAKE OF NOV. 14, 1980, 13H, 37M, 4.00S (GMT)
EPICENTER: 121-47.49E 24-35.14N
DEPTH : 62.06 (KM)
MAGNITUDE: 5.90

| STATION CODE | G COMPONENT | EW COMPONENT | NS COMPONENT |  |  |  |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
|  | gal | second | gal | second | gal | second |
| C00 | 19.8 | 24.342 | 56.8 | 23.522 | 49.7 | 25.732 |
| I03 | 23.4 | 22.626 | 34.4 | 23.946 | 45.0 | 24.606 |
| I06 | 19.5 | 23.578 | 31.0 | 23.508 | 29.0 | 25.688 |
| M02 | 29.7 | 15.297 | 60.3 | 25.387 | 78.7 | 23.377 |
| M03 | 14.9 | 22.637 | 19.9 | 27.557 | 40.1 | 24.547 |
| M04 | 14.4 | 15.037 | 37.0 | 25.597 | 39.2 | 24.017 |
| M05 | 21.4 | 15.402 | 49.2 | 23.182 | 36.7 | 25.392 |
| M06 | 24.2 | 24.709 | 28.3 | 22.999 | 40.6 | 24.709 |
| M08 | 17.0 | 22.936 | 67.8 | 23.486 | 35.1 | 23.746 |
| M09 | 11.5 | 15.442 | 27.7 | 23.472 | 29.8 | 24.672 |
| M10 | 17.9 | 23.936 | 61.5 | 24.866 | 60.9 | 24.616 |
| M12 | 21.5 | 25.506 | 34.3 | 24.616 | 36.2 | 23.546 |
| O03 | 20.4 | 15.023 | 37.0 | 24.013 | 68.6 | 24.853 |
| O06 | 27.9 | 23.841 | 69.7 | 24.031 | 72.8 | 23.931 |
| O09 | 20.8 | 23.428 | 42.4 | 24.478 | 38.9 | 23.748 |
| O12 | 9.3 | 22.647 | 51.9 | 24.277 | 33.2. | 24.067 |

TABLE 3.2
Maximum Acceleration: Event 5
EARTHQUAKE OF JAN. 29, 1981, 4H, 51M, 36.06 S (GMT)
EPICENTER: 121-53.78E 24-25.75N
DEPTH : 11.05 (KM)
MAGNITUDE: 6.9


TABLE 3.2 (continued)

| STATION CODE | V COMPONENT |  | EW COMPONENT | NS COMPONENT |  |  |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
|  | gal | second | gal | second | gal | second |
| 005 | 23.4 | 43.560 | 97.7 | 47.790 | 115.4 | 48.330 |
| 006 | 39.8 | 47.183 | 117.8 | 48.653 | 102.7 | 48.343 |
| 007 | 27.4 | 47.240 | 84.5 | 48.130 | 79.3 | 48.060 |
| 009 | 34.7 | 47.310 | 116.2 | 48.220 | 92.7 | 49.200 |
| 010 | 40.9 | 48.478 | 90.1 | 48.458 | 112.3 | 48.508 |
| 012 | 26.8 | 47.822 | 87.0 | 48.622 | 161.5 | 48.682 |



Fig. 3.1 Location of SMART 1 and epicenters of earthquakes recorded during the first six months of operation

SMART 1 PLAYBACK TRACES
Vertical scale $1 \mathrm{~cm}=100 \mathrm{GAL}$
Vertical scale $1 \mathrm{~cm}=100 \mathrm{GAL}$
smart 1 playback traces 212

SMART 1 PLAYBACK TRACES
Vertical scale $1 \mathrm{~cm}=300 \mathrm{GAL}$

SMART 1 PLAYBACK TRACES
Vertical scale $1 \mathrm{~cm}=300 \mathrm{GAL}$
EW component

 COB 11 .
 CO5 $\square$ $\square$ 1me iesci Acceleration waveforms of the EW component of Event 5 Fig. 3.3b
SMART 1 PLAYBACK TRACES
Vertical scale $1 \mathrm{~cm}=300 \mathrm{GAL}$
NS component


EARTHQUAKE No. 5 (1981-01-29-04. 51 GMT) STATION LOTUNG (1)




Fig. 3.5a Correlation coefficients of the whole waveform between paired sites for Event 5


Fig. 3.5b. Correlation coefficients of the waveform for the low-frequency band between paired sites for Event 5


Fig. 3.5c. Correlation coefficients of the waveform for the high-frequency band between paired sites for Event 5

## 4. DATA PROCESSING

### 4.1 Timing

SMART 1 is designed so that individual elements trigger when seismic waves having peak accelerations above 0.01 g propagate across the Lotung area. Complete wave trains are obtained because of the 2.5 second memory associated with each element. Universal time, correct to at least 0.01 sec , is marked on each tape at the time of the first earthquake that triggers the element. Timing of aftershocks is given by the relative interoccurrence times specified by the internal crystal clock. Immediately after a significant earthquake is recorded, technicians check the internal clock of each element with the portable comparator. This final check of the internal clock is made no later than two or three hours after the recording of the main shock so that inter-element time corrections are less than 0.01 sec . In this section, some basic processing of recorded data from SMART 1 is discussed.

### 4.2 Digital Processing

The cassettes obtained in the field at the array elements are taken to the digital playback system (shown in Fig. 4.1) at the Institute of Earth Sciences in Taipei, where they are converted to computer-compatible digital stacks and filed on magnetic tape by the laboratory playback system.

When the recorded cassette tapes are sent back to the laboratory, they are played back on paper for visual inspection. Valid records are picked out and transformed from the cassette tapes to a regular 9-track magnetic tape. The raw data tape is then read into a computer for decoding and editing. The edited records with related header information are written onto a user's data tape for further processing.

The traces of the $V$, EW, and NS components of acceleration recorded by each element are plotted for easy visual inspection by potential users of the

SMART 1 data. The digital format of recording makes it possible to perform fast data processing on an extensive scale. The following six steps summarize the decoding and editing involved in the processing of the SMART I data.
a) The recorded cassette tapes are played back on paper. On these playback traces, the number of stations that recorded during the earthquake are marked as well as the event number and the maximum ground acceleration (see Figs. 3.2 and 3.3).
b) The recorded cassette tapes are transformed to 9-track magnetic tape.
c) Decode: The seismic event is recorded as a file consisting of 5120 character records for header, data and trailer. The number of records per file depends on the event duration. The file organization is shown in Tables 4.1 to 4.4.
d) The record is printed out and errors corrected. Both the original record and the transformed record (decode) are printed out. The error corrections are needed for missing data, adjustments for time mark errors, glitches and D.C. shifts. Examples of possible errors are given in Figs. 4.2 to 4.4 .
e) The time correction, hypocentral location, and magnitude are all inserted in the data. The time correction is shown in Fig. 4.5 .
f) The corrected data are transferred to regular 9-track magnetic tape.

After data processing, the basic instrument correction and base-line correction developed by Trifunac $^{1}$ and Hudson ${ }^{2}$ are applied. Then the Fourier amplitude spectrum, response spectrum, correlation coefficient and the velocity and displacement are calculated from the corrected data. The data processing procedure is shown graphically in Fig. 4.6.

The natural frequency of the $\operatorname{SMART} I$ instrument is $>50 \mathrm{~Hz}$ and the damping ratio is $0.7 \pm 0.2$ critical damping; however, the cutoff-frequency of the 3-channel, anti-aliasing filter (5-pole low-pass Butterworth) is set to 25 Hz . The filter response curve for the test input which is shown in Fig. 4.7 indicates that the recorded accelerogram is quite close to the ground acceleration. Hence, no instrument correction was applied to the SMART 1 data. The positive direction of the recording is shown in Fig. 4.8.

### 4.3 References

1. Trifunac, M.D., "A Note on Correction of Strong Motion Accelerograms for Instrument Response," Bull. Seisn. Soc. Am., 62, No. 1, 401-409 (1972).
2. Hudson, E.C., Reading and Interpreting Strong Motion Records, Earthquake Engineering Research Institute, Berkeley, California (1979) .

TABLE 4.1
File Organization

A file consists of records as follows:

| $\frac{\text { Record }}{1}$ | $\frac{\text { Data }}{}$ |
| :---: | :---: |
| 2 | Header Data |
| $"$ | Digital Data |
| " | " |
| " | ". |
| N | Digital Data |
| N+1 | Trailer Data |
| File Mark |  |

TABLE 4.2
Header Record
The header record is a 5120 character record consisting of ASCII coded BCD for DAYS, HRS, MINS, SEC, SERIAL NUMBER of recorder, EVENT COUNT, and SYSTEM (16 characters). The remaining characters in the record are ASCII spaces (Hex 20). A header record is therefore:

| Char. 1 | Data |
| :---: | :--- |
| 1 | Days MSD $(N * 100)$ |
| 2 | Days MSD $(N * 10)$ |
| 3 | Days LSD $(N * 1)$ |
| 4 | Hours MSD $(N * 10)$ |
| 5 | Hours LSD $(N * 1)$ |
| 6 | Mins MSD $(N * 10)$ |
| 7 | Mins LSD $(N * 1)$ |
| 8 | Secs MSD $(N * 10)$ |
| 9 | Secs LSD $(N * 1)$ |
| 10 | S/N MSD $(N * 100)$ |
| 11 | S/N MSD $(N * 10)$ |
| 12 | S/N LSD $(N * 1)$ |
| 13 | EV MSD $(N * 10)$ |
| 14 | EV LSD $(N * 1)$ |
| 15 | SYS MSD $(N * 10)$ |
| 16 | SYS LSD $(N * 1)$ |
| 17 | ASCII Spaces |
| 17 | 1 |

TABLE 4.3
Data Record
The data samples are formatted into 6 ASCII characters per sample, as follows:

| Char.\# |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| 1 | ID\#1. | ASCII | 0,1, | or 2 V |
| 2 | SIGN | ASCII | + or | - |
| 3 | MSD | ASCII | BCD | ( $\mathrm{N} * 1000$ ) |
| 4 | " |  |  | ( $\mathrm{N} \times 100$ ) |
| 5 | " | " | " | ( $\mathrm{N} * 10$ ) |
| 6 | L.SD |  |  | $(\mathrm{N} * 1)$ |

The above pattern repeats for 853 samples ( 284 samples/channel), a total of 5118 characters. The remaining 2 characters are ASCII spaces.

TABLE 4.4
Trailer Record
The trailer record is a 5120 character record consisting of 16 ASCII coded BCD characters and 5104 ASCII nulls (Hex 00). A trailer record is as follows:

| Char.\# | Data |
| :---: | :---: |
| 1 | Days MSD ( ${ }^{*} 100$ ) |
| 2 | Days MSD ( $\mathrm{N} * 10$ ) |
| 3 | Days LSD ( $\mathrm{N} * 1$ ) |
| 4 | Hours MSC ( $\mathrm{N} * 10$ ) |
| 5 | Hours LSD ( $\mathrm{N} \div 1$ ) |
| 6 | Mins MSD ( $\mathrm{N} * 10$ ) |
| 7 | Mins LSD ( $\mathrm{N} * 1$ ) |
| 8 | Secs. MSD ( $\mathrm{N} * 10$ ) |
| 9 | Secs LSD ( $\mathrm{N} *$ 1) |
| 10 | S/N MSD ( $\mathrm{N} * 100$ ) |
| 11 | S/N " ( $\mathrm{N} * 10$ ) |
| 12 | S/N LSD ( $\mathrm{N} \div 1$ ) |
| 13 | EV MSD ( $N * 10$ ) |
| 14 | EV LSD ( $\mathrm{N} * 1$ ) |
| 15 | SYS MSD ( $\mathrm{N} * 10$ ) |
| 16 | SYS LSD ( $\mathrm{N} * 1$ ) |
| 17 | ASCII Nulls |
| " | " |
| 5120 |  |



Fig. 4.1 Digital playback system DP-200

| $0+0000$ | $1-0004$ | $2+0006$ | $0+0000$ | $1-0004$ | $2+0006$ | $0+0000$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $0+0000$ | $1-0002$ | $2+0002$ | $0-0001$ | $1-0002$ | $2+0002$ | $0+0000$ |
| $0+0000$ | $1-0002$ | $2+0002$ | $0+0000$ | $1+0000$ | $2+0000$ | $0+0000$ |
| $0+0000$ | $1+0000$ | $2+0002$ | $0+0000$ | $1+0000$ | $2+0002$ | $0+0000$ |
| $0-0002$ | $1-0002$ | $2+0003$ | $0-0002$ | $1+0000$ | $2+0002$ | $0-0002$ |
| $0+0000$ | $1-0002$ | $2+0003$ | $0+0000$ | $1-0002$ | $2+0002$ | $0+0000$ |
| $0-0002$ | $1-0002$ | $2+0002$ | $0-0002$ | $1-0002$ | $2+0002$ | $0+0000$ |
| $0+0000$ | $1-0002$ | $2+0002$ | $0+0000$ | $1+0000$ | $2+0003$ | $0+0000$ |
| $0+0000$ | $1+0000$ | $2+0003$ | $0+0000$ | $1+0000$ | $2+0003$ | $0+0000$ |
| $0+0000$ | $1-0002$ | $2+0002$ | $0-0001$ | $1-0002$ | $2+0002$ | $0+0000$ |
| $0+0000$ | $1+0000$ | $2+0002$ | $0+0000$ | $1+0000$ | $2+0002$ | $0-0002$ |
| $0-0002$ | $1+0000$ | $2+0002$ | $0-0002$ | $1+0000$ | $2+0002$ | $0-0002$ |
| $0+0000$ | $1+0000$ | $2+0003$ | $0+0000$ | $1+0000$ | $2+0003$ | $0+0000$ |
| $0+0000$ | $1+0000$ | $2+0003$ | $0+0000$ | $1+0000$ | $2+0003$ | $0+0000$ |
| $0+0000$ | $1+0000$ | $2+0002$ | $0+0000$ | $1+0000$ | $2+0002$ | $0+0000$ |
| $0+0000$ | $1-0002$ | $2+0003$ | $0+0000$ | $1-0002$ | $2+0003$ | $0-0002$ |
| $0+0000$ | $1-0002$ | $2+0002$ | $0+0500$ | $1-0002$ | $2+0002$ | $0+0000$ |
| $0+0000$ | $1-0002$ | $2+0003$ | $0+0000$ | $1-0002$ | $2+0003$ | $0+0000$ |
| $0-0002$ | $1-0002$ | $2+0003[0-0002$ | $1+00$ |  |  |  |

Fig. 4.2 Data missing at end of file

| 2+0002 | - | 1-0005 | 3 | 0-0013 |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2+0005 | 0-0013 | 1-000 | 2+0003 | 0-0013 | 1-0002 | $2+8203$ | 0-0013 |
| 2+0004 | 0-0011 | 1-0008 | $2+0005$ | 0-0011 | 1-0007 | $2+8006$ | 0-0012 |
| $2+0005$ | $0-0013$ | 1-0012 | $2+0005$ | $0-0013$ | 1-0012 | 2+000 | 0-0014 |
| 2+0005 | 0-0014 | 1-00.98 | $2+0005$ | 0-0014 | 3-0008 | 2+0004 | 0-0014 |
| 2+0000 | 0-0015 | 1-0007 | $2+0001$ | 0-0015 | 1-0009 | 2+0001 | 0-0015 |
| 2+0002 | 0-0010 | 1-0011 | $2+0003$ | 0-0010 | 1-0010 | $2+6003$ | 0-0011 |
| +0002 | 0-00:3 | 1-0.11 | 2+0001 | 0-0013 | 1-0011 | 2+0.00 | 0-0013 |
| 2-0003 | $0+2047$ | $1+2047$ | $2+2047$ | 0+2047 | 1+2047 | $2+2047$ | 0-0013 |
| +0002 | 0-0013 | 1-C005 | $2+0001$ | -0013 | 1-0004 | $2^{3}+0201$ | 0-6014 |
| $2+0007$ | 0-0013 | 1-0007 | $2+0003$ | 0-0013 | 1-0007 | 2+0310 | 0-0011 |
| $2+0007$ | 0-0013 | 1-0009 | $2+0003$ | 0-0013 | 1-0010 | $2+0500$ | 0-0014 |
| E+0001 | 0-0013 | 1-0012 | 2+0002 | 0-0013 | 1-0092 | $2+0503$ | 0-0012 |
| 2+0005 | 0-0013 | 1-0009 | $2+0003$ | 0-0013 | 1-0008 | 2+000: | 0-0013 |
| 2+0001 | $0-0013$ | 1-0007 | 2+0002 | -0013 | 1-000日 | 2+0002 | 0-0013 |
| $2+0005$ | 0-0013 | 1-0011 | 2+0005 | 0-0013 | 1-0011 | 2+0204 | 0-0013 |
| +0001 | C-00 | $1-$ | $2+0000$ | $0-0$ | 1-0 | 玉 | 0-0013 |

Fig. 4.3 Repeated time mark occurring in
the middle of the data file

FILE 53191337252990132

| 2-0683 | 0-0634 | 1-1878 | 0-0683 | $1+0514$ | 0-0683 |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $1 .+0680$ | 707 | 0-0763 | 1+0682 | 0-0594 | 197 | $0 \div 83$ | 1+0692 |  |
| 0-0683 | $1+0642$ | 0-0683 | 1+0652 |  |  | 0003 | 1+0002 | 3 |
| 0+0000 | 1+000 | 2-0006 | 0+0000 | 1+0000 | 2-0008 | 0+0000 | $1+0000$ | 1 |
| $0+0000$ | $1+0003$ | 2-0002 | 0-0002 | $1+0003$ | 2-0002 | 0-0003 | $1+0003$ |  |
| 0+0003 | 1+0002 | 05 | 0+0005 | $1+0000$ | 2-0006 | $0+0004$ | 1-0001 | 07 |
| $0+0001$ | $1+0000$ | 2-0006 | 0+0000 | $1+0000$ | 2-0004 | 0-000: | $1+0000$ | 0 |
| 0-0003 | $1+0000$ | 2-0002 | 0-0002 | 1-0002 | 2-0002 | $0+000$ | $1+0000$ | -0004 |
| $0+0003$ | +0003 | 2-0004 | 0+0003 | $1+0002$ | 2-0002 | 0+000.3 | +C0.0 | - |
| 0+0004 | $1+0000$ | 2+000 | 0+0002 | $1+0002$ | $2+0002$ | $0+0000$ | +0002 | 02 |
| 0 | $1+$ | 2-0002 | $0+0000$ | $1+0002$ | 2-0004 | 0 | $1+0000$ | -0006 |
| 00 | 1+0000 | 2-0004 | $0+0002$ | $1+0000$ | -0002 | 0+000? | +0000 | , |
| 0+0000 | $1+0002$ | 2-0006 | 0-0002 | $1+0000$ | 2-0006 | 0-0003 | +0000 | 06 |
| +0002 | $1+0000$ | $2+0000$ | 0+0002 | $1+0000$ | 2+0002 | 0+0003 | $1+0000$ | 0 |
| 0+0003 | $1+0002$ | 2-0006 | 0+0002 | $1+0002$ | 2-0006 | $0+0000$ | $1+0002$ |  |
| 0+0000 | $1+0000$ | 2-0014 | 0+0002 | $1+0002$ | 2-0013 | 0+0005 | $1+0003$ | -0010. |
| +0003 | $1+0002$ | 2-0004 | $0+0002$ | $1+0002$ | 2-0002 | $0+0000$ | $1+0000$ | -0002 |

Fig. 4.4a Glitch in the data at beginning of the data file

|  | 0+0002 |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | 2 |  |  |  |  |  |
|  | $0+$ | $1+0003$ | ? | $0+0003$ |  |  |  |  |
|  | O+ | $1+0003$ | ? | $0+0003$ |  |  |  |  |
|  | 0+0001 |  |  | $0+0000$ |  |  |  |  |
|  |  |  | $2+0005$ | - | $1+0004$ | $2+0006$ | +6002 |  |
|  |  | $1+0003$ | 2+0005 |  | $1+0003$ |  |  | 4 |
| S | $4+$ | $1-2040$ | 2-2035 | 10 |  | $2+0006$ |  |  |
| O | 0+000 | 1+0003 | 2+000' |  | $1+$ | $2+0005$ |  |  |
| 005 | 0-0003 | $1+000$ |  | -000 | $1+$ | 6 |  | +0005 |
| $2+0005$ | 0 | 1 | - |  |  |  |  |  |
|  | 0+0004 |  | , |  |  |  |  | $1+0003$ |
|  | 0+0004 | 1 |  |  | $1+0002$ |  |  |  |
|  | $0+0000$ | $1+0003$ |  |  |  |  |  |  |
| $+$ | $+000$ | $1+$ | 00 | + | $1+$ | $+0004$ |  |  |

Fig. 4.4b Glitch in the data at the middle of the data file

$T_{1}$ : Time of the time-error checking before event
$\mathrm{T}_{2}$ : Time of the time-error checking after event
$T_{E}$ : Time of event
$\Delta T_{s}: \begin{aligned} & \text { Time-error of } T S-500 \text { time comparator (checked by standard } \\ & \text { time receiver and scope }\end{aligned}$
$\Delta T_{r}$ : Time-error between $T S-500$ and DR-100 digital event recorder
$\Delta \mathrm{T}_{\mathrm{a}}$ : Actual time-error used for correction
$\Delta \mathrm{T}_{\mathrm{l}}$ : Estimated time-error (by using linear interpolation)
$\Delta \mathrm{T}_{\ell}-\Delta \mathrm{T}_{\mathrm{a}}$ : Error of time correction (should be $<10$ millisec.)

Fig. 4.5 Time correction


Fig. 4.6 Data processing procedure
(ga) NOILVONGLLV



POSITIVE OUTPUT FROM THE SENSORS RESULTS FROM ACCELERATIONS WHICH CAUSE GROUND MOTION AS SHOWN

Fig. 4.8 Positive direction of sensor

### 5.1 Introduction

The format of SMART 1 records makes processing by computer relatively fast and easy. For instance, the Fourier spectra of the considerable number of records obtained in the first six months were calculated in one pass. This speed is difficult to match with conventional film accelerograms. Because absolute time is available, the records can be correlated against epicentral distance in real time.

The high $P$ wave signal strength for the January 29, 1981 earthquake (Event 5) resulted in both $P$ and $S$ waves being recorded by all 27 operating instruments. The signal amplitudes are different for the three components, with the vertical and north-south components being the weakest and strongest, respectively.

### 5.2 Fourier Spectra and Response Spectra

Figure 5.1 shows the smoothed Fourier spectra of the acceleration waveforms of the vertical, EW and NS components at the Site $C 00$, at the center of the array, for Event 2, the November 14, 1980 earthquake of $M_{L}=5.9$. It should be noted that the vertical scales in each figure are not always the same for the three components. Variations in the Fourier spectra of the vertical components are greater than those of the horizontal components across SMART 1.

The SMART 1 records also permit the ready calculation of the response spectra. The group of records for the first six months was processed together to generate individual response spectra and produce mean response spectra. A goal of the project is, eventually, to separate the effects of site and source conditions on the response spectra by appropriate group
analysis. Figures $5.2 \mathrm{a}, \mathrm{b}$, and c show the response spectra of the vertical, EW and NS components, respectively, of the C00 records for Event 5, the January 29, 1981 earthquake of magnitude $M_{L}=6.9$. These curves are representative of the response curves of most sites for Event 5. They show that the NS component has more energy than the EW component for periods greater than 0.5 sec , and that the vertical component has significantly lower spectral levels and a flatter shape than the horizontal components.

Figures $5.3 \mathrm{a}, \mathrm{b}$, and c show the response spectra of the vertical, EW and NS components, respectively, of the C00 records for Event 2. For this earthquake, the EW and NS components have about the same spectral level and, as for Event 5, the vertical component has corresponding1y lower levels than the horizontal components. In comparison with Event 5, this event has relatively less energy for periods greater than one second than for shorter periods, especially in the case of the NS component.

In general, the shapes of the response spectra differ between vertical and horizontal components as well as between different earthquakes.

### 5.3 Frequency-Wave Number Spectra1 Analysis

Figure 5.4 shows the three components of ground motion measured at two array elements (stations 001 and 002) during Event 5. Wave trains of what are assumed a priori to be predominantly $P, S$ and surface waves can be seen lasting about 20 sec . Each record is aligned vertically according to Universal Time. The records demonstrate significant spatial variability (confirmed separately by the frequency spectrum analysis described in Section 5.2) between array elements about 1 km apart. This aspect of the variability of strong ground motion will be discussed at length in a later study.

Consider next the phased correlations of a specified portion of such records for a given component at all array elements so that not only the average power in the seismic signal may be estimated, but also the speed and direction of any coherently propagating seismic wave. A convenient method is to plot the power spectrum for a particular time window as a function of wave number $k$ (cycles per $k m$ ) and azimuth. An outline of the algorithm is given in Appendix $E$. If the $p l o t$ is made at a particular frequency $f$, the distance from the center is inversely proportional to the apparent wave speed $c$ (where $k c=f$ ).

As an illustration of the method, wave-number spectral plots are shown in Figs. 5.5 and 5.6 , computed using a high resolution algorithm ${ }^{1}$ from 26 SMART I vertical and north-south component accelerograms, respectively. (Digital data from one triggered element were not included in the analysis.) The two time windows chosen are marked 1 and 4, respectively, at the bottom of Fig. 5.4. Similar spectra of each ground motion component were computed for frequencies of $8,6,4,2,1,0.5,0.25$, and 0.125 Hz for each sequential time window, 1 through 5 in Fig. 5.4 , from the beginning to the end of the record. Preliminary analysis of these 120 spectral plots have been made but for the sake of brevity only Figs. 5.5 and 5.6 are reproduced here.

The spectra show that the wave trains in the first and second windows (each 4 sec long) correspond principally to $P$ waves crossing the array. In Fig. 5.5. the main power (marked A) is at 1 to 2 Hz and arrives at an apparent velocity of about $8.3 \mathrm{~km} / \mathrm{sec}$ (appropriate for $P$ waves) from an azimuth of $\mathrm{E} 58^{\circ} \mathrm{S}$. (The azimuth of the earthquake focus is $\mathrm{E} 64^{\circ} \mathrm{S}$. ) In the third window, the predominant maximum power (not shown here) is very coherent at 1 to 2 Hz , but propagates from $E 68^{\circ} \mathrm{S}$ at about $3 \mathrm{~km} / \mathrm{sec}$. This motion (see Fig, 5.4) corresponds mainly to Rayleigh and $S$ waves crossing
the array. The spectral plots show also that during this time interval a large amount of the energy being produced by the rupturing dislocation was being scattered away from the direct path between source and array. This scattering may be associated with structural irregularities in the crust and the superficial soil layers.

The spectrum shown in Fig. 5.6 for a window of 10 sec length in the coda of strong ground motion has a maximum peak energy (A) appropriate to waves moving with an apparent speed of $\because 1.0 \mathrm{~km} / \mathrm{sec}$ across the array from E $75^{\circ}$ S. The interpretation, supported by the orbital motion measured by the three components of acceleration, is that at this time the NS component of wave motion is predominantly of Rayleigh type. A summary of the estimated average apparent velocities and directions of approach of the seismic waves in each of the five time windows is given in Fig. 5.7. The diagram indicates that the preliminary body wave arrivals ( $P$ and $S$ waves) are from a direction to the east of the epicenter, while the later arrivals (surface coda waves) arrive successively from directions more and more westerly of the epicenter. This change in azimuth may be due to lateral refraction in the crustal structure or it may arise from the propagation of the seismic dislocation on the rupturing fault. A separate determination of the fault plane parameters is now under way.

### 5.4 Wave Coherency and Type

The above examples demonstrate that arrays like SMART 1 may have the capability, for the first time in seismology, of following the elastic dislocation as it moves along the fault. There is also the ability to determine whether, in a given time, the predominant seismic motion is of $P$ wave, $S$ wave or surface wave type. The lack of such identification has previously hindered crucial discrimination between theoretical models. The present prelimin-
ary analysis does not make use of the three recorded components of wave motion at each array element. The wave-number frequency spectral method can, however, be extended to this general case and orbits of the particle motions calculated.

A further use of the array data relates to two hypotheses now often appealed to: (1) that strong-motion accelerograms are largely superpositions of random motions ${ }^{2}$ and (2) that coda waves from local earthquakes arise from scattering ${ }^{3}$ from randomlymistributed heterogeneities in the crust. From SMART 1 recordings of the January 29 earthquake, both hypotheses appear to be only partly correct. Comparison of seismograms and wave-number frequency spectral plots shows that coherent energy (i.e., physically correlated) is present throughout the 20 sec duration of strong shaking, at least for frequencies $0.5<£<2 \mathrm{~Hz}$. (In this frequency range no problems from either spatial or temporal aliasing should arise.) Further, the major part of this coherent energy corresponds to the expected body and surface waves of seismology. In most time windows, however, at higher frequencies ( $f>6 \mathrm{~Hz}$ ), the wave number spectra lose coherence.

The illustration given in Fig. 5.8 is the NS component in window 3 ; the maximum energy (point A) is weak and represents very slow waves approaching from the southwest. At higher frequencies, the calculated spectra are consistent with the hypothesis of a large proportion of scattered waves arriving from widely-distributed heterogeneities. The actual extent of geological structural variations is not yet known from borehole information in the SMART 1 region. Seismic surveys indicate, however, a surficial layer of recent alluvium with $P$ wave velocities of 500 to $1000 \mathrm{~m} / \mathrm{sec}$ overlying pleistocene rock with $P$ wave velocities of 1800 to $2000 \mathrm{~m} / \mathrm{sec}$.

Another example of the capability of a near-source array like SMART 1 is that spatial correlations of waveform can answer the long-standing question of what is the minimum distance from the seismic source at which surface waves appear. Theoretical calculations are not specific and definite observational field evidence has not been observed. In the example above (Fig. 5.6), Rayleigh waves of period 2 sec are clearly present 30 km from the shallow-focus source. More extensive analyses ${ }^{4}$ of all the above questions will be given in later studies using the complete set of earthquakes recorded by SMART 1.

### 5.5 References

1. Capon, J., "High-Resolution Frequency-Wave Number Spectrum Analysis," Proc. IEEE, 57, 1408-1418 (1969).
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3. Aki, K. and B. Chouet, "Origin of Coda Waves, Source Attenuation and Scattering Effects," J. Geophys. Res., 80, 3322-3342 (1975).
4. Bolt, B.A., Tsai, Y.B, Yeh K. and M. K. Hsu, "Earthquake Strong Motions Recorded by a Large Near-Source Array of Digital Seismographs," Earthquake Eng. Struct. Dyn., 10, 561-573, (1982).


Fig. 5.1 Smoothed Fourier spectra of acceleration waveforms of the vertical, EW and NS components at C00 for Event 2

EARTHQUAKE NO. 5 (1981.1 . 29.4 .51) GMT
STATION COO COMP V
DAMPING VALUES ARE 0. 2. 5. 10 AND 20 PERCENT OF CRITICAL


Fig. 5.2a Response spectrum of the vertical component at C 00 for Event 5

EARTHQUAKE NO. 5 (1981.1 . 29.4 .51) GMT
STATION COO COMP EW
DAMPING VALUES ARE 0. 2. 5. 10 AND 20 PERCENT OF CRITICAL


Fig. 5.2b Response spectrum of the EW component at C00 for Event 5

EARTHQUAKE NO. 5 (1981.1 .29.4 .51) GMT
STATION COO COMP NS
DAMPING VALUES ARE 0. 2. 5. 10 AND 20 PERCENT OF CRITICAL


Fig. 5.2c Response spectrum of the NS component at C00 for Event 5

EARTHQUAKE NO. 2 (1980.11.14.13.37) GMT
STATION COO COMPONENT V
DAMPING VALUES ARE 0. 2. 5. 10 AND 20 PERCENT OF CRITICAL


Fig. 5.3a Response spectrum of the vertical component at C00 for Event 2


EARTHQUAKE NO. 2 (1980.11.14.13.37) GMT
STATION COO COMPONENT NS
DAMPING VALUES ARE 0. 2. 5. 10 AND 20 PERCENT OF CRITICAL


Fig. 5.3c Response spectrum of the NS component at COO for Event 2



Fig. 5.5 Contours of the summed power at 26 stations of the vertical component of seismic waves in time window 1 (see Fig. 5.4) at a frequency of 2 Hz plotted against wave number in the EW and NS directions. The circles indicate constant velocities of 5 and $10 \mathrm{~km} / \mathrm{sec}$. Peak power is at A.


Fig. 5.6 Similar wave number diagram to Fig. 5.5 for time window 4 and a frequency of 0.5 Hz . The clear peak A of high energy corresponds to coherent wave motion of period 2 sec across the array during this time interval with velocity $1 \mathrm{~km} / \mathrm{sec}$ and azimuth of approach E $75^{\circ} \mathrm{S}$.


Fig. 5.7 Vectors showing azimuth of approach and apparent velocity of the predominant coherent waves in five time intervals for Event 5 . (Epicenter azimuth is relative to array center.)


Fig. 5.8 Contours as in Fig. 5.5 of the NS component for time window 3 and a frequency of 6 Hz . The circles indicate constant velocities of 5 and $10 \mathrm{~km} / \mathrm{sec}$. The maximum power (point $A$ ) is now to be found to the southwest at an apparent velocity of $2.4 \mathrm{~km} / \mathrm{sec}$.
6. LOCAL MAGNITUDE VARIATIONS ACROSS ARRAY

### 6.1 Magnitude Measurements

For all records analyzed, the strong-motion accelerograms from stations of the SMART 1 array were converted to equivalent Wood-Anderson seismograms using a response spectrum written by A. Roca that is similar to that used by Kanamori and Jennings. ${ }^{1}$ Richter local magnitude is given as

$$
\begin{equation*}
M_{L}=\log A-\log A_{0} \tag{1}
\end{equation*}
$$

It was determined by two methods based on the peak amplitude $A$ (in millimeters) of the equivalent Wood-Anderson records as follows:

1. For the largest event of January 29, 1981 (see Table 1.2, Event 5), the equivalent Wood-Anderson seismogram appeared normal so that, by definition, the peak amplitude was taken to be the greatest value recorded for the zero-to-peak displacement on the Wood-Anderson record.
2. For the smaller events transformed, recordings (accelerogram or equivalent Wood-Anderson seismogram) showed evidence of incompleteness. Some records appeared to trigger late as distinct phases were not always readily apparent. Further, surface waves seemed disproportionately large, as if they had been used to set the record scale because $P$ and $S$ phases were missing. Long-period perturbations of the Wood-Anderson record were apparent in the records with low signal-to-noise ratio ( $\mathrm{S} / \mathrm{N}$ ). The causes for this arise from two sources: (i) when the $S / N$ is low, the least significant bit is unable to sample low signals adequately; (ii) a mid-record shift in the DC level is often apparent in the original accelerogram - a problem occurring in the early stages because of "sticky" pendulums in some of the new instruments.

In the second case, the peak amplitude was taken as one-half of the greatest manually-measured peak-to-peak Wood-Anderson displacement. The log of the peak Wood-Anderson displacement was averaged for the two horizontal components $(\log A)$ and added to $-\log A_{o}$, determined individually for each station by linearly interpolating the $-\log A_{o}$ table published by Richter. ${ }^{2}$

The adequacy of the second technique for determining $\log \mathrm{A}$ is not always assured because of subtle changes observed in the computed WoodAnderson records across the array. The technique, however, was employed for all events, except that of January 29, 1981. Further, an event recorded on March 22, 1981 had such extreme $S / N$ and DC-level shift problems that it was felt that even the second technique of amplitude measurement was not applicable.

It should be noted (Event 2, Table 1.2) that on November 14, 1980, a magnitude 5.9 earthquake (Taiwan magnitude) occurred about 10 km from the array, triggering several of the array instruments. Unfortunately for this study, the hypocenter was at a depth of over 60 km , precluding proper application of the Richter attenuation relation ( $-\log A_{o}$ versus distance), based on shallow southern California earthquakes (depth less than 15 km ).

The various measurements and computed magnitudes are listed in Table 6.1. The following summary compares the magnitudes of the earthquakes assigned by the Institute of Earth Sciences and also those determined from SMART 1.

| Event | Date | Taiwan ML | SMART $1 M_{L} \pm$ s.e. |
| :---: | :---: | :---: | :---: | :---: |
|  | October 18, 1980 | 5.8 | $5.66 \pm 0.08$ |
| 5 | January 29, 1981 | 6.9 | $6.24 \pm 0.08$ |
| 7 | March 2, 1981 | 6.9 | $6.51 \pm 0.04$ |
| 8 | March 10, 1981 | 4.4 | $4.10 \pm 0.11$ |

It is interesting to note that all magnitudes determined by SMART 1 are consistently smaller than those given by the Institute. Several
explanations may be offered.

1. The magnitude determination for many smaller earthquakes in Taiwan is based on measured durations. The single Wood-Anderson instrument at the Institute provides the calibration of the nationwide network of short period seismometers. Such procedures give rise to unresolved problems from the mechanisms and crustal scattering.
2. The attenuation curve, $-\log A_{o}$ versus distance, used for the SMART 1 magnitudes, was originally designed for southern California and may not be applicable to Taiwan earthquakes.
3. The final determination of Richter magnitudes assigned to an earthquake is meant to be made as an average of magnitude determinations over a wide azimuthal distribution. The area sampled by SMART 1 would normally be represented by only the Taipei Institute station (if any), and the results here may indicate that, due to local geologic conditions, magnitude estimates are lower for the SMART 1 area than the average over the rest of Taiwan.

### 6.2 Peak Amplitude Attenuation

The linear regression of the logarithm of peak amplitude onto distance was determined for several components, as listed in Table 6.1. Several of these are also plotted in Figs. 6.1 to 6.5.

We would expect that the slope of the regressed curve would be negative owing to the physics of attenuation. It is seen, however, that for some components the slope is positive, indicating that the peak amplitude is actually increasing with the distance travelled across the array. Though the data are scattered, these positive slopes appear significant. This is particularly true of the $\log$ A attenuation plot for January 29 ,

1981 (Fig. 6.1), which shows minimal scatter of the data points. Linear regression for the two horizontal components individually, $\log A_{E W}$ and $\log A_{N S}$, shows distinctly different attenuation curves. (N.B. For every station, $A_{N S}$ was greater than $A_{E W}{ }^{\circ}$ ) As Event 5 occurred SSE of the array, the difference between the two horizontal components indicates that significant $S V$ energy is contributing to the peak horizontal amplitude. Initially, it was supposed that as the seismic energy travelled across the array, there was refraction of the wavefronts due to the wedge-shaped delta structure under the Lotung area, causing a transfer of energy from the EW component into the NS component. On its own, however, this explanation of the transfer of horizontal component energy does not necessarily explain the positive slope in the $\log A$ plot. Further, the plot of $\log A_{H Z}(F i g .6 .2)$, where $A_{H Z}$ is the peak amplitude of the vector sum of the horizontal components, still shows an increase in peak amplitude with distance across the array. By comparison, the $\log$ peak amplitude plot for the vertical component (log $A_{Z}$ ), in Fig. 6.3, shows a definite negative slope. It is possible, cherefore, that path effects and mode conversion are enhancing the horizontal components of the waves by some transfer of energy from the vertical component.

The SMART 1 results also indicate that local (Richter) magnitude estimates are subject to significant variation due to local structural changes within a linear dimension of 2 km . Contours illustrating the $M_{L}$ variation for Event 5 are drawn in Fig. 6.6. The equivalent Richter magnitude for this earthquake ranged between 6.0 and 6.4 across SMART 1 with a mean of $6.24 \pm 0.08$. The scatter about the mean is not random, however, but as shown in Fig. 6.6, there is a systematic azimuthal trend.

It is important to reiterate that the local magnitude estimate for the January 29, 1981 main shock by the Institute of Earth Sciences in Taipei is
6.9. This value is calculated from a Wood-Anderson seismograph operated inTaipei and follows standard procedures used in Taiwan for many years. Adirect comparison between this value and the SMART 1 mean of 6.24 and the"true" Richter magnitude cannot be made because regional attenuation curvesare not vet available for Taiwan.
6.3 References1. Kanamori, H. and P.C. Jennings, "Determination of Local Magnitude,$M_{L}$, from Strong-Motion Accelerograms," Bull. Seism. Soc. Am.,68, 471-485 (1978).
2. Richter, C., Elementary Seismology, W.H. Freeman, San Francisco(1958).

TABLE 6.1

> Peak Amplitudes and Magnitudes (see Notes at end)
> October 18, 1980

| Station | Dist (km) | $-\log A_{0}$ | $\underline{\log \mathrm{A}_{\mathrm{Z}}}$ | $\mathrm{M}_{\mathrm{Z}}$ | $\underline{\log A}$ | $M_{L}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| C-00 | 45.47 | 2.509 | 2.862 | 5.371 | 3.243 | 5.753 |
| I-06 | 45.27 | 2.505 | 2.846 | 5.352 | 3.214 | 5.720 |
| I-09 | 45.45 | 2.509 | 3.000 | 5.509 | 3.262 | 5.771 |
| I-12 | 45.67 | 2.513 | 2.811 | 5.324 | 3.173 | 5.686 |
| M-01 | 46.37 | 2.527 | 2.747 | 5.275 | 3.177 | 5.704 |
| $\mathrm{M}-02$ | 46.14 | 2.523 | 2.661 | 5.184 | 3.197 | 5.720 |
| M-04 | 45.03 | 2.500 | 2.797 | 5.298 | 3.116 | 5.617 |
| M-05 | 44.70 | 2.494 | 2.777 | 5.271 | 3.059 | 5.553 |
| M-06 | 44.46 | 2.489 | 2.881 | 5.371 | 3.091 | 5.580 |
| M-07 | 44.19 | 2.484 | 2.863 | 5.347 | 3.138 | 5.622 |
| M-08 | 44.90 | 2.498 | 2.888 | 5.386 | 3.164 | 5.662 |
| M-10 | 45.82 | 2.516 | 2.827 | 5.344 | 3.200 | 5.716 |
| M-12 | 46.47 | 2.529 | 2.745 | 5.274 | 3.179 | 5.708 |
| 006 | 43.46 | 2.469 | 2.634 | 5.103 | 3.109 | 5.578 |
| 009 | 45.28 | 2.506 | 2.638 | 5.144 | 2.972 | 5.478 |
| 012 | 47.47 | 2.549 | 2.608 | 5.157 | 3.204 | 5.753 |
|  |  |  |  | $\bar{M}_{Z}=5.29$ | $\bar{M}_{L}$ | 5.66 $\pm 0$ |

TABLE 6.1 (continued)
January 29, 1981

| Station | Dist (km) | $\underline{-10 g} A_{0}$ | $\underline{\log \mathrm{A}_{2}}$ | $\underline{M}_{Z}$ | $\underline{\log A}$ | $M_{L}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{C}-00$ | 30.28 | 2.111 | 3.540 | 5.651 | 4.209 | 6.320 |
| I-03 | 30.25 | 2.110 | 3.343 | 5.453 | 4.198 | 6.308 |
| I-06 | 30.09 | 2.104 | 3.410 | 5.514 | 4.104 | 6.208 |
| I-12 | 30.48 | 2.119 | 3.523 | 5.642 | 4.147 | 6.266 |
| M-01 | 31.08 | 2.143 | 3.376 | 5.519 | 4.106 | 6.249 |
| M-02 | 30.75 | 2.130 | 3.430 | 5.560 | 4.151 | 6.281 |
| M-03 | 30.22 | 2.109 | 3.376 | 5.485 | 4.034 | 6.143 |
| M-04 | 29.65 | 2.086 | 3.526 | 5.612 | 4.147 | 6.233 |
| M-05 | 29.41 | 2.076 | 3.490 | 5.566 | 4.097 | 6.173 |
| M-06 | 29.29 | 2.071 | 3.952 | 6.024 | 4.137 | 6.208 |
| M-07 | 28.78 | 2.051 | 3.472 | 5.523 | 4.137 | 6.139 |
| M-08 | 29.91 | 2.096 | 3.650 | 5.746 | 4.185 | 6.281 |
| M-09 | 30.38 | 2.115 | 3.383 | 5.498 | 4.118 | 6.233 |
| M-10 | 30.82 | 2.133 | 3.424 | 5.557 | 4.137 | 6.270 |
| M-11 | 31.22 | 2.149 | 3.603 | 5.751 | - | - |
| M-12 | 31.27 | 2.151 | 3.469 | 5.620 | 4.134 | 6.285 |
| 0-01 | 31.92 | 2.177 | 3.352 | 5.529 | 4.184 | 6.361 |
| 0-02 | 31.07 | 2.143 | 3.442 | 5.585 | 4.202 | 6.345 |
| 0-03 | 30.03 | 2.101 | 3.437 | 5.538 | 4.125 | 6.226 |
| 0-04 | 29.12 | 2.065 | 3.367 | 5.432 | 4.097 | 6.162 |
| 0-05 | 28.46 | 2.038 | 3.523 | 5.562 | 4.008 | 6.046 |
| 0-06 | 28.29 | 2.031 | 3.476 | 5.508 | 4.118 | 6.149 |
| 0-07 | 28.71 | 2.048 | 3.624 | 5.672 | 4.093 | 6.141 |

## TABLE 6.1 (continued) <br> January 29, 1981

| Station | Dist (km) | $\underline{-10 g} A_{0}$ | $\underline{\log A_{Z}}$ | $\underline{M}_{Z}$ | $\underline{\log A}$ | M ${ }_{\text {L }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0-09 | 30.57 | 2.123 | 3.492 | 5.615 | 4.140 | 6.263 |
| 0-10 | 31.58 | 2.163 | 3.471 | 5.634 | 4.161 | 6.324 |
| 0-12 | 32.26 | 2.190 | 3.380 | 5.570 | 4.205 | 6.396 |
|  |  |  | $\bar{M}_{Z}=5.59$ |  | $\bar{M}_{L}=6.24$ |  |

TABLE 6.1 (continued)

## January 29, 1981

| Station | Dist (km) | $\underline{-10 g A_{0}}$ | $\xrightarrow{\log \mathrm{A}_{H Z}}$ | $\mathrm{M}_{\mathrm{HZ}}$ |
| :---: | :---: | :---: | :---: | :---: |
| C-00 | 30.28 | 2.111 | 4.572 | 6.683 |
| I-03 | 30.25 | 2.110 | 4.524 | 6.634 |
| I-06 | 30.09 | 2.104 | 4.446 | 6.550 |
| I-12 | 30.48 | 2.119 | 4.625 | 6.744 |
| M-01 | 31.08 | 2.143 | 4.712 | 6.855 |
| M-02 | 30.75 | 2.130 | 4.564 | 6.694 |
| M-03 | 30.22 | 2.109 | 4.514 | 6.622 |
| M-04 | 29.65 | 2.086 | 4.668 | 6.755 |
| M-05 | 29.41 | 2.076 | 4.593 | 6.669 |
| M-06 | 29.29 | 2.071 | 4.424 | 6.495 |
| M-07 | 28.78 | 2.051 | 4.549 | 6.600 |
| M-08 | 29.91 | 2.096 | 4.506 | 6.602 |
| M-09 | 30.38 | 2.115 | 4.471 | 6.587 |
| M-10 | 30.82 | 2.133 | 4.609 | 6.742 |
| M-11 | 31.22 | 2.149 | - | - |
| M-12 | 31.27 | 2.151 | 4.691 | 6.842 |
| 0-01 | 31.92 | 2.177 | 4.611 | 6.788 |
| 0-02 | 31.07 | 2.143 | 4.818 | 6.961 |
| 0-03 | 30.03 | 2.101 | 4.711 | 6.812 |
| 0-04 | 29.12 | 2.065 | 4.536 | 6.601 |
| 0-05 | 28.46 | 2.038 | 4.442 | 6.480 |
| 0-06 | 28.29 | 2.031 | 4.502 | 6.534 |
| 0-07 | 28.71 | 2.048 | 4.429 | 6.478 |
| 0-09 | 30.57 | 2.123 | 4.551 | 6.674 |
| O-10 | 31.58 | 2.163 | 4.487 | 6.650 |

## TABLE 6.1 (continued) <br> January 29, 1981



TABLE 6.1 (continued)

January 29, 1981

| Station | Dist (km) | ${\xrightarrow{\log A^{\prime}} \text { EW }}^{\text {d }}$ | $\xrightarrow{\text { log A }}$ AS $^{\text {N }}$ |
| :---: | :---: | :---: | :---: |
| $\mathrm{C}-00$ | 30.28 | 4.0648 | 4.3528 |
| I-03 | 30.25 | 4.0539 | 4.3419 |
| I-06 | 30.09 | 3.9434 | 4.2654 |
| I-12 | 30.48 | 3.9768 | 4.3178 |
| M-01 | 31.08 | 3.7960 | 4.4160 |
| M-02 | 30.75 | 3.9712 | 4.3305 |
| M-03 | 30.22 | 3.8423 | 4.2257 |
| M-04 | 29.65 | 4.0513 | 4.2429 |
| M-05 | 29.41 | 3.9941 | 4.2004 |
| M-06 | 29.29 | 4.0496 | 4.2244 |
| M-07 | 28.78 | 4.0238 | 4.2509 |
| M-08 | 29.91 | 4.0756 | 4.2909 |
| M-09 | 30.38 | 3.9488 | 4.2871 |
| M-10 | 30.82 | 3.9639 | 4.3097 |
| M-11 | 31.22 | - | 4.3236 |
| M-12 | 31.27 | 3.8723 | 4.3959 |
| O-01 | 31.92 | 3.9606 | 4.4073 |
| 0-02 | 31.07 | 3.8889 | 4.5144 |
| 0-03 | 30.03 | 4.0158 | 4.2335 |
| 0-04 | 29.12 | 4.0251 | 4.1694 |
| 0-05 | 28.46 | 3.9338 | 4.0816 |
| 0-06 | 28.29 | 4.0269 | 4.2082 |
| 0-07 | 28.71 | 3.9285 | 4.2568 |
| 0-09 | 30.57 | 3.9587 | 4.3222 |

TABLE 6.1 (continued)

January 29, 1981

| Station | Dist (km) | ${\underline{l o g} A_{E W}}^{\text {l }}$ | $\log ^{\text {A }}$ NS |
| :---: | :---: | :---: | :---: |
| 0-10 | 31.58 | 3.9910 | 4.3311 |
| $0-12$ | 32.26 | 3.9859 | 4.4244 |

March 2, 1981

| Station | Dist (km) | $\xrightarrow{-\log A_{0}}$ | ${\underline{L o g ~} A_{Z}}^{\text {l }}$ | $\mathrm{M}_{\mathrm{Z}}$ | $\underline{\log A}$ | $\mathrm{M}_{-}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| M-05 | 194.28 | 3.500 | 2.554 | 6.054 | 3.057 | 6.557 |
| 0-02 | 196.46 | 3.500 | - | - | 2.970 | 6.470 |
| 0-06 | 192.98 | 3.500 | 2.436 | 5.936 | 3.014 | 6.514 |
|  |  |  | $\bar{M}_{Z}=6.00$ |  | $\bar{M}_{L}=6.51$ |  |

TABLE 6.1 (continued)

March 10, 1981


## TABLE 6.1 (continued)

## Notes

1. $-\log A_{0}$ is linearly interpolated from values given in Richter ${ }^{2}$.
2. $\quad \log A=\left(\log A_{E W}+\log A_{N S}\right) / 2$ where $A_{E W}$ and $A_{N S}$ are peak amplitudes (in millimeters) for the Wood-Anderson instrument displacement on the eastwest and north-south components, respectively.
3. $A_{Z}$ is the peak vertical amplitude for an equivalent Wood-Anderson instrument.
4. $A_{H Z}$ is the peak horizontal amplitude measured from a record given by the Pythagorean (vector) sum of the two horizontal components.

TABLE 6.2
Attenuation Across SMART 1

Linear Regression (see Footnotes)

Type of Displacement
October 18, $1980 \Delta \sim 45 \mathrm{~km}$
${ }^{A} Z$
A
January 29, $1981 \Delta \sim 30 \mathrm{~km}$

| $\mathrm{A}_{\mathrm{Z}}$ | 4.751 | -0.0420 | 0.1221 |
| :--- | :--- | :--- | :--- |
| $\mathrm{~A}_{\mathrm{EW}}$ | 4.622 | -0.0215 | 0.1029 |
| $\mathrm{~A}_{\mathrm{NS}}$ | 2.152 | +0.0710 | 0.6615 |
| $\mathrm{~A}_{\mathrm{HZ}}$ | 3.025 | +0.0512 | 0.2784 |
| A | 3.364 | +0.0256 | 0.2980 |

March 2, $1981 \Delta \sim 194 \mathrm{~km}$

| $\mathrm{A}_{\mathrm{Z}}$ | -15.081 | +0.0908 | 1.0000 |
| :--- | ---: | ---: | ---: |
| A | 6.022 | -0.0155 | 0.3907 |

March 10, $1981 \Delta \sim 7 \mathrm{~km}$

| $A_{Z}$ | 2.201 | -0.0072 | 0.0013 |
| :--- | :--- | :--- | :--- |
| A | 2.884 | -0.0322 | 0.0731 |

* test for fit: $r^{2}=1$ for perfect fit
$\log A=a+b \Delta$
$A \equiv W-A$ displacement in millimeters
$\Delta \equiv$ epicentral distance in kilometers

Fig. 6.1 Attenuation curve of $\log$ A for Event 5 (January 29, 1981)






Fig. 6.6 Contours of computed Richter magnitude for Event 5. Values for individual magnitudes are shown at those array elements which recorded this earthquake.

## 7. IDENTIFICATION OF WAVE TYPES, DIRECTIONS, AND VELOCITIES

### 7.1 Correlation and Coherence

In an attempt to identify wave types, directions, and velocities produced by the earthquakes of November 14, 1980 (Event 2), and January 29, 1981, (Event 5), let us first examine the cross correlation coefficient given by

$$
\begin{equation*}
\rho_{i j}(\tau) \equiv \frac{R_{i j}(\tau)}{\sqrt{R_{i i}(0) R_{j j}(0)}} \tag{1}
\end{equation*}
$$

where

$$
R_{i j}(\tau) \equiv \int_{t_{0}-\Delta T / 2}^{t_{0}+\Delta T / 2} x_{i}(t) x_{j}(t+\tau) d t
$$

and where $x_{i}(t)$ and $x_{j}(t)$ are the recorded acceleration time-histories in the x-direction (see Fig. 7.1) at stations $i$ and $j$, respectively, $\Delta t$ is a time window centered on time $t_{0}$, and $\tau$ is a time lag. If the ground motions at these stations were produced primarily by a single travelling wave, then the above cross correlation coefficient, which can range from +1 to -1 , would show high correlation for $\tau$ equal to the time required for the wave to travel between the two stations. This value of $\tau$ would, of course, depend upon the direction of wave propagation as well as wave velocity.

Plots of the cross correlation coefficient given by (1) are shown in Figs. 7.2 a to 7.2 c for both earthquakes mentioned above using time windows which contain the significant high intensity motions as show in Fig. 7.3, and for selected station pairs as indicated. The distances given in these figures are true distances (not projected distances) between corresponding station pairs. The maximum absolute values of the cross correlation coefficients are shown in Fig. 7.4 along with an exponential curve fitted by least squares.

It is significant to note that the cross correlation coefficient plots in Figs. 7.2a to 7.2c are not characteristic of motions dominated by a single travelling wave train. Their shapes and low values of correlation suggest the simultaneous presence of multiple waves travelling in different directions with different velocities. The wide scatter of maximum absolute values in Fig. 7.4 also supports this general conclusion. As a consequence resolution of the motions into their frequency components and into their components of principal directions is required before identification of wave types, directions, and velocities is possible.

Following along these lines, let us transform the $x$ and $y$ recorded components of horizontal ground motion at a point into their $\tilde{x}$ and $\tilde{y}$ components in accordance with Fig. 7.1; thus,

$$
\begin{align*}
& \tilde{x}(t)=x(t) \cos \phi+y(t) \sin \phi \\
& \tilde{y}(t)=-x(t) \sin \phi+y(t) \cos \phi . \tag{3}
\end{align*}
$$

Next, using time and frequency domain windows, the Fourier transforms of these new components are calculated using relations of the type

$$
\begin{align*}
& A_{\tilde{x}}(f) \equiv \int_{t_{0}-\Delta T / 2}^{t_{0}+\Delta T / 2} \quad \tilde{x}(t) \exp (-i 2 \pi f t) d t  \tag{4}\\
& -\mathrm{f}_{0}+\Delta \mathrm{f} / 2 \\
& \tilde{x}(t) \equiv \int_{-f_{0}-\Delta f / 2} A_{\tilde{x}}(f) \exp (i 2 \pi f t) d f  \tag{5}\\
& f_{0}+\Delta f / 2 \\
& +\int_{f_{0}-\Delta f / 2}^{A_{\tilde{x}}(f)} \exp (i 2 \pi f t) d f
\end{align*}
$$

where window lengths $\Delta T$ and $\Delta E$ are centered on time $t_{0}$ and frequency $f_{0}$, respectively. A coherence function for components $\tilde{x}_{i}$ and $\tilde{x}_{j}$ ( $i$ and $j$ refer to station numbers) can now be defined by

$$
\begin{equation*}
\gamma_{\tilde{x}_{i} \tilde{x}_{j}}(f) \equiv \frac{\left|S_{\tilde{x}_{i}} \tilde{x}_{j}^{(f)}\right| 2}{S_{\tilde{x}_{i} \tilde{x}_{i}}(f) S_{\tilde{x}_{j}} \tilde{x}_{j}(f)} \tag{6}
\end{equation*}
$$

where

$$
\begin{align*}
& S_{\tilde{x}_{i} \tilde{x}_{j}(f) \equiv} \int_{-\infty}^{\infty} R_{\tilde{x}_{i}} \tilde{x}_{j}(\tau) \exp (-i 2 \pi f \tau) d \tau  \tag{7}\\
& R_{\tilde{x}_{i} \tilde{x}_{j}}(\tau) \equiv \int_{0}+\Delta T / 2  \tag{8}\\
& t_{0}-\Delta T / 2
\end{align*}
$$

and where $S_{\tilde{x}_{i}} \tilde{x}_{i}(f)$ and $R_{\tilde{x}_{j}} \tilde{x}_{j}(f)$ are similarly defined. Note that the coherence function (6), which ranges from 0 to 1 , provides a measure of the statistical dependence of motion $\tilde{x}_{j}$ on motion $\tilde{x}_{i}$.

Coherence functions as defined by (6) are plotted in Figs. 7.5a and 7.5b for components of motion produced by the earthquake of January 29, 1981, in the $\tilde{y}$ and $\tilde{x}$ directions, respectively. In what follows the value $\phi=64^{\circ}$ is adopted so that the $\tilde{\mathbf{x}}$ direction corresponds with the direction to the epicenter from station $\mathbf{C 0 0}$. The station pairs represented in these figures are located along the radial line of SMART 1 running from station 006 to 012 which is oriented in approximately the epicentral direction. The distance coordinate shown in these plots represents true distance between stations $i$ and $j$. Note that while the average coherence with distance is relatively low for most frequencies over the range $0<f<10 \mathrm{~Hz}$, it is relatively high in the neighborhood of frequencies 3.0 and 4.5 Hz , in Fig. 7.5 a and at frequencies about 1.1 and 3.5 Hz in Fig. 7.5 b , as indicated by $f_{1}$ and $f_{2}$, respectively. This observation is encouraging as the corresponding Fourier amplitude spectra for motions $\tilde{x}_{i}$ and $\tilde{x}_{j}$ for all station pairs have large peaks in the vicinity of the same frequencies. Thus, the high intensity ground motions which are caused primarily by frequencies in the neighborhood of $f_{1}$ and $f_{2}$ appear to be caused largely by single wave trains moving
across the array. In other frequency ranges, the motions appear to be caused to a much greater degree by multiple waves moving with different apparent velocities.

Let us now examine the influence of direction $\phi$ on the cross spectral density function defined by (7) for components $\tilde{x}(t)$ and $\tilde{y}(t)$ as given by (3) using measured components $x(t)$ and $y(t)$ for station pairs which are separated by only 0.2 km . This shortest distance between station pairs is selected so that coherences $\gamma_{\tilde{x}_{i}} \tilde{x}_{j}$ and $\gamma_{\tilde{Y}_{i}} \tilde{Y}_{j}$ are as large as possible; thus, the variations in $S_{\tilde{x}_{i}} \tilde{x}_{j}$ with respect to direction $\phi$ and frequency $f$ show variations in the intensities of motions $\tilde{x}_{i}$ and $\tilde{x}_{j}$. Figures $7.6 a$ and $7.6 b$ show plots of $S_{\tilde{x}_{i}} \tilde{x}_{j}$ as a function of frequency $f$ for discrete values of direction $\phi$ over the entire range $-90^{\circ}<\phi<+90^{\circ}$. Figure 7.6 a represents the earthquake of January 29, 1981, using station pair $\mathrm{COO-Il2}$ while Fig. 7.6 b represents the earthquake of November 14, 1980, using station pair I06-C00. From these figures, it is clear that the high intensity motions tend to be concentrated in the neighborhood of frequencies $f_{1}, f_{2}$, and $f_{3}$. For these discrete frequencies, the values of $\phi$ yielding the greatest values of cross spectral density can be observed. It should be pointed out that functions $S_{\tilde{x}_{i}} \widetilde{x}_{j}$. need not be generated through the use of (3), (4), (5), (7), and (8) for each value of $\phi$ since they are more easily obtained from the transformation

$$
\begin{align*}
S_{\tilde{x}_{i} \tilde{x}_{j}}(f, \phi) & =S_{x_{i} x_{j}} \text { (f) } \cos ^{2} \phi+S_{y_{i} y_{j}} \text { (f) } \sin ^{2} \phi  \tag{9}\\
& +S_{x_{i} y_{j}}(f) \cos \phi \sin \phi+S_{y_{i} x_{j}} \text { (f) } \cos \phi \sin \phi
\end{align*}
$$

The cross spectral density function (9) can easily be maximized with respect to $\phi$ for discrete values of frequency $f$, to give the direction of maximum intensity. The directions of maximum intensity shown in Fig. 7.7 were obtained by first maximizing the spectral densities for $f=2.9 \mathrm{~Hz}$ and then averaging the corresponding two values of $\phi$ for each set of adjacent station pairs along the
array line 006 to 012 during the earthquake of January 29, 1981. There is a definite shift in the direction of maximum intensity at this frequency as one moves across the array from station 006 to station 012.

The direction of maximum intensity as a function of frequency $f_{0}$ can also be obtained by maximizing the variance function ${ }^{3,4,5}$ (see (8))

$$
\begin{equation*}
R_{\tilde{x}_{i} \tilde{x}_{i}}(\tau=0, \phi)=R_{x_{i} x_{i}}(0) \cos ^{2} \phi+R_{y_{i} y_{i}}(0) \sin ^{2} \phi+2 R_{x_{i} y_{i}}(0) \cos \phi \sin \phi \tag{10}
\end{equation*}
$$

with respect to $\phi$; thus, giving

$$
\begin{equation*}
\phi_{0}\left(f_{0}\right)=\frac{1}{2} \tan ^{-1} \frac{2 R_{x_{i} y_{i}}^{(0)}}{R_{x_{i} x_{i}}(0)-R_{y_{i} y_{i}}(0)} \tag{11}
\end{equation*}
$$

Angle $\phi_{0}$ in (11) denotes the two principal directions which are $90^{\circ}$ apart; one being the major principal direction, the other the minor principal direction. The corresponding principal variances will be denoted by $R_{\tilde{x}_{i}} \tilde{x}_{i}\left(f_{0}, \phi_{0}\right)$ and ${ }^{R} \tilde{Y}_{i} \tilde{y}_{i}\left(f_{0}, \phi_{0}\right)$. The angles of maximum intensity obtained by this procedure are quite close to those obtained by the previously described procedure of maximizing the cross spectral density function for station pairs with respect to direction $\phi$

### 7.2 The Principal Variance Ratio

Let us now define a principal variance ratio as given by

$$
\begin{equation*}
R\left(f_{0}, \phi_{0}\right) \equiv \frac{R_{\tilde{Y}_{i}} \tilde{y}_{i}\left(f_{0}, \phi_{0}\right)}{R_{\tilde{x}_{i}} \tilde{x}_{i}\left(f_{0}, \phi_{0}\right)} \tag{12}
\end{equation*}
$$

which varies over the range $0<R<1$. If we examine, the motion at station $i$ for
discrete values of $f_{0}$, consistent with the discrete frequencies of the Fast Fourier Transform method used in evaluating (4) and (5), we find the following results. First, when $R\left(f_{0}, \phi_{0}\right)=1$ there are no principal directions because the harmonic motion at frequency $f_{0}$ moves along a circular path at constant angular velocity, $2 \pi f_{0}$, as shown in Fig. 7.8; i.e., the motion is equivalent to two resultant harmonics in orthogonal directions having equal amplitudes but being $90^{\circ}$ out-of-phase. When $R\left(f_{0}, \phi_{0}\right)<1$, principal directions do exist with the motion being along a straight line for $R\left(f_{0}, \phi_{0}\right)=0$ and along an ellipse for $0<R\left(f_{0}, \phi_{0}\right)<l$. In the latter case, the resultant harmonics in the principal directions have different amplitudes as shown in Fig. 7.8 and they are $90^{\circ}$ out-of-phase. Secondly, it is significant to note that only for $R\left(f_{0}, \phi_{0}\right)=0$ can a pure single harmonic wave exist. For $R\left(f_{0}, \phi_{0}\right)>0$ multiple waves moving in different directions are present. Thus, in the interest of identifying wave types, directions, and velocities, attention should be concentrated on those discrete frequencies having low values of $R\left(f_{0}, \phi_{0}\right)$. Fortunately, in the SMART 1 data analysed here as will be shown subsequently, those frequencies usually represent waves of high energy transmission.

Figures 7.9 a and 7.9 b show plots of the major principal variance, the principal variance ratio, and dominant (or major principal) direction for the ground motions recorded at stations COO, IO3, and IO6 during the earthquakes of January 29, 1981, and November 14, 1980, respectively. It is significant to note in Fig. 7.9a that at frequencies, $f_{1}, f_{2}, f_{3}$, and $f_{4}$, representing high intensity motions, the corresponding variance ratios are low indicating relatively pure single wave transmissions at these frequencies. Note that the dominant directions are nearly toward the epicenter for frequencies $f_{1}$ and $f_{2}$ but are much closer to the normal direction for frequencies $f_{3}$ and $f_{4}$. This observation suggests that Rayleigh waves are the primary source of energy
transmission for frequencies less than about 2.5 Hz and that shear waves (SH waves, perhaps in part Love waves) are the primary source of energy transmission for frequencies from 2.5 Hz to about 6 Hz . Above these frequencies, the directions of propagation are quite variable. In Fig. 7.9b, the variance ratio has fairly low values at frequencies $f_{1}$ and $f_{2}$ which also correspond to frequencies of relatively high intensity. However the variance ratio is quite high for most frequencies suggesting a mix of waves. Again it is significant to note the change in dominant direction from the epicentral direction(in the range $1.4<f_{0}<2.0 \mathrm{~Hz}$ to the normal direction (at higher frequencies up to 8 Hz ). As mentioned earlier, this change suggests a shift with increasing frequency from dominant Rayleigh wave transmission to SH or Love wave transmission.

Let us now examine in further detail, the ground motion characteristics at frequencies $f_{1}=1.17 \mathrm{~Hz}$ and $f_{3}=2.85 \mathrm{~Hz}$, as indicated in Fig. 7.9a, for many stations in addition to stations $\mathbf{C O O}, \mathrm{IO3}$, and I06. As suggested above, the dominant ground motions at these frequencies seem to be caused primarily by Rayleigh and shear (SH) waves, respectively. Figures 7.10a and 7.10b show the dominant directions at frequencies 1.17 Hz and 2.85 Hz , respectively, at many stations for the earthquake of January 29, 1981, evaluated using (11). The average dominant direction $\phi_{0}$ over the array is also shown in these figures as computed from frequency-wave number spectral analysis ${ }^{6}$. Note that the average dominant direction in Fig. 7.10a is reasonably close to the epicentral direction while the average dominant direction in Fig. 7.10 b is close to the normal direction.

We may now use these two average dominant directions to generate corresponding cross correlation functions defined by (8) for ground motions recorded at station pairs across the array during the earthquake of January 29, 1981. We plot in Fig. 7.11 for each station pair the delay time $\tau$, for maximum cross correlation, against the corresponding relative distance between stations as
projected on the average dominant axis. Straight lines fitted by least squares yield wave velocities (inverse values of the line slopes) equal to $2.4 \mathrm{~km} / \mathrm{sec}$ and $5.3 \mathrm{~km} / \mathrm{sec}$ for frequencies 1.17 and 2.85 Hz , respectively. The Rayleigh wave identified above at fxequency 1.17 Hz moving in the direction $\phi=68^{\circ}$ at velocity $2.4 \mathrm{~km} / \mathrm{sec}$ is with little doubt the same wave type characterized in Chapter 5 by the wave number spectrum analysis which showed waves at frequencies 1 to 2 Hz moving in the direction $\phi=68^{\circ}$ at velocity $3.0 \mathrm{~km} / \mathrm{sec}$.

Because a uniform elastic half space transmits Rayleigh waves at a velocity equal to 0.9 times the shear wave velocity, an explanation is needed of the mixture in the same time window of SH waves with local velocity of $5.3 \mathrm{~km} / \mathrm{sec}$ and Rayleigh waves with velocities of $2.4 \mathrm{~km} / \mathrm{sec}$. The usual seismological interpretation of this large difference in local apparent velocities is that the $S H$ waves are associated with longer travel paths from the earthquake source to the array in the vicinity of which the SH wave fronts move steeply upwards through the soil. Thus the apparent shear wave velocity is largely controlled by the more rigid, deeper rocks in the crust. On the other hand, the Rayleigh waves develop near the surface between the source and the array so that their wave velocities are largely controlled by the shallower materials.

According to this explanation the vertical component ground motions in the time windows studied should be significant in the frequency range of the Rayleigh waves but relatively insignificant in the frequency range of the shear (transverse) waves described above. This prediction was tested by computing particle motions from the accelerograms as a function of frequency. Results are shown in Fig. 7.12. The particle orbits agree well with the above prediction with significant vertical displacement in the frequency bands 0.25 to 1.5 Hz and 0.75 to 1.5 Hz , but almost none transverse to the wave direction in the 2.5 to 3.1 Hz frequency band.

### 7.3 References

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Fig. 7.1 Coordinate transformation of two horizontal components.


Fig. 7.2a Correlation coefficient for different station pairs: Event 5; EW direction; time window 47:00-54:00


Fig. 7.2a continued


Fig. 7.2a continued

|  |
| :---: |

Fig. 7.2b Correlation coefficient for different station pairs: Event 2; EW direction; time window 22:30-29:30


Fig. 7.2c Correlation coefficient for different station pairs: Event 2; NS direction; time window 22:30-29:30

Fig. 7.3 Time window used in the analysis: Event 5


Fig. 7.4 Attenuation of correlation coefficient $\rho$






Fig. 7.7 Direction of wave propagation


Fig. 7.8 Physical meaning of principal variance ratio


Fig. 7.9a Major principal variance, variance ratio and dominant direction for Event 5


Flg. 7.9b Major principal variance, variance ratio and dominant direction for Event 2


Fig. 7.10a Dominant directions at 1.17 Hz for Event 5


Fig. 7.10b Dominant directions at 2.85 Hz for Event 5


Fig. 7.11 Identification of wave velocity at frequencies 1.17 Hz and 2.85 Hz

Fig. 7.12 Particle ground motions drawn in two vertical planes for Event 5 and time window 47:00-53:00
8. ENGINEERING ANALYSIS OF SMART 1 ARRAY ACCELEROGRAMS

### 8.1 Introduction

The engineering studies of the ground motion data from the SMART I array concentrate on the influence of spatial variations of ground motions on the dynamic response of large structural systems such as industrial buildings, bridges, and dams. The results presented in this chapter focus on the correlations of multi-support excitations and their influence on the dynamic response of linear structural systems for selected accelerograms recorded during the earthquakes of November 14, 1980 (Event 2) and January 29, 1981 (Event 5).

### 8.2 Response of Linear Systems to Multi-Support Excitations

A. General System

The equations of motion for a discrete parameter, linear structural system subjected to multi-support excitations can be written in the form

$$
\begin{equation*}
\underline{m} \ddot{\ddot{r}}^{t}+\underline{c} \underline{\dot{r}}^{t}+\underline{k}^{t} \underline{r}^{t}=\underline{p}(t) \tag{1}
\end{equation*}
$$

where $\underline{r}^{t}$ is the total displacement vector from a fixed reference containing $n$ components, i.e., $n=n_{s}+n_{b}$ where $n_{s}$ is the number of degrees of freedom in the system exclusive of support displacements and $n_{b}$ is the number of degrees of freedom associated with the support displacements, $p(t)$ is the load vector containing non-zero components only for the support interaction forces, and $\underline{m}, \underline{c}$, and $k$ are the $n \times n$ mass, damping, and stiffness matrices, respectively. This equation can be partitioned and written in the form
where $\underline{r}_{s}^{t}$ and $\underline{r}_{b}^{t}$ represent the $n_{s}$ and $n_{b}$ degrees of freedom, respectively.
The total response can be separated into quasi-static and dynamic response of the form

$$
\underline{\underline{r}}^{\mathrm{t}}=\left\{\begin{array}{l}
\underline{\mathrm{r}}_{\mathrm{s}}^{\mathrm{qs}}  \tag{3}\\
\underline{\underline{r}}_{\mathrm{b}}^{\mathrm{qs}}
\end{array}\right\}+\left\{\begin{array}{l}
\underline{\mathrm{r}}_{\mathrm{s}}^{\mathrm{d}} \\
\underline{o}
\end{array}\right\}
$$

where components in vector $\underline{\underline{r}}_{\mathrm{b}}^{\mathrm{qs}}$ are identical to the corresponding prescribed support displacements in vector $\underline{r}_{b}^{t}$, components in $\underline{r}_{s}^{q S}$ are the quasi-static displacements in the $n_{s}$ degrees of freedom caused by the support displacements in $\underline{r}_{b}^{t}$, and components in $\underline{r}_{s}^{d}$ are dynamic displacements in the $n_{s}$ degrees of freedom.

The quasi-static response is obtained from the first equation of (2) upon letting $\underline{\underline{r}}^{t}$ and $\underline{\dot{r}}^{t}$ equal zero vectors; thus

$$
\begin{equation*}
\underline{\underline{r}}_{s}^{\mathrm{qs}}=-\underline{\mathrm{k}}_{\mathrm{ss}}^{-1} \underline{\mathrm{k}}_{\mathrm{sb}} \underline{\underline{r}}_{\mathrm{b}}^{\mathrm{t}} \tag{4}
\end{equation*}
$$

The dynamic response is obtained from the first equation of (2) upon substitution of (3) and (4); thus

$$
\begin{equation*}
\underline{m}_{s s} \ddot{\ddot{r}}_{s}^{\mathrm{d}}+\underline{c}_{s s} \ddot{\dot{r}}_{s}^{\mathrm{d}}+\underline{k}_{s s} \underline{r}_{s}^{\mathrm{d}}=\left[\underline{m}_{s s} \underline{k}_{s s}^{-1} \underline{k}_{s b}-\underline{m}_{s b}\right] \ddot{\mathrm{r}}_{b}^{\mathrm{t}}+\left[\underline{c}_{s s} \underline{k}_{s s}^{-1} \underline{k}_{s b}-\underline{c}_{s b}\right] \dot{r}_{b}^{\mathrm{t}} \tag{5}
\end{equation*}
$$

The second term on the right hand side of (5) equals zero for stiffness proportional damping and is small for other forms of damping when the damping ratios are low, say less than 10 percent of critical; therefore, it can be dropped from the equation without introducing significant error. The dynamic response can then be obtained from the approximate relation

$$
\begin{equation*}
\underline{m}_{s s} \ddot{\ddot{r}}_{s}^{d}+\underline{c}_{s s} \dot{r}_{s}^{d}+\underline{k}_{s s} \underline{r}_{s}^{d} \simeq\left[\underline{m}_{s s} \underline{k}_{s s}^{-1} \underline{k}_{s b}-\underline{m}_{s b}\right] \ddot{\ddot{r}}_{b}^{t} \tag{6}
\end{equation*}
$$

Solving for fixed base structural mode shapes and frequencies using

$$
\begin{equation*}
\underline{m}_{S S} \ddot{\underline{r}}_{s}^{d}+\underline{k}_{S S} \underline{r}_{s}^{d}=\underline{o} \tag{7}
\end{equation*}
$$

the vector $\underline{r}_{S}^{d}$ can be expressed in terms of the resulting $n_{s} \times n_{S}$ modal matrix $\Phi_{S}$ and the $n_{S}$ fixed base modal coordinates $Y_{S}$ as given by

$$
\begin{equation*}
\underline{r}_{\mathrm{S}}^{\mathrm{d}}=\Phi_{\mathrm{S}} \underline{Y}_{\mathrm{S}} \tag{8}
\end{equation*}
$$

Introducing (8) into (6) and using the orthogonality properties of the fixed base modes, uncoupled normal mode equations of motion for the fixed base structure are obtained as given by

$$
\begin{equation*}
\underline{M}_{S} \ddot{Y}_{s}+\underline{C}_{s} \dot{Y}_{s}+\underline{K}_{s} \underline{Y}_{S}=\underline{\Phi}_{s}^{T}\left[\ddot{m}_{S S} \underline{k}_{s s}^{-1} \underline{k}_{s b}-\underline{m}_{s b}\right] \ddot{\ddot{r}}_{b}^{t} \tag{9}
\end{equation*}
$$

where $\underline{M}_{S}, \underline{C}_{S}$, and ${\underset{-}{K}}_{S}$ are $n_{S} x n_{S}$ diagonal matrices defined by
and

$$
\begin{align*}
& \underline{M}_{S} \equiv \underline{\Phi}_{S}^{T} \underline{m}_{S S} \underline{S}_{S} \\
& \underline{C}_{S} \equiv \underline{\Phi}_{S}^{T} \underline{c}_{S S} \Phi_{S}=2 \underline{M}_{S} \underline{\omega}_{S} \xi_{S}  \tag{10}\\
& \underline{K}_{S} \equiv \underline{\Phi}_{S}^{T} \underline{k}_{S S} \underline{\xi}_{S}=\underline{\omega}_{S}^{2} \underline{M}_{S}
\end{align*}
$$

where ${\underset{S}{W}}$ is a diagonal matrix containing the fixed base normal mode frequencies, and $\underline{\xi}_{s}$ is a vector containing the $n_{s}$ normal mode damping ratios. It is assumed here that the damping matrix $c_{S S}$ is of the Caughey form so that uncoupled damped normal modes exist.

It should be recognized that generalized shape functions and corresponding amplitudes could also be used in formulating the original discrete parameter equations of motion. Normally, however, the standard finite element approach would be used.
B. Special Case of the General System

Consider a special case of the general system formulated above where $n_{s}=1, n_{b}=2$, and $n=3$. Let the two prescribed single-component support displacements at supports $A$ and $B$ in this case be denoted by $v_{g A}(t)$ and $v_{g B}(t)$, respectively. Equation (3) can now be written as

$$
\underline{r}^{t}=\left\{\begin{array}{c}
r_{1}^{t}(t)  \tag{11}\\
v_{g A}(t) \\
v_{g B}(t)
\end{array}\right\}=\left\{\begin{array}{c}
r_{1}^{q s}(t) \\
v_{g A}(t) \\
v_{g B}(t)
\end{array}\right\}+\left\{\begin{array}{c}
x_{1}^{d}(t) \\
o \\
0
\end{array}\right\}
$$

Note that the single degree of freedom in the fixed base system as represented by $r_{1}^{d}(t)$ could be any single normal mode of the multi-degree fixed base system or any other single generalized shape function for that system.

The quasi-static solution as given by (4) becomes

$$
\begin{equation*}
\mathrm{r}_{1}^{\mathrm{qs}}=-\frac{\mathrm{k}_{12}}{\mathrm{k}_{11}} \mathrm{v}_{\mathrm{gA}}-\frac{\mathrm{k}_{13}}{\mathrm{k}_{11}} \mathrm{v}_{\mathrm{gB}}, \tag{12}
\end{equation*}
$$

and (5), yielding the dynamic response, reduces to

$$
\begin{equation*}
\ddot{r}_{1}^{\mathrm{d}}+2 \xi_{1} \omega_{1} \dot{\mathrm{r}}_{1}^{\mathrm{d}}+\omega_{1}^{2} \mathrm{r}_{1}^{\mathrm{d}}=\left(\frac{\mathrm{k}_{12}}{\mathrm{k}_{11}}-\frac{\mathrm{m}_{12}}{\mathrm{~m}_{11}}\right) \ddot{\mathrm{v}}_{\mathrm{gA}}+\left(\frac{\mathrm{k}_{13}}{\mathrm{k}_{11}}-\frac{\mathrm{m}_{13}}{\mathrm{~m}_{11}}\right) \ddot{\mathrm{v}}_{\mathrm{gB}} \tag{13}
\end{equation*}
$$

where

$$
\begin{align*}
& \omega_{1}=\sqrt{k_{11} / m_{11}}  \tag{14}\\
& \xi_{1}=c_{11} / 2 \mathrm{~m}_{11} \omega_{1}
\end{align*}
$$

For the subsequent development, it is convenient to write (13) in the form

$$
\begin{equation*}
\ddot{\mathrm{r}}_{1}^{\mathrm{d}}+2 \xi_{1} \omega_{1} \dot{\mathrm{r}}_{1}^{\mathrm{d}}+\omega_{1}^{2} \mathrm{r}_{1}^{\mathrm{d}}=-\mathrm{A} \ddot{\mathrm{v}}_{\mathrm{gA}}-\mathrm{B} \ddot{\mathrm{v}}_{\mathrm{gB}} \tag{15}
\end{equation*}
$$

where

$$
\begin{equation*}
A \equiv-\left(\frac{k_{12}}{k_{11}}-\frac{m_{12}}{m_{11}}\right) \quad ; \quad B \equiv-\left(\frac{k_{13}}{k_{11}}-\frac{m_{13}}{m_{11}}\right) \tag{16}
\end{equation*}
$$

Now compare the maximum absolute value of dynamic response with the two simultaneous inputs as expressed by (15) with the average of the maximum absolute values of response produced by the two inputs applied as rigid base inputs separately, i.e., the averages of the maximum absolute values of response derived from

$$
\begin{align*}
& \ddot{\mathrm{r}}_{1}^{\mathrm{d}}+2 \xi_{1} \omega_{1} \dot{\mathrm{r}}_{1}^{\mathrm{d}}+\omega_{1}^{2} r_{1}^{\mathrm{d}}=-(\mathrm{A}+\mathrm{B}){\ddot{\stackrel{\rightharpoonup}{v}_{g A}}}^{\ddot{r}_{1}^{\mathrm{d}}+2 \xi_{1} \omega_{1} \dot{\mathrm{r}}_{1}^{\mathrm{d}}+\omega_{1}^{2} r_{1}^{d}=-(A+B) \ddot{v}_{g B}} . \tag{1.7}
\end{align*}
$$

Letting $S_{a}^{A A}(\xi, \Upsilon)$ and $S_{a}^{B B}(\xi, T)$ represent the standard pseudo-acceleration response spectra for ground accelerations $\ddot{v}_{g A}$ and $\ddot{v}_{g B}$, respectively, the maximum absolute values for $r_{1}^{d}$ as given by (17) and (18) will be $\frac{1}{\omega_{1}^{2}}(A+B) S_{a}^{A A}(\xi, T)$ and $\frac{1}{\omega_{1}^{2}}(A+B) S_{a}^{B B}(\xi, T)$, respectively. The average of these two maximum responses will be $\frac{1}{2 \omega_{1}^{2}}(A+B)\left[S_{a}^{A A}(\xi, T)+S_{a}^{B B}(\xi, T)\right]$. The quantity $T$ introduced here is the fixed base structural period $2 \pi / \omega_{1}$.

Consider now the maximum absolute value of response resulting from (15). It is convenient to designate inputs $\ddot{v}_{g A}$ and $\ddot{v}_{g B}$ so that $|A| \leq|B|$ and to introduce a participation factor ratio $\gamma$ defined by

$$
\begin{equation*}
\gamma \equiv \frac{A}{B} \tag{19}
\end{equation*}
$$

Because $|A| \leq|B|, \gamma$ must always be in the range

$$
\begin{equation*}
-1 \leq \gamma \leq+1 \tag{20}
\end{equation*}
$$

Using this participation factor ratio, (15) can be written as

$$
\begin{equation*}
\ddot{r}_{1}^{\mathrm{d}}+2 \xi_{1} \omega_{1} \dot{\mathrm{r}}_{1}^{\mathrm{d}}+\omega_{1}^{2} \mathrm{r}_{1}^{\mathrm{d}}=-\mathrm{B}\left[\gamma \ddot{\mathrm{v}}_{\mathrm{gA}}+\ddot{\mathrm{v}}_{g B}\right] \tag{21}
\end{equation*}
$$

Defining $S_{a}^{A B}(\gamma, \xi, T)$ as the standard pseudo-acceleration response spectrum derived using $1 / 2\left[\ddot{\gamma}_{g A}+\ddot{v}_{g B}\right]$ as the single input to the single degree of freedom system, the maximum absolute value of response resulting from (21) is $\frac{2 B}{\omega_{1}^{2}} S_{a}^{A B}(\gamma, \xi, T)$.

A generalized dynamic response ratio $\Phi^{d}(\gamma, \xi, T)$ is now defined as the ratio of the maximum absolute value of response derived from (21) to the average of the maximum absolute values of response given by (17) and (18); thus

$$
\begin{equation*}
\Phi^{\mathrm{d}}(\gamma, \xi, \mathrm{~T}) \equiv \frac{4}{(\gamma+1)} \frac{\mathrm{S}_{\mathrm{a}}^{\mathrm{AB}}(\gamma, \xi, \mathrm{~T})}{\left[\mathrm{S}_{\mathrm{a}}^{\mathrm{AA}}(\xi, \mathrm{~T})+\mathrm{S}_{\mathrm{a}}^{\mathrm{BB}}(\xi, \mathrm{~T})\right]} \tag{22}
\end{equation*}
$$

Note that as $\ddot{\mathrm{v}}_{\mathrm{gA}}(\mathrm{t})$ and $\ddot{\mathrm{v}}_{\mathrm{gb}}(\mathrm{t})$ approach full positive correlation with each other, $\Phi^{\mathrm{d}}(1, \xi, \mathrm{~T}) \rightarrow 1$.

The generalized dynamic response ratio defined by (22) can be used effectively to measure the modified dynamic response resulting from the differences in the two simultaneous inputs $\ddot{v}_{g A}$ and $\ddot{v}_{g B}$. These differences obviously depend upon the distance between supports $A$ and $B$ as well as other factors.

Since $S_{a}^{A B}(1, \xi, T)$ and $S_{a}^{A B}(-1, \xi, T)$ are the pseudo-acceleration response spectra for single degree of freedom inputs $1 / 2\left[\ddot{v}_{g B}+\ddot{v}_{g A}\right]$ and $1 / 2\left[\ddot{v}_{g B}-\ddot{v}_{g A}\right]$, i.e., the in-phase and out-of-phase components, respectively, for motions at $A$ and $B$, the non-dimensional normalized form of (22) given by

$$
\begin{equation*}
\frac{(\gamma+1)}{2} \Phi^{\mathrm{d}}(\gamma, \xi, \mathrm{~T})=\frac{2 \mathrm{~S}_{\mathrm{a}}^{\mathrm{AB}}(\gamma, \xi, \mathrm{~T})}{\left[\mathrm{S}_{a}^{\mathrm{AA}}(\xi, \mathrm{~T})+\mathrm{S}_{a}^{\mathrm{BB}}(\xi, \mathrm{~T})\right]} \tag{23}
\end{equation*}
$$

can be used for $\gamma=+1$ and $\gamma=-1$ to measure the intensity of in-phase motions and out-of-phase motions, respectively.

Example No. 1 of the Special Case - Consider the simple system shown in Fig. 8.1 with support inputs at $A$ and $B$ as indicated. For this system,
(4) and (6) become

$$
\begin{equation*}
\mathrm{r}_{1}^{\mathrm{qS}}=\frac{1}{2}\left[\mathrm{v}_{\mathrm{gA}}+\mathrm{v}_{\mathrm{gB}}\right] \tag{24}
\end{equation*}
$$

and

$$
\begin{equation*}
\ddot{r}_{1}^{\mathrm{d}}+2 \xi_{1} \omega_{1} \dot{\mathrm{r}}_{1}^{\mathrm{d}}+\omega_{1}^{2} r_{1}^{\mathrm{d}}=-\frac{1}{2}\left[\ddot{v}_{\mathrm{gA}}+\ddot{\mathrm{v}}_{\mathrm{gB}}\right] \tag{25}
\end{equation*}
$$

where $\omega_{1}=\sqrt{k / m}$, and $\xi_{1}$ is the fixed base damping ratio. Constants $A$ and $B$ as defined by (16) are both equal to $1 / 2$; thus $\gamma=+1$. The dynamic response ratio reduces to the form

$$
\begin{equation*}
\Phi^{\mathrm{d}}(1, \xi, \mathrm{~T})=\frac{2 \mathrm{~S}_{a}^{\mathrm{AB}}(\gamma, \xi, \mathrm{~T})}{\left[\mathrm{S}_{\mathrm{a}}^{\mathrm{AA}}(\xi, \mathrm{~T})+\mathrm{S}_{a}^{\mathrm{BB}}(\xi, \mathrm{~T})\right]} \tag{26}
\end{equation*}
$$

and the shear forces are given by

$$
\begin{equation*}
V_{A}(t)=\frac{k}{2}\left[r_{1}^{d}+\left(\frac{v_{g B}-v_{g A}}{2}\right)\right] ; \quad V_{B}(t)=\frac{k}{2}\left[r_{1}^{d}-\left(\frac{{ }_{\mathrm{gB}}{ }^{-v} g \mathrm{gA}}{2}\right)\right] . \tag{27}
\end{equation*}
$$

Let us now define two new acceleration spectra $S_{A}(\xi, T)$ and $S_{B}(\xi, T)$ by the relations

$$
\begin{align*}
& \mathrm{S}_{A}(\xi, \mathrm{~T}) \equiv \omega_{1}^{2}\left|\mathrm{r}_{1}^{\mathrm{d}}+\left(\frac{\mathrm{v}_{\mathrm{gB}}{ }^{-\mathrm{v}} \mathrm{gA}}{2}\right)\right|_{\max } ; \\
& \mathrm{S}_{\mathrm{B}}(\xi, \mathrm{~T}) \equiv \omega_{1}^{2}\left|\mathrm{r}_{1}^{\mathrm{d}}-\left(\frac{\mathrm{v}_{\mathrm{gB}}{ }^{-\mathrm{v}_{\mathrm{gA}}}}{2}\right)\right|_{\max } . \tag{28}
\end{align*}
$$

Note that when $\ddot{v}_{B}=\ddot{v}_{A}$,

$$
\mathrm{S}_{\mathrm{B}}(\xi, \mathrm{~T})=\mathrm{S}_{\mathrm{A}}(\xi, \mathrm{~T})=\mathrm{S}_{\mathrm{a}}^{\mathrm{AA}}(\xi, \mathrm{~T})
$$

and when $\ddot{\mathrm{v}}_{\mathrm{A}}=\ddot{\mathrm{v}}_{\mathrm{B}}$,

$$
S_{B}(\xi, T)=S_{A}(\xi, T)=S_{a}^{B B}(\xi, T) .
$$

If a new generalized dynamic response ratio $\Phi^{t}(\xi, T)$ is defined as the ratio of the average of the maximum absolute values of $V_{A}(t)$ and $V_{B}(t)$ produced by the multiple inputs as represented by (24) and (25) to the average of maximum absolute shears as produced by separate rigid base (single input) inputs $\ddot{\mathrm{v}}_{\mathrm{gA}}$ and $\ddot{\mathrm{v}}_{\mathrm{gB}}$, then

$$
\begin{equation*}
\Phi^{t}(\xi, T)=\frac{S_{A}(\xi, T)+S_{B}(\xi, T)}{S_{a}^{A A}(\xi, T)+S_{a}^{B B}(\xi, T)} \tag{29}
\end{equation*}
$$

Note that for systems of the above type which are statically indeterminant through their supports, the forces produced by the quasi-static responses are proportional to the out-of-phase ground displacement $\left(v_{g B}-v_{g A}\right) / 2$.

Example No. 2 of the Special Case - Consider the simple system shown in Fig. 8.2 with support inputs at $A$ and $B$ as indicated. It is of interest to consider the absolute maximum response of a single mode of vibration for simultaneous inputs $\ddot{v}_{A}(t)$ and $\ddot{v}_{B}(t)$ and to compare this maximum response with the average of the corresponding absolute maximum responses produced by rigid base inputs $\ddot{v}_{A}(t)$ and $\ddot{v}_{B}(t)$.

Considering the first mode, its dynamic response is given by

$$
\begin{equation*}
v^{d}(x, t)=r_{1}^{d}(t) \sin \frac{\pi x}{2}, \tag{30}
\end{equation*}
$$

and its quasi-static response is given by

$$
\begin{equation*}
\mathrm{v}^{\mathrm{qs}}(\mathrm{x}, \mathrm{t})=\mathrm{v}_{\mathrm{gA}}(\mathrm{t})+\left(\frac{\mathrm{v}_{\mathrm{gB}}(\mathrm{t})-\mathrm{v}_{\mathrm{gA}}(\mathrm{t})}{\mathrm{L}}\right) \mathrm{x} \tag{31}
\end{equation*}
$$

Adding (30) and (31), the total response is given by

$$
\begin{equation*}
v^{t}(x, t)=r_{1}^{d}(t) \Phi_{1}(x)+v_{g A} \Phi_{2}(x)+v_{g B} \Phi_{3}(x) \tag{32}
\end{equation*}
$$

where

$$
\begin{align*}
& \Phi_{1}(x)=\sin \frac{\pi x}{L} \\
& \Phi_{2}(x)=1-\frac{x}{L}  \tag{33}\\
& \Phi_{3}(x)=\frac{x}{L} .
\end{align*}
$$

The principle of virtual work and standard finite element methods give

$$
\begin{align*}
& \mathrm{m}_{11}=\frac{\overline{\mathrm{mL}}}{2} ; \quad \mathrm{m}_{12}=\mathrm{m}_{13}=\frac{\overline{\mathrm{mL}}}{2} \\
& \mathrm{k}_{11}=\frac{\pi^{4} \overline{\mathrm{EI}}}{2 \mathrm{~L}^{3}} ; \quad \mathrm{k}_{12}=\mathrm{k}_{13}=0 \tag{34}
\end{align*}
$$

from which

$$
\begin{equation*}
\omega_{1}^{2}=\mathrm{k}_{11} / \mathrm{m}_{11}=\frac{\pi^{4} \overline{\mathrm{EI}}}{\overline{\mathrm{~mL}}} ; \quad \mathrm{T}_{1}=2 \pi / \omega_{1} \tag{35}
\end{equation*}
$$

Substituting (34) into (16) gives $A=B=2 / \pi$; therefore, $\gamma$ as defined by (19) equals 1. Because this structure is statically determinant through its supports, the quasi-static response produces no internal forces in the system. This is consistent with (4) with $r_{1}^{q S}=0$. It is quite clear now that the generalized dynamic response ratio given by (26) for $\xi^{=} \xi_{1}$ and $T=T_{1}$ is a direct measure of the modified total force (or stress) response caused by the differences in the two inputs $\ddot{v}_{A}(t)$ and $\ddot{v}_{B}(t)$.

For the second mode response, (32) and (33) still apply except that

$$
\begin{equation*}
\Phi_{I}(x)=\sin \frac{2 \pi x}{L} \tag{36}
\end{equation*}
$$

This mode shape leads to

$$
\begin{align*}
& \mathrm{m}_{11}=\frac{\overline{\mathrm{m} L}}{2} ; \quad \mathrm{m}_{12}=\frac{\overline{\mathrm{m}} \mathrm{~L}}{2 \pi} ; \quad \mathrm{m}_{13}=-\frac{\overline{\mathrm{m}} \mathrm{~L}}{2 \pi} \\
& \mathrm{k}_{11}=\frac{8 \pi^{4} \overline{\mathrm{EI}}}{\mathrm{~L}^{3}} ; \quad \mathrm{k}_{12}=\mathrm{k}_{13}=0 . \tag{37}
\end{align*}
$$

Thus,

$$
\begin{equation*}
\omega_{1}^{2}=\frac{\mathrm{k}_{11}}{\mathrm{~m}_{11}}=\frac{16 \pi^{4} \overline{\mathrm{EI}}}{\overline{\mathrm{~mL}}{ }^{4}} \text { (second mode freq.) } \tag{38}
\end{equation*}
$$

Substituting (37) into (16) gives $A=1 / \pi$ and $B=-1 / \pi$; therefore, $\gamma$ as defined by (19) equals -1 . From (26), it is seen that $\Phi^{d}(-1, \xi, T)$ becomes infinite. The reason for this is that the second mode is excited only by the
out-of-phase motion ( $\ddot{v}_{g B}-\ddot{v}_{g A}$ )/2. In other words, the rigid base (in--phase) inputs produce no second mode response.

### 8.3 Correlations of Multi-Support Excitations

A. Multiple Components at One Support

Consider input accelerations $a_{r x}(t), a_{r y}(t)$, and $a_{r z}(t)$ at support $r$ in directions $x, y$, and $z$, respectively. These motions can easily be transformed to any other orthogonal set of axes, say $\bar{x}, \bar{y}$, and $\bar{z}$, through a transformation matrix $\underline{a}$ which satisfies the condition $\underline{a}^{T} \underline{a}=\underline{I}$, where $I$ is the identity matrix. Then

$$
\left\{\begin{array}{l}
a_{r \bar{x}}(t)  \tag{39}\\
a_{r \bar{y}}(t) \\
a_{r \bar{z}}(t)
\end{array}\right\}=\left[\begin{array}{lll}
a_{11} & a_{12} & a_{13} \\
a_{21} & a_{22} & a_{23} \\
a_{31} & a_{32} & a_{33}
\end{array}\right]\left\{\begin{array}{l}
a_{r x}(t) \\
a_{r y}(t) \\
a_{r z}(t)
\end{array}\right\}
$$

The transformation giving the principal axes, i.e., the directions for which no cross-correlations exist among the three transformed components of acceleration ${ }^{1}$ can easily be found. For small structures, the directions of the principal axes for all inputs would be approximately the same; however, for large structures significant differences could exist, particularly when the site conditions are complex.
B. Uni-Directional Components at Two Supports

Let $a_{r i}(t)$ and $a_{s i}(t)$ be the recorded ground accelerations at stations $r$ and $s$, respectively, in the $i$ th coordinate direction ( $i=x, y, z$ ) at time t. These motions can be separated into their in-phase and out-of-phase components as shown by

$$
\begin{align*}
& a_{r i}(t)=\left[\frac{a_{r i}(t)+a_{s i}(t)}{2}\right]+\left[\frac{a_{r i}(t)-a_{s i}(t)}{2}\right]  \tag{40}\\
& a_{s i}(t)=\left[\frac{a_{r i}(t)+a_{s i}(t)}{2}\right]-\left[\frac{a_{r i}(t)-a_{s i}(t)}{2}\right]
\end{align*}
$$

The first term on the right-hand side of (40) represents the in-phase component while the second term represents the out-of-phase component. It is very informative to compare these two components directly for different pairs of stations and for different directions when studying the correlations of $a_{r i}(t)$ and $a_{s i}(t)$. As pointed out previously, (23) can also be used for this same purpose by letting $\gamma=+1$ and $\gamma=-1$ and comparing the two results obtained.

Correlation studies of $a_{r i}(t)$ and $a_{s i}(t)$ can also be carried out using the so called "moving window" technique. To develop this method, the Fast Fourier Transform algorithm can be used to generate

$$
\begin{align*}
& a_{r i}(\bar{i} \bar{\omega}, t) \equiv \int_{t-\frac{\Delta t}{2}}^{t+\frac{\Delta t}{2}} a_{r i}(\alpha) e^{-i \bar{\omega} \alpha} d \alpha  \tag{41}\\
& b_{r i}(\bar{\omega}, t, \alpha) \equiv \frac{1}{2 \pi} \int_{-\frac{\Delta \bar{\omega}}{2}}^{\bar{\omega}+\frac{\Delta \bar{\omega}}{2}} a_{r i}(i \bar{\beta}, t) e^{+i \bar{\beta} \alpha} d \bar{\beta} \tag{42}
\end{align*}
$$

where $\alpha$ is a dummy variable for time $t, \Delta t$ is the window width in the time domain, $\overline{\Delta \omega}$ is the window width in the frequency domain, and $\bar{\beta}$ is a dummy variable for circular frequency $\bar{\omega}$. Time $t$ in (41) can be varied continuously for a fixed value of $\Delta t$ resulting in a moving window in the time domain. Likewise, frequency $\bar{\omega}$ in (42) can be varied continuously for a fixed value of $\Delta \bar{\omega}$ resulting in a moving window in the frequency domain. Equation (41)
is actually the Fourier Transform of $a_{r i}(t)$, but considering only its values over the time range $\Delta t$ centered on $t$, while (42) is the inverse Fourier Transform of $a_{r i}(i \bar{\omega}, t)$ but considering only its values over the frequency range $\Delta \bar{\omega}$ centered on $\bar{\omega}$. In some cases, $a_{r i}(i \bar{\omega}, t)$ and $b_{r i}(i \bar{\omega}, t, \alpha)$ are calculated for $\Delta t$ infinite and $\Delta \bar{\omega}$ equal a finite value, respectively; while in other cases, they are calculated for $\Delta t$ equal a finite value and $\Delta \bar{\omega}$ infinite, respectively. In certain special cases, finite values are used for both $\Delta t$ and $\Delta \bar{\omega}$.

To continue with this moving window approach, generate the crosscorrelation coefficients (or functions) as defined by

$$
\begin{equation*}
\rho_{r i, s i}(\bar{\omega}, t, \tau) \equiv \frac{\int_{-\infty}^{\infty} b_{r i}(\bar{\omega}, t, \alpha) b_{s i}(\bar{\omega}, t, \alpha+\tau) d \alpha}{\sqrt{\int_{-\infty}^{\infty} b_{r i}(\bar{\omega}, t, \alpha)^{2} \alpha} \sqrt{\int_{-\infty}^{\infty} b_{s i}(\bar{\omega}, t, \alpha+\tau)}{ }^{2} d \alpha} \tag{43}
\end{equation*}
$$

where $\tau$ is a time difference. By this definition, the cross correlation coefficients fall in the range

$$
\begin{equation*}
-1 \leq \rho_{r i, s i}(\bar{\omega}, t, \tau) \leq+1 . \tag{44}
\end{equation*}
$$

The use of (43) to study the cross correlation of motions $a_{r i}(t)$ and $a_{s i}(t)$ is described in the next section.

### 8.4 Numerical Results of Analyses

A. Directions of Principal Axes

Directions of principal axes were determined for the ground accelerations produced at stations M02, M05, and M12 during the earthquake of November 14, 1980 (Event 2), and at stations C00, IO6, and 009 during the earthquake of January 29, 1981 (Event 5). The directions of these axes when projected on a horizontal plane are shown in Figs. 8.3 and 8.4 for eight different overlapping time segments of 4 sec each. The crosses and dots indicate that the
major and minor axes, respectively, are approximately vertical while the short and long solid lines indicate directions of the intermediate and major axes, respectively. The most significant of these results are those for time segments in the range $0<t<8 \mathrm{sec}$. which covers the high intensity periods of the motions.

During this high intensity time range, the major principal axis for Event 2 points downward towards the hypocenter located approximately 10 km $\mathrm{S} 16^{\circ} \mathrm{E}$ of the center station of the array and at a depth of 62 km . This observation is consistent with high $P$-wave contributions to the ground motions. During the time range $6<t<18 \mathrm{sec}$. , the $4-\mathrm{sec}$. segments show the major principal axis to be approximately horizontal and usually pointing in the general direction of the epicenter.

For Event 5, the major principal axis is approximately vertical only during the first $4-s e c$. segment at stations COO and IO6. For all other time segments, it is approximately horizontal. During the high intensity time range and considerably beyond, the directions of the major principal axis correlate reasonably well with direction to the epicenter located 30 km S $26^{\circ} \mathrm{E}$ of the array's center station. The hypocenter depth for this earthquake was approximately 11 km . These observations are consistent with high S-wave contributions to the high intensity motions.
B. In-Phase and Out-Of-Phase Components of Uni-Directional Motions

In-phase and out-of-phase components of uni-directional motion at selected pairs of stations were calculated using the definition of (40). Figs. 8.5 to 8.9 show Fourier amplitude spectra for each of these components as recorded during Event 2 and Event 5, respectively, for the station pair C00 and I03. The in-phase component for the earthquake of November 14, 1980, is much stronger than the out-of-phase component except for frequencies in
the approximate range 5 to 6 Hz . The large percentage of in-phase motion is consistent with wave fronts of the P-wave type moving in an approximately vertical direction as indicated by the vertically oriented major principal axis previously described. The in-phase and out-of-phase components for Event 5 are approximately equal in intensity if averaged over the entire frequency band $0<t<7 \mathrm{~Hz}$; however, there is a definite shifting of the intensity from one component to the other as a function of frequency. To illustrate this observation, notice the high percentage of out-of-phase motion for frequencies in the neighborhood of 1,3 , and 5 Hz and the low percentage for frequencies in the neighborhood of 2,4 , and 6 Hz . While some effort has been made to rationalize the cause of this phenomenon, no explanation will be set forth at this time. Obviously, further study of these and other results is needed.

## C. Non-Dimensional Normalized Dynamic Response Ratio

The generalized dynamic response ratio $\Phi^{d}(\gamma, \xi, T)$ defined by (22) can be used to correlate the in-phase and out-of-phase components of uni-directional motions at station pairs when placed in its non-dimensional normalized form shown by (23) and when evaluated for $\gamma=+1$ and $\gamma=-1$. Plots of this nondimensional normalized ratio against structural period $T$ are shown in Figs. 8.9 to 8.13 for $\xi=0.05$.

Figures 8.9 and 8.10 show plots of this ratio for station pairs C00 and I03 and C00 and I06, respectively, using $\gamma=+1$ which emphasizes the in-phase component of motion. Notice that the percentage of in-phase motion for Event 2 is very high compared with the corresponding percentage for Event 5, particularly as shown by the longer structural periods. This observation is quite similar for station pairs C00 and 103 and C00 and I06. Clearly, the results of Figs. 8.9 and 8.10 are consistent with mainly propagating SV-waves
for Event 2 and predominant S-waves propagating horizontally for Event 5 .
The non-dimensional normalized response ratio for $\gamma=+1, \xi=0.05$, and for station pair $C 00$ and IO 3 is again plotted against structural period $T$ in Figs. 8.11 and 8.12. Also plotted in these figures is the same response ratio for $\gamma=-1$ which emphasizes the out-of-phase component of motion. Again notice the very high percentage of in-phase motion $(\gamma=+1)$ for Event 2 , as compared with Event 5. Comparison of curves in these same figures for $\gamma=-1$ shows a high higher percentage of out-of-phase motion for Event 5 as compared with Event 2. The plots in Fig. 8.13 correspond to those in Fig. 8.12 except they represent station pair COO and 106 instead of station pair COO and I 03. The results for both station pairs are quite similar.

The observation previously mentioned of an oscillatory shifting of the intensities of in-phase and out-of-phase motions with frequency for Event 5 is again apparent in Figs. 8.12 and 8.13 .

## D. Shear Ratio

The generalized response ratio $\Phi^{t}(\xi, T)$ defined by (29) (called the shear ratio here) is plotted in Figs. 8.14 and 8.15 for Event 2 and Event 5, respectively, using the recorded EW motions for station pair $C 00$ and IO3. The plot in Fig. 8.14 showing the shear ratio to be nearly equal to 1 over the entire structural period range indicates a very large percentage of in-phase motion, in fact, so large a percentage that the rigid base input assumption usually made in engineering practice would be reasonably valid for this case. This observation is quite significant considering the fact that stations $C 00$ and 103 are separated by 200 m .

The shear ratio plot in Fig. 8.15 for Event 5 is quite different from that in Fig. 8.14. It shows a shear ratio considerably less than 1 over most of the structural period range which indicates the double-support input pro-
duces response considerably less than the average of the separate rigid base inputs. The out-of-phase components are obviously strong for this case causing a large reduction in structural response.

By definition, the shear ratio must approach infinity as the structural period approaches zero because the quasi-static shear forces approach infinity while the dynamic shear forces remain finite. This fact explains why the shear ratio is larger than 1 for the shorter structural periods. The quasi-static response also increases the shear ratio above unity in the 1onger structural period range for the case of Event 2 because of the large percentage of in-phase motion. One should note that the shear ratio is exactly unity when the motions at stations C00 and I03 are identically equal. This ratio can exceed unity only as a result of the quasi-static response caused by the out-of-phase motion.

## E. Cross-Correlation Coefficients

The cross correlation coefficient defined by (43) can be used to study the correlation of motions $a_{r i}(t)$ and $a_{s i}(t)$ measured at stations $r$ and $s$, respectively, in the $i$ th direction. Letting $\Delta t$ and $\Delta \bar{\omega}$ in (41) and (42), respectively, become infinite, the cross correlation coefficient is a function of time difference $\tau$ only. Figure 8.16 shows plots of this coefficient for the EW components of motion at two station pairs, namely C00 and I06, and 106 and M08, as recorded during Event 2. The maximum cross correlations for these two station pairs were found to be +0.476 and -0.291 , respectively, while the corresponding cross correlations for zero time difference were found to be +0.204 and +0.167 . These correlations are relatively low as their numerical values are dominated by the higher frequencies in the ground motions. The values of time difference $\tau$ associated with maximum values of correlation are now being used to assist in studies of wave transmission
characteristics (wave type, velocity, and direction). The results of these studies will be reported later.

Because of the dominance of higher frequencies on the cross correlation coefficient and the differences in correlation which exist among frequencies, a moving window in the frequency domain was used to obtain cross correlation as a function of frequency $\bar{\omega}$ and time difference $\tau$. In this case $\Delta t$ was set equal to infinity.

Figures 8.17 to 8.20 show this correlation plotted against ground motion period $(2 \pi / \bar{\omega})$ for $\tau=0$ and for $\Delta f=\Delta \bar{\omega} / 2 \pi=0.488 \mathrm{~Hz}$. East-west components of motion for stations $C 00, I 03, I 06$, and 012 recorded during Event 2 and Event 5 were used as indicated. Figures 8.17 and 8.18 show the cross correlations to be very high for the longer periods of motion recorded during Event 2, and they show a relatively fast drop in correlation with decreasing periods below 1 sec . In contrast, the cross correlations are relatively low over the entire period range for the motions recorded during Event 5, as shown in Figs. 8.19 and 8.20 , except in the near neighborhood of certain discrete periods. The significance of the oscillatory character of these cross correlation functions is now under investigation with no definitive conclusion having yet been reached.

Cross correlation coefficients have been generated for components of motion using both time and frequency moving windows. For example, they were generated for the major principal components of motion at stations M02 and M05 as recorded during the earthquake of November 14, 1980, within the time period 9 to 14 sec , and within the frequency band 2.6 to 3.0 Hz ; see Fig. 8.21. The resulting cross correlation is plotted against time difference $\tau$ in Fig. 8.22. Because of the narrow band character of the components of motion and the phase angles involved, this function has the appearance of
a slowly varying harmonic with a 3.3 sec . period which peaks at about $\tau=5$ sec. where $\rho=0.8$. The significance of this shape is now being correlated with other information to shed lignt on the wave transmission characteristics to be reported later.

## F. Pseudo-Acceleration Response Spectra

Standard normalized pseudo-acceleration response spectra were generated using 5 percent of critical damping for the components of motion recorded during Event 2 and Event 5. The averages of these spectra are shown plotted against structural period in Figs. 8.23 to 8.26 where they can be compared with previously published average spectra representing 4 different soil types ${ }^{2}$. The average spectra for these two earthquakes have shapes which correlate best with the previously published averages for hard site conditions. This observation is not consistent with the relatively soft site conditions of the SMART 1 array, and this suggests dominant influences from the source mechanism.

### 8.5 References

1. Penzien, J. and M. Watabe, "Characteristics of 3-Dimensional Earthquake Ground Motions," Earthquake Engineering and Structural Dynamics, Vol. 3, No. 4, April-June, 1975.
2. Seed, H.B., C. Ugas, and J. Lysmer, "Site-Dependent Spectra for Earthquake-Resistant Design," Report No. EERC-74-12, Earthquake Engineering Research Center, University of California, Berkeley, November, 1974.


Fig. 8.1 Simple shear frame with multi-support excitations.


Fig. 8.2 Simple beam with multi-support excitations.


Fig. 8.3 Directions of principal axes for ground motions produced by the earthquake of November 14, 1980.

| $\begin{gathered} \text { JAN. } 29 \\ 1981 \end{gathered}$ | $\begin{aligned} & \text { STATION } \\ & \text { COO } \end{aligned}$ | $\begin{gathered} \text { STATION } \\ \text { IOG } \end{gathered}$ | $\begin{gathered} \text { STATION } \\ 009 \end{gathered}$ |
| :---: | :---: | :---: | :---: |
| 0-4 SEC. | t | $*$ |  |
| 2-6 SEC. | $1$ | $1$ |  |
| 4-8 SEC. | $1$ | $0$ |  |
| 6-10 SEC. |  | or | $K$ |
| 8-12 SEC. | $1$ |  |  |
| 10-14 SEC. | $1$ |  |  |
| 12-16 SEC. |  |  |  |
| 14-18 SEC. | $\$$ |  | $-$ |

Fig. 8.4 Directions of principal axes for ground motions produced by the earthquake of January 29, 1981.


Fig. 8.5 Fourier amplitude spectrum of the EW in-phase component of motion for the station pair COO and IO3: Event 2


Fig. 8.6 Fourier amplitude spectrum of the EW out-of-phase component of motion for the station pair COO and I03: Event 2


Fig. 8.7 Fourier amplitude spectrum of the E-W in-phase component of motion for the station pair COO and I03: Event 5


Fig. 8.8 Fourier amplitude spectrum of the EW out-of-phase component of motion for the station pair C00 and I03: Event 5


Fig. 8.9 Normalized dynamic response ratio of EW components of motion at stations C00 and I03: $\gamma=+1$


Fig. 8.10 Normalized dynamic response ratio of EW components of motion at stations $C 00$ and IO6: $\gamma=+1$


Fig. 8.Il Normalized dynamic response ratio of EW components of motion at stations C00 and I03: Event 2; $\gamma=+1, \gamma=-1$


Fig. 8.12 Normalized dynamic response ratio of EW components of motion at stations COO and I03: Event 5: $\gamma=+1, \gamma=-1$


Fig. 8.13 Normalized dynamic response ratio of EW components of motion at stations C00 and I06: Event 5; $\gamma==1, \gamma=-1$


Fig. 8.14 Shear ratio of EW components of motion at stations C00 and I03: Event 2


Fig. 8.15 Shear ratio of EW components of motion at stations COO and I03: Event 5

Fig. 8.16 Cross correlation coefficient of EW components of motion for the
station pair C00 and IO6, and for $I 06$ and M08,


Fig. 8.17 Cross correlation coefficient of EW components of motion for the station pair C00 and 103 using a frecuency domain moving window: Event 2


Fig. 8.18 Cross correlation coefficient of EW components of motion for the station pair C00 and IO6 using a frequency domain moving window: Event 2


Fig. 8.19 Cross correlation coefficient of EW components of motion for the station pair C00 and I06 using a frequency domain moving window: Event 5


Fig. 8.20 Cross correlation coefficient of EW components of motion for the station pair 106 and 012 using a frequency domain moving window: Event 5


Fig. 8.21 Direction of principal axes at stations M02 and M05 using both frequency and time domain moving windows: Event 2


Fig. 8.22 Cross correlation coefficient of major principal components
of motion at stations M02 and M05: Event 2


Fig. 8.23 Normalized pseudo-acceleration response spectra: EW component; Event 2


Fig. 8.24 Normalized pseudo-acceleration response spectra: EW component; Event 5


Fig. 8.25 Normalized pseudo-acceleration response spectra: NS component; Event 5


Fig. 8.26 Normalized pseudo-acceleration response spectra: vertical component; Event 5

## 9. CONCLUSIONS AND RECOMMENDATIONS

### 9.1 Conclusions

This report summarizes the design, installation, operational and analysis aspects of the development of the SMART 1 array, particularly up to about the end of its first year of operation (September 1980 - September 1981). The array represents a substantial investment in research funds and technical effort by the National Science Foundation and the National Science Council and by seismologists, engineers, and technicians at the Institute of Earth Sciences and the University of California, Berkeley. As the report demonstrates, the enterprise has exceeded the initial expectations with a valuable file of strong-motion data already available. Because the instrument selection, array installation and operation of this digital array involve novel features, it was thought valuable to set out in more detail than usual the more important experiences encountered in practice. Such practical matters should be helpful in the design and operation of other large-scale digital arrays.

The seismological and engineering research based on the measurements of strong motion of earthquakes obtained since September 1980 using SMART 1 is, of course, only in its beginning stages. Nevertheless, we have incorporated in this report some preliminary studies of the recorded ground motions to indicate the type of research that is now feasible and to give an idea of the probable applications. The complete results will eventually be published elsewhere.

This summary report also provides an opportunity to evaluate strengths and weaknesses of the various aspects of the concept of large digital arrays, although perhaps a decade is needed for a balanced and complete critique. An assumption at the International Workshop on Strong Motion in Hawaii (refer-
ence 1 , Section 1.3) was "There is an adequate understanding of the nature of earthquake ground motion to be able to design useful strong-motion arrays which will provide answers to some of the important unresolved questions facing the designers of structures and other facilities in the earthquakeprone regions of the world." Based on the first year of operation of SMART 1, this expectation is substantially correct, but it must be stressed that siting and local technical competence were relatively favorable in this case.

As described in the first chapter of the report, the site of the SMART 1 array on the Lanyang plain is located at the northeast part of Taiwan, only a few hours by car or train from the Institute of Earth Sciences in Taipei. Electricity and telephone services are excellent and the local road system is superior. Cooperation from local authorities and land owners was uniformly favorable. The region was selected also because it has the highest seismic activity in Taiwan, with both shallow and intermediate focus earthquakes of sufficient strength to trigger array elements. The expectation of earthquake recordings in the short term has proved correct. A seismic reflection survey had been done in 1976 across the Lanyang plain which showed a flat surficial alluvial layer with 800 to $1000 \mathrm{~m} / \mathrm{sec} P$ wave propagation velocity, underlain by dipping alluvial layers with $1800-2000 \mathrm{~m} / \mathrm{sec} P$ wave propagation velocity. It is clear, however, that a full understanding of the recorded wave patterns will require more detailed mapping of the soil layers and geological structure; further geophysical surveys supplemented by boreholes will be required. The region is undergoing economic development with some multi-story buildings, substantial bridges and harbor facilities now appearing and planned. Some structures have already been instrumented with regular three-component accelerometers so that valuable engineering
comparisons between structural response and array recordings will be possible.

The selection of a concentric circular array has proved beneficial. From the seismological point of view, this configuration helps in the determination of wave velocity, wave number, and the structure under this array, given various source locations. In other locations, where sources are restricted to specific faults, an omni-directional configuration may not be optimal. From the engineering point of view, the 2 km radius of the outer ring, containing 12 instruments, yields an inter-element distance that is larger than needed in practice. For most spatial variation of ground motion of engineering interest, a more densely spaced array is required. The interelement spacing of the inner ring (about 100 m ) is, however, directly applicable, even though the relative distance between stations in some smallerscale arrays is much less. (The spacing is about 20 m in the 1979 E1 Centro, California, differential array ${ }^{2}$.)

The instruments selected for SMART 1 have proved to be relatively trouble-free and to have a number of useful characteristics. In particular, the crystal oscillator is precise and the anti-aliasing filter adequate. A trigger level setting of 0.05 g has proved satisfactory. Because each instrument is checked every 2 to 3 days, no conclusion can be reached about reliability of such digital devices when servicing is long-term. Initial experience with the special digital processing equipment designed for SMART 1 is favorable. The data playback and correction, including removal of time marks. glitches and the DC shift are remarkably fast. Generally, it takes less than fifteen minutes to scan and correct a single acceleration record. So far only the digital records of two major earthquakes, November 14,1980 (Event 2) and January 29, 1981 (Event 5) have beeh analyzed to any extent
from 9-track tape copies. The experience with these tapes and records on the Mod Comp mini-computer system at the U.C. Seismographic Station has been quite satisfactory. A number of tape copies have been made available for analysis at other research centers but a survey of their performance is premature.

It should be pointed out that some of the smaller ground motions that have triggered array elements at the 0.05 g threshold setting provide only limited digital samples. This leads to accelerograms that appear stepwise discontinuous when played back visually. . The difficulty can be overcome if necessary by decreasing the trigger level and increasing the gain.

In response to a crucial need in engineering design, research with array records has concentrated on what can be learned about in-phase and out-of-phase components of horizontal seismic ground motion. It has been found that, in the frequency range 1.0 to 10 Hz , cross-correlation coefficients are dominated by higher frequencies. Cross-correlations as a function of frequency for different pairs of stations have shown that high Fourier amplitudes of in-phase or out-of-phase waves may produce a high dynamic response of linear systems. The model indicates the influence on the structure of the out-ofphase input.

Another aspect of the phase problem, related to foundation-structure interaction, is the frequency dependence of the dominant direction of incident wave propagation. It has been demonstrated with SMART 1 records that the variance ratio $R(f)$ can be used to infer the dominant directions of the harmonic wave components. For high values of $R(f)$, there is no dominant direction at this frequency $f$. Also, different types of seismic waves (P. SH, Rayleigh, Love, etc.) can be identified by the use of the ratio of the principal variances and the maximum power spectral density function.

The principal variance calculation also provides a way to identify inter-element wave propagation characteristics for comparison with the average values obtained from frequency-wave number analysis for the whole array. Most probabilistic analyses of structural response assume that the ground motion inputs are uncorrelated, i.e., the cross-spectral density function of the excitation is assumed zero. Because of the special configuration of the SMART 1 array, there is no difficulty in calculating the coherence between different station pairs and thus establishing a cross-spectral model. Studies of the phase change and distance attenuation of the amplitude of the cross-spectra show promise, even though the parameters of the crossspectral density function depend on the focal depth and magnitude of the earthquake.

In the measurement of coherency of Rayleigh waves of frequency about 1 Hz propagating across the array, a loss of correlation was found to be significant for the largest earthquake recorded. This effect may be due to the scattering of waves for larger station separation. McLaughlin et al. ${ }^{3}$ have also discussed wave attenuation and random scattering in a study of waves across a sparser array from underground explosions in Nevada.

A few other papers on strong motion recorded by other arrays have recently appeared, allowing limited comparison with SMART 1. Smith et al. ${ }^{1}$ have analyzed digital accelerograms from a small-scale linear E1 Centro differential array for the 1979 Imperial Valley earthquake. Because absolute time was not available at each element, they use an aftershock record to align the arrival of $P$ waves and establish the time reference. In their subsequent correlation study, they define the covariance of two records in the usual way (see Chapter 7), as

$$
r_{x_{i} x_{j}}(k)=\frac{{ }_{x_{i} x_{j}}^{2}(k)}{\sigma_{x_{i} x_{i}}{ }_{x_{j} x_{j}}}
$$

It is important to study the covariance not only for $k=0$, but also for different values of $k$, and this analysis is being done with the SMART 1 data.

Besides the establishment of a cross-spectrum model of ground motion, spatial averaging of array data also provides important information on the effect of rigid non-embedded foundations on the seismic waves (the "tau" effect). We have defined a ground motion spectral ratio RTAU as the ratio of the spectrum of the array-average time history to the array-average spectrum of each individual time history, i.e.,

$$
\operatorname{RTAU}=\frac{F\left\{\ddot{v}_{g 1}+\ddot{v}_{g 2}+\ldots .+\ddot{v}_{g m}\right\}}{F\left\{\ddot{v}_{g 1}\right\}+F\left\{\ddot{v}_{g 2}\right\}+\cdots \cdot F\left\{\ddot{v}_{g m}\right\}}
$$

where $F\}$ is the Fourier transform of the time signal. The average of the free-field ground motions at each instant in time over the array provides an estimate of the translational motion that a rigid foundation, secured to the ground over the array dimension, will undergo as a result of the seismic excitation. Calculations using ground motion measurements over the inner ring yield a spectral ratio RTAU that approaches 1 from 1 Hz up to 4 Hz , and then decays to zero above 4 Hz (see Figs. 9.1 to 9.3). Further, it has been found that the foundation averaging "tau" depends on the phase difference of the input signals.

Another promising line of research using inter-element array motions concerned the ground strains developed. The seismic behavior of oil or gas pipelines is predominantly controlled by the ground strain/displacement characteristics. Free field motion on the surface of the ground is suf-
ficient to represent ground motion input for such systems because, even for buried pipelines, depth in general is shallow relative to the surface soil layer. By transfoming coordinates to the longitudinal direction and the transverse direction, the normal ground strain $\varepsilon_{i j}$ along the epicentral direction between stations 006 to 012 (see Fig. 1.2) was expressed as

$$
\varepsilon_{i j}=\frac{U_{x}^{i}-U_{x}^{j}}{L_{i j}}
$$

where $\varepsilon_{i j}$ represents the average strain between stations $i$ and $j$, and $U_{x}^{i}$ and $U_{x}^{j}$ are ground displacements in the $x$ direction at the two stations, respectively; $L_{i j}$ is the distance between $i$ and $j$. Based on this procedure, the strain time histories for the SMART 1 site are as shown in Fig. 9.4. The maximum strains at the site are given in Table 9.1.

Finally, as noted in the work of $N$. Newmark, measurements of torsional components of strong ground motion are of engineering importance. The close element spacing and circular geometry of SMART 1 allow estimation of rotational motions (i.e., the components of curl $\underset{\sim}{u}$ ). Some promising calculations have begun on this parameter and details will be published elsewhere.

### 9.2 Recommendations

A special seminar on Strong-Motion Seismic Instrument Arrays was held in Taipei and Lotung on September $7-10,1981$, with about thirty seismologists and earthquake engineers participating. It was agreed that the SMART 1 project is one of the most productive undertaken under the present Cooperative Science Program. The meeting participants (1isted at end of Section 9.3) strongly endorsed the following recommendations:

1. Support should continue by both the NSF and the NSC for the operation of the SMART 1 array with provision of the necessary funds for the
vital analysis and interpretation of data already obtained and likely to be obtained in the future.
2. The efficiency of data analysis at the Institute of Earth Sciences, Academia Sinica, which handles the data processing for the SMART 1 array, needs improvement by acquisition of additional computer CPU capacity and peripheral hardware and software support.
3. A seismic profile should be conducted to allow critical delineation of the subsurface structure of the Lanyang sedimentary basin near the array site and at least one borehole to basement rock should be drilled and logged within the array.
4. The present SMART 1 array should be augmented by the addition of a string of downole sensors and one or more extended surface radial arms to an appropriate distance for the study of attenuation of strong ground motion on various foundation materials.
5. Strong motion instruments should be installed in high-rise buildings and other suitable structures in the vicinity of the SMART 1 array site particularly for structural response studies and soil-structure interaction studies.
6. Timely distribution of the raw data and analysis results to the general scientific and engineering communties is essential. The principal investigators of the SMART 1 project are urged to take proper measures to ensure that scientific data and information are expeditiously distributed for general use and application.

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TABLE 9.1

Maximum ground strain $\left[x \quad 10^{-5}\right]$ along the profile from site 006 to 012 of SMART 1.

| Segment | Strain $\varepsilon_{i j}$ |
| :---: | :---: |
| $006-$ M06 | -3.3 |
| M06-I06 | -3.1 |
| I06-C00 | -3.1 |
| C00-I12 | 4.6 |
| I12-M12 | 2.4 |
| M12-012 | -2.5 |

Earthquake: Jan. 29, 1981


Fig. 9.1 Spectral ratio RTAU in the NS direction: Event 5

Earthquake: Jan. 29, 1981


Fig. 9.2 Spectral ratio RTAU in the EW direction: Event 5

Earthquake: Nov. 14, 1980


Fig. 9.3 Spectral ratio RTAU in the EW direction: Event 2

Earthquake: Jan. 29, 1981
(radial direction)


Fig. 9.4 Ground strains between selected pairs of elements: Event 5

APPENDIX A

3-Component Data Listing of Station IO3 of Earthquake of January 29, 1981 (Event 5)


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APPENDIX B

Time History of Station I03
(see opposite page)


## APPENDIX C

Calculated Velocity and Displacement of NS Component of Station 103 (see opposite page)


## APPENDIX D

Fourier Amplitude Spectrum of Acceleration of Station I03 (see opposite page)
fourier amplitude spectrum of acceleration


## APPENDIX E

Frequency-Wave Number Spectral Formula

The formula for the high resolution method for frequency-wave number analysis can be represented in the following way.

For station $j$, the spectrum is

$$
f_{j}(\omega)=\int_{t_{0}}^{t_{0}+\Delta T} a_{j}(t) e^{-i \omega t} d t
$$

Define the cross-spectrum as

$$
S_{j \ell}(\omega)=f_{j}(\omega) f_{\ell}^{*}(\omega)
$$

and compute

$$
P(\omega, \underline{k})=\left\{\sum_{j, \ell} Q_{j \ell}(\omega) e^{\left.-i \underline{k} \cdot\left(\underline{r}_{j}-\underline{r}_{\ell}\right)^{-1}\right\}^{-1}, ~}\right.
$$

where

$$
\left\{Q_{j \ell}(\omega)\right\}=\left\{S_{j \ell}(\omega)\right\}^{-1}
$$

Then normalize the maximum $P(\omega, k)$ to 0 db . Finally, $P(\omega, k)$ is contoured. The contoured diagram can be analyzed for average horizontal phase velocity and direction of wave propagation (see Figs. 5.5 and 5.6).

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[^0]:    Azim: Array to epicenter azimuth; $\mathrm{*}^{\mathrm{T}}$ : Number of stations triggered
    

[^1]:    fndut โeวfixan ox

