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**SEISMIC FRAGILITY ANALYSIS OF  
SHEAR WALL STRUCTURES**

by

**Jing-Wen Jaw and Howard H.M. Hwang**

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April 30, 1988

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## PREFACE

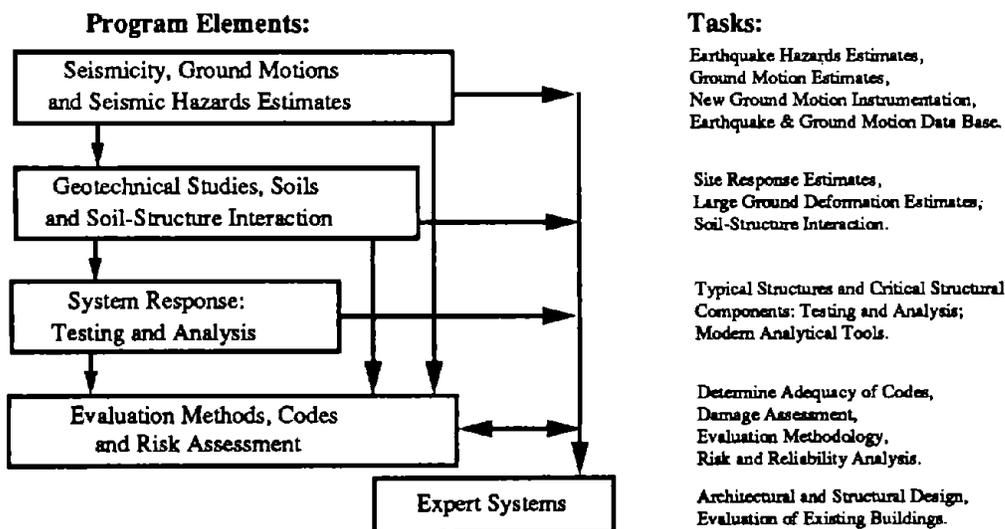
The National Center for Earthquake Engineering Research (NCEER) is devoted to the expansion of knowledge about earthquakes, the improvement of earthquake-resistant design, and the implementation of seismic hazard mitigation procedures to minimize loss of lives and property. Initially, the emphasis is on structures and lifelines of the types that would be found in zones of moderate seismicity, such as the eastern and central United States.

NCEER's research is being carried out in an integrated and coordinated manner following a structured program. The current research program comprises four main areas:

- Existing and New Structures
- Secondary and Protective Systems
- Lifeline Systems
- Disaster Research and Planning

This technical report pertains to Program 1, Existing and New Structures, and more specifically to Evaluation Methods and Risk Assessment.

The long term goal of research in Existing and New Structures is to develop methods for rational probabilistic risk assessment for damage or collapse of structures, mainly existing buildings, especially in regions of moderate seismicity. The work will rely on improved definitions of seismicity and site response, experimental and analytical evaluations of systems response, and more accurate assessment of risk factors. This technology will be incorporated in expert systems tools and improved code formats for existing and new structures. Methods of retrofit will also be developed. When this work is completed, it should be possible to characterize and quantify societal impact of seismic risk in various geographical regions and large municipalities. Toward this goal, the program has been divided into five components, as shown in the figure below:



Evaluation Methods and Risk Assessment Studies constitute one of the important areas of research in Existing and New Structures. Current research activities include the following:

1. Development of a damage estimation procedure for the eastern United States.
2. Evaluation of Response Modification Factor (RMF) for buildings and bridges.
3. Development of a probabilistic procedure to determine load and resistance factors.
4. Development of procedures for the evaluation of seismic safety of buildings in zones of moderate seismicity.
5. Development of computer codes for identification of degree of building damage and for damage-based automated design.

The ultimate goal of projects concerned with Evaluation Methods and Risk Assessment is to provide practical tools for engineers to assess seismic risk to individual structures and thus, to estimate social impact.

*In this report, analytical procedures for developing fragility curves for building structures are presented and demonstrated with numerical examples carried out on actually designed shear wall structures. As such, this study is useful for urban seismic risk assessment as well as risk assessment of individual building structures.*

## ABSTRACT

This report presents a fragility analysis method to generate seismic fragility curves for structures, in particular, shear wall structures. Uncertainties including randomness and modeling uncertainty in earthquake ground motion and structure are quantified by evaluating uncertainties in pertinent parameters which define earthquake load-structure system. The uncertainty in each parameter is characterized by several representative values and then the Latin hypercube sampling technique is utilized to combine these values to construct samples of earthquake load-structure system. For the response analysis, the modified Takeda hysteretic model is utilized to describe the nonlinear structural behavior. The nonlinear seismic analyses are performed in time domain for all samples of earthquake load-structure system to obtain an ensemble of structural responses, which are then statistically analyzed. Five limit states representing various degrees of structural damage due to earthquake are established. Then, the statistics of the structural capacity corresponding to each limit state can be established. For a specified level of peak ground acceleration, the limit state probability is evaluated on the basis of statistics of response and capacity for each limit state. The fragility curve is generated by evaluating the limit state probabilities at different levels of peak ground acceleration. For illustration, the fragility curves for a low-rise shear wall building is constructed. The fragility data can be utilized in the seismic risk study to determine potential earthquake-induced loss of life and property damage, then the economic and societal risk can be estimated. In addition, the fragility data can be used by the authority to develop emergency response plan.



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## SECTION 1 INTRODUCTION

The occurrence of earthquakes is potentially catastrophic events. A large earthquake may cause loss of lives, damage of buildings, and interruption of essential services (electricity, gas and water, etc.). Thus, the societal and economic impact due to earthquakes and emergency response after earthquakes are the major concerns to governmental agency, e.g., Federal Emergency Management Agency (FEMA), the professional and the general public. In order to determine earthquake-induced loss of life and damage of properties, evaluate economic as well as societal impact, and develop emergency response plan, it is necessary to assess the vulnerabilities of structures due to different levels of earthquakes. Earthquake-induced damage of structures may result from ground failures such as faulting, landslide and liquefaction. The damage of structures, in particular, building structures is mainly due to ground shaking. Thus, earthquake ground shaking is the only hazard source considered in this study.

At a very low level of ground shaking, one can be almost certain that the building would not collapse. Conversely, at an extreme high level of ground shaking, one can reasonably assume that the building would collapse. The likelihood of structural damage due to different levels of earthquakes is usually expressed by a damage probability matrix or a fragility curve [1,2]. The damage probability matrix describes the probability of different possible damages at a specific level of earthquake, while the fragility curve describes the probability of a specific type of damage at various levels of ground shaking. The fragility curve approach is used in this study to express the vulnerabilities of structures.

Fragility data can be generated by using the following: (1) Actual earthquake data; (2) Fragility or qualification test data; (3) Detailed analytical model; (4) Simplified analytical model; and (5) Design information and engineering judgement. The most desirable fragility data are from actual earthquake experience or from experimental tests, since such data (failure or success) provide information with high confidence. When earthquake and test data do not provide sufficient information, simplified or detailed analytical model may be used to predict damage of structures due to earthquakes. The model can include the randomness and uncertainties in earthquake ground motion and structure. The analytical constructed fragility curves should be verified with actual earthquake data, if available.

The use of design information and engineering judgement is the most economical way to construct fragility data. However, the result may be very sensitive to subjective judgment, especially it is based on the opinions of a few engineers [2].

For nuclear structures, several methods have been proposed for generating fragility data for seismic probabilistic risk assessment studies [3-5]. These methods vary from that based on subjective judgement and design drawings to that based on probabilistic structural mechanics. For conventional structures, two recent efforts were made to estimate the vulnerabilities of structures. Applied Technology Council (ATC) has conducted a project to develop earthquake-induced damage data for facilities in California (ATC-13) [1]. The damage data were developed based on the experience and judgement of engineers, who participated in the questionnaire process for consensus damage estimation. Currently, an effort is being made to modify the California-based damage data to represent the damage data for the facilities in the eastern United States. Another effort was made as part of Central United States Earthquake Preparedness Project [6]. As subcontract to Allen and Hoshall, Inc., Kircher and McCann [7] developed seismic fragility curves for sixteen types of structures common to facilities located in the Mississippi Valley region. Fragility curves for structures were mainly produced by calculations blended with engineering judgment. An attempt to calibrate with damage data observed from past earthquakes was also carried out. In performing fragility calculations, the procedure similar to the so-called Zion method [8], which is heavily rely on engineering judgment, was employed for the purpose of rapid curve development.

In view that the earthquake-induced damage data are too scarce to provide sufficient information for the fragility evaluation, and the fragility data estimated from engineering judgment may not be reliable, therefore, the fragility data generated from analytical models and calibrated with available earthquake experience may be an alternative. Since the detailed analytical model such as the time history analysis with finite element modeling of structures may be too expensive to carry out, the simplified analytical model seems more appropriate for the purpose of fragility evaluation. This report presents a simplified analytical approach to generate fragility data for structures, in particular, shear wall structures. The general methodology is described in Section 2, while Section 3 gives the fragility estimate of a shear wall structure. Then, Section 4 presents the conclusions.

## SECTION 2

### METHODOLOGY OF FRAGILITY ANALYSIS

The generation of fragility curves for structures by using an analytical approach requires to consider appropriate models for earthquake accelerations and structures. In reality, the earthquake ground accelerations and structures involve randomness and other uncertainties. For example, we cannot predict the occurrence of an earthquake in advance and cannot precisely estimate its amplitude, frequency content and duration. Structural responses are usually evaluated with idealized structural models, thus, the computed structural responses may deviate considerably from the actual structural responses. Furthermore, the structural capacity cannot be accurately determined since the basic parameters such as material strength always exhibit statistical variation. In view of uncertainty in earthquake loads, structural response, and structural capacity, a probabilistic approach, which can incorporate the uncertainty arising from different sources, is appropriate for generating seismic fragility data. In this study, uncertainties including randomness and modeling uncertainty in earthquake ground motion and structure are quantified by evaluating uncertainties in pertinent parameters which define earthquake load-structure system. Figure 2-1 outlines the procedure for the proposed fragility analysis method and the important features are described in the following sub-sections.

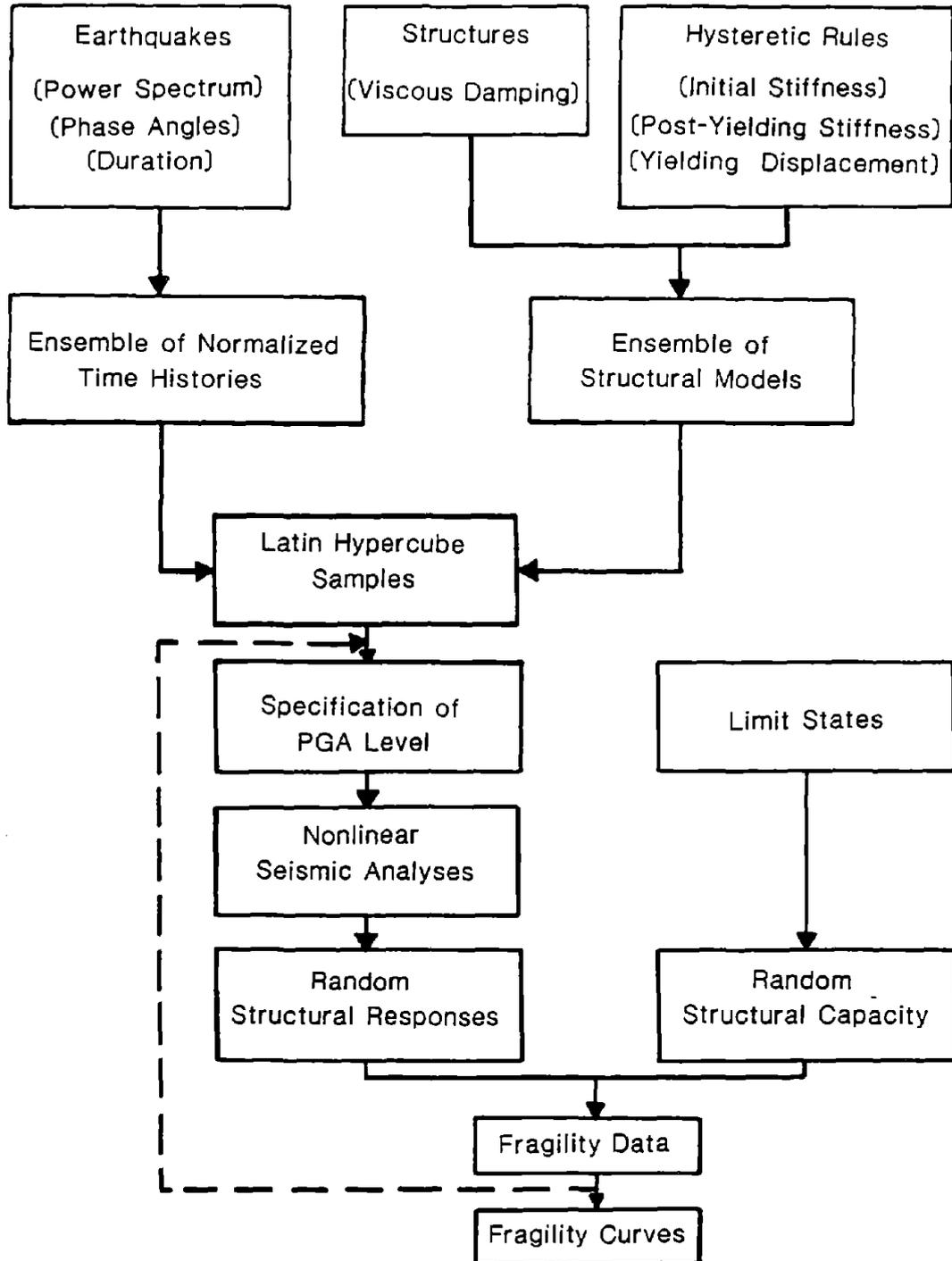
#### 2.1 Nonlinear Seismic Analysis

In order to evaluate the statistics of nonlinear structural responses, it is necessary to perform multiple nonlinear time history analyses to obtain the response data. For such purpose, nonlinear seismic analysis with complicated structural modeling such as finite element approach is too expensive to carry out. Thus, a relatively simple structural model which captures the major features of nonlinear characteristics is more appropriate.

In this study, the structure is represented by a multi-degree-of-freedom (MDF) stick model fixed at the base as shown in Fig. 2-2. Each mass is assumed to have one degree of freedom, i.e., the horizontal displacement in the direction of earthquakes. The equations of motion for such an MDF system subjected to a horizontal earthquake ground acceleration is

$$[M]\{\ddot{X}\} + [C]\{\dot{X}\} + \{F_s\} = -[M]\{I\} a_g \quad (2.1)$$

where



Note: Parameters listed in parentheses are considered as random variables.

Fig. 2-1 Fragility Analysis Procedure

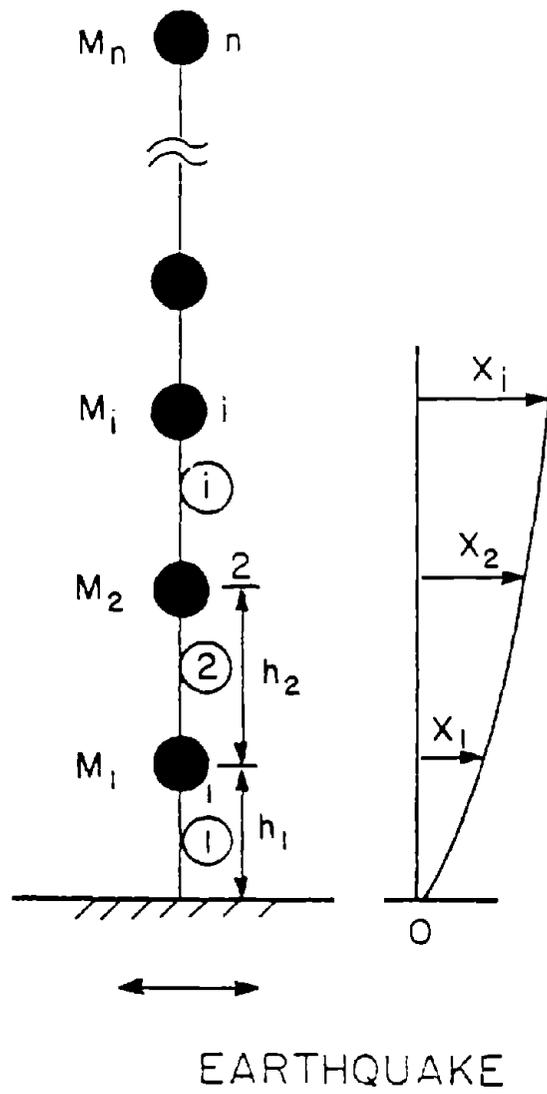


Fig. 2-2 Stick Model of Structure

- $[M]$ : mass matrix
- $[C]$ : damping matrix
- $\{I\}$ : identity vector
- $\{X\}$ : nodal displacement vector relative to the fixed base
- $\{F_s\}$ : restoring force vector
- $a_g$ : earthquake ground acceleration

The mass of the building is discretized at the mid-height of each story and lumped at the floor level. Thus, the mass matrix  $[M]$  is a diagonal matrix. The damping matrix  $[C]$  is taken as the Rayleigh damping matrix, which is the combination of the mass matrix  $[M]$  and the initial stiffness  $[K_e]$  of the structure. The damping matrix  $[C]$  is thus given by the equation:

$$[C] = a_0[M] + a_1[K_e] \quad (2.2)$$

where

$$a_0 = \frac{2\zeta\omega_1\omega_2}{\omega_1 + \omega_2}$$

$$a_1 = \frac{2\zeta}{\omega_1 + \omega_2} \quad (2.3)$$

in which  $\zeta$  is the critical damping ratio;  $\omega_1$  and  $\omega_2$  are the first two natural frequencies of the structure.

The restoring shear force acting on a beam element of the stick model is related to the relative displacement between two adjacent masses. This displacement is denoted as the inter-node (inter-story) displacement. The structure may behave nonlinearly under severe earthquake excitation. Under this situation, it is generally recognized that the degradation of structural stiffness and pinching phenomenon exist in the hysteretic curves. In this study, the hysteretic relationship between the restoring shear force and the inter-node displacement is modeled by the modified Takeda model [9] as shown in Fig. 2-3. This model has a bilinear skeleton curve and includes both stiffness degrading and pinching effects. The modified Takeda model is governed by the following five rules:

1. Elastic loading and unloading with initial stiffness.
2. Inelastic loading with post-yielding stiffness.
3. Inelastic unloading with degrading stiffness.

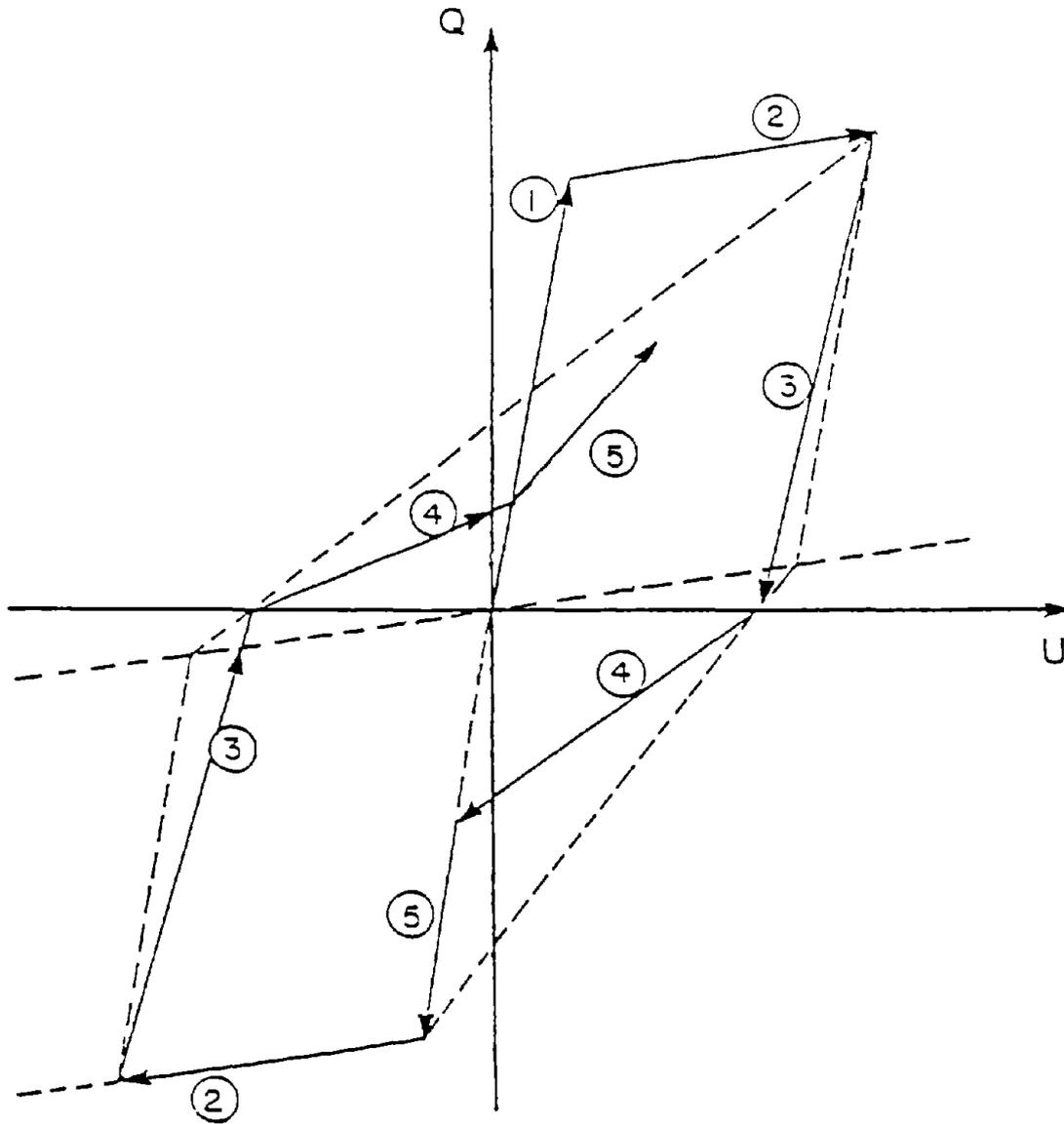


Fig. 2-3 Hysteretic Diagram

4. Inelastic pinched reloading.
5. Peak oriented inelastic reloading.

These five rules result in five possible paths in the hysteretic diagram as identified in Fig. 2-3 by corresponding numbers in circles. Detailed description of the hysteretic rules is presented in Ref. 9. The restoring force vector  $\{F_s\}$  in Eq. 2.1 can be derived based on these hysteretic rules.

In this study, the artificial earthquake acceleration time histories are utilized as seismic input and applied at the base of the structure. For a given earthquake time history, the Newmark's beta method with beta equal 1/4 is used to integrate equations of motion in time domain to obtain structural responses.

## 2.2 Ground Motion Characterization

There are two basic approaches to represent earthquake acceleration time histories. One method is the use of recorded ground motion accelerograms to represent earthquakes that may be expected at a site. Although the number of earthquake records has been increased in past decades, there is a scarcity of strong motion records for some regions, for example, the eastern United States. Aside from the lack of records, neither does this approach grasp the randomness of future earthquakes nor reflect the local site condition. These concerns give rise to the use of simulated artificial earthquake time histories to represent ground motion. Artificial earthquakes may be generated by the following approaches: (1) modify amplitudes and frequencies of actual recorded ground motion accelerograms, (2) develop compatibly from a specified response spectrum, and (3) generate from an appropriate power spectrum. The latter approach, i.e. power spectrum approach, is used in this study.

The stationary acceleration time history  $a(t)$  is simulated by the following expression [10].

$$a(t) = \sqrt{2} \sum_{k=1}^{N_f} \sqrt{S_g(\omega_k) \Delta\omega} \cos(\omega_k t + \phi_k) \quad (2.4)$$

where

- $S_g(\omega)$ : one-sided earthquake power spectrum
- $N_f$ : number of frequency intervals
- $\Delta\omega$ :  $\omega_u / N_f$

- $\omega_u$ : cutoff frequency  
 $\omega_k$ :  $k\Delta\omega$   
 $\phi_k$ : random phase angle uniformly distributed between 0 and  $2\pi$

The power spectrum used in this study is a Kanai-Tajimi power spectrum [11].

$$S_g(\omega) = S_0 \frac{1 + 4\zeta_g^2 \left(\frac{\omega}{\omega_g}\right)^2}{\left[1 - \left(\frac{\omega}{\omega_g}\right)^2\right]^2 + 4\zeta_g^2 \left(\frac{\omega}{\omega_g}\right)^2} \quad (2.5)$$

where  $S_0$  is the intensity of the spectrum which is related to the peak ground acceleration (PGA) [12];  $\omega_g$  and  $\zeta_g$  are the dominant ground frequency and the critical damping, respectively, which depend on the site soil condition.

The normalized nonstationary time history  $a_m(t)$  is obtained by applying an envelope function  $f(t)$  to a stationary time history  $a(t)$ , and then normalized by the maximum of the time history  $a_{max}$ .

$$a_m(t) = \frac{a(t)f(t)}{a_{max}} \quad (2.6)$$

The nonstationary time history  $a_g(t)$  is then obtained from the product of a specified peak ground acceleration  $A_p$  and a normalized nonstationary time history  $a_m(t)$

$$a_g(t) = A_p \times a_m(t) \quad (2.7)$$

## 2.3 Uncertainty Analysis

In this study, uncertainties in structure and earthquake ground motion are quantified by investigating the uncertainty in various relevant parameters describing the analytical model for earthquake load-structure system.

### 2.3.1 Uncertainty in Structural System

The structure is idealized as a stick model with masses lumped at the floor levels. The values of the lumped mass can be determined more or less accurately, thus, the mass is assumed to be deterministic in the present study.

The response of a structure to earthquakes is affected by the energy-dissipation characteristics of the structure. The input seismic energy may be dissipated by structural viscous damping and hysteretic behavior of the structure. It is well known that judgment is usually involved in selecting a value of viscous damping for the dynamic analysis. Therefore, structural viscous damping is treated as random variable and used in conjunction with the structural hysteretic model in the nonlinear seismic analysis.

The modified Takeda hysteretic model utilized in this study is characterized by four parameters: the initial stiffness  $k_e$ , the post-yielding stiffness  $k_p$ , the yielding displacement  $U_y$ , and the pinching factor  $\alpha_p$ . These parameters can be determined from the comparison of simulation results and experimental data. However, the values of these parameters determined from the simulation of one experimental work may differ from the values obtained from the simulation of the other experiments. Moreover, even from one simulation, the hysteretic parameters can not be evaluated precisely. For example, it is generally recognized that the initial stiffness  $k_e$  is less than the uncracked stiffness due to concrete cracking. The degree of reduction in stiffness can not be determined accurately. Thus, the initial stiffness  $k_e$  is treated as random variable. Similarly, the post-yielding stiffness  $k_p$  and the yielding displacement  $U_y$  can not determine exactly and are also treated as random variables. The pinching of the hysteretic loops is caused by the opening and closing the shear cracks during the cyclic loadings. The degree of pinching in hysteretic loops has a significant effect on the area of hysteretic curve which is related to the amount of energy dissipated under cyclic loading. However, the pinching may have less effect on the maximum deformation of the structure. In this study, the maximum ductility ratio, which is closely related to maximum deformation of the structure, is used to represent the structural response. Thus, it is reasonable to assume the pinching factor as deterministic.

### 2.3.2 Uncertainty in Ground Motion

The Kanai-Tajimi (K-T) power spectrum is employed in this study to simulate earthquake acceleration time histories. The K-T power spectrum is defined by three parameters  $S_0$ ,  $\omega_g$  and  $\zeta_g$ . The variation of  $\omega_g$  and  $\zeta_g$  due to site soil conditions has been examined in several recent studies and the statistics of  $\omega_g$  and  $\zeta_g$  for different soil conditions were suggested [13-15]. Thus, in this study,  $\omega_g$  and  $\zeta_g$  are considered as random variables. The parameter  $S_0$  in the K-T power spectrum is related to peak ground acceleration. For the purpose of evaluating the fragility of the structure, the peak ground acceleration is

treated as a parameter, hence,  $S_0$  is deterministic. As shown in Eq. 2.4, a set of random phase angles is generated to simulate an acceleration time history. Of course, different sets of random phase angles are utilized to generate a number of acceleration time histories. Furthermore, an envelope function  $f(t)$  is applied to a stationary time history so that the earthquake acceleration becomes nonstationary with finite duration. The duration of the strong motion is considered as random in this study.

### 2.3.3 Analysis of Uncertainty

In this study, the Latin hypercube sampling technique [16] is utilized to establish samples for nonlinear time history analysis. If the simple random sampling technique is used to generate samples, then the required sample size would be very large. Thus, it is not feasible for nonlinear time history response analysis due to the prohibitive cost. On the contrary, the Latin hypercube sampling technique can provide response statistics using a reasonable number of samples [17].

The four parameters describing the structural model, which are treated as random variables, are: structural viscous damping, initial stiffness, post-yielding stiffness, and yielding displacement. The uncertainty in each parameter is characterized by several representative values obtained from available data in the literature. By combination of the representative values of all parameters, a total of  $N$  samples of the structural model is constructed. For example, for the four parameters mentioned above, if three representative values are selected to characterize uncertainty in each parameter, then 81 structural models will be created.

To characterize uncertainty in ground motion, two power spectrum parameters, i.e.,  $\omega_g$  and  $\zeta_g$ , and strong motion duration as well as phase angle are treated as random. The representative values are selected to characterize the uncertainty associated with each parameter. Several power spectra are obtained from combining representative values of  $\omega_g$  and  $\zeta_g$ . From each power spectrum, a number of artificial earthquakes are generated by using the selected durations and different sets of random phases angles. The total number of artificial earthquakes should be equal to  $N$  which is the same as the number of structural models. Then, following the principle of the Latin hypercube sampling technique, the structural models are matched to the earthquake time histories to construct  $N$  samples of earthquake load-structure system for nonlinear seismic analysis.

## 2.4 Probabilistic Structural Response

For each earthquake load-structure system, nonlinear seismic analysis is carried out to evaluate the responses of the structure, e.g., the story ductility ratios of all stories. The  $i$ -th story ductility ratio  $\mu_i$  is defined as the ratio of the maximum absolute inter-story displacement  $U_{max,i}$  to the yielding displacement  $U_{y,i}$ .

$$\mu_i = U_{max,i}/U_{y,i} \quad (2.8)$$

The maximum ductility ratio of the structure  $\mu_E$  is the largest value among all story ductility ratios.

$$\mu_E = max(\mu_i) \quad (2.9)$$

In this study, the maximum ductility ratio  $\mu_E$  is utilized to represent structural response. The  $N$  samples of  $\mu_E$ , which are obtained from time history analyses for all earthquake load-structure systems, is statistically analyzed in order to determine sample mean and sample standard deviation. The data are also plotted in the probability paper to determine the appropriate distribution.

## 2.5 Limit States and Structural Capacity

In order to generate structural fragility curve, the limit states of a structure must be defined. A limit state generally represents a state of undesirable structural behavior, for example, structural collapse or instability. For a structure, it is likely that more than one limit state has to be considered. The damage of a structure due to earthquakes usually involves nonlinear structural behavior. The presence of the nonlinear behavior makes it difficult to formulate limit states based on strengths of the structure. Various damage models which incorporate maximum deformations and/or energy dissipation have been proposed [18]. However, the use of energy-related damage model to define limit states sometimes is difficult due to the lack of experimental data. In general, both structural and non-structural damages due to earthquakes can be attributed to excessive inter-story displacement. The inter-story displacement is, therefore, a good measure of the degrees of damage. The ductility ratio is closely related to inter-story displacement as indicated in

Eq. 2.8. Thus, in this study, the limit state is defined in terms of the maximum ductility ratio of the structure.

In the event of earthquakes, damage of structures is observed to occur in varying degrees from no damage to collapse. Thus, in this study, five limit states representing nonstructural damage, slight structural damage, moderate structural damage, severe structural damage, and collapse of the structure are considered. For each limit state, a corresponding capacity in terms of the maximum ductility ratio can be established. The structural capacity  $R$  is usually modeled by a lognormal distribution [19].

$$R \equiv LN(\tilde{R}, \beta_R) \quad (2.10)$$

where LN stands for the lognormal variable;  $\tilde{R}$  and  $\beta_R$  are the median value and the logarithmic standard deviation of  $R$ , respectively.

## 2.6 Fragility Curves

For a given level of peak ground acceleration, the structural fragility with respect to a particular limit state is defined as the conditional probability that the structural response  $S$  exceeds the structural capacity  $R$ . It can be shown that the conditional limit state probability  $P_f$  may be written as [20]:

$$P_f = P_r(R \leq S) = \int_0^{\infty} [1 - F_S(r)] f_R(r) dr \quad (2.11)$$

where  $F_S(\cdot)$  is the cumulative probability distribution of  $S$  and  $f_R(\cdot)$  is the probability density function of  $R$ . The fragility curve for a particular limit state can be constructed by evaluating  $P_f$  at different levels of PGA. Fragility curves for various limit states can be developed in a similar manner.



## SECTION 3 FIVE-STORY SHEAR WALL BUILDING

### 3.1 Description of Structure

The building selected to demonstrate the fragility analysis methodology is a five-story reinforced concrete office building assumed to be located in New York City [21]. Figure 3-1 shows a typical floor plan and section of the building. A reinforced concrete frame system is used to resist dead and live loads, while the lateral loads such as earthquakes are resisted by shear walls in both directions. In this study, seismic fragility analysis is performed for the two shear walls in the north-south direction. The detail of the design is shown in Ref. 21, and a brief summary of the design is outlined below.

The shear wall building is designed according to the provisions of ANSI A58.1-1982 Standard [22] and ACI 318-83 code [23]. Three types of loads, i.e., dead, live, and earthquake loads are considered to act on the building. The dead and live loads acting on each shear wall are shown in Ref. 21. Originally, various combinations of seismic zones and soil conditions were considered. In this study, only the design case with seismic zone 2 and soil type 2 is utilized. The design seismic base shear is determined by the formula specified in ANSI A58.1. This design base shear is distributed over the height of the building, and then the shear force and overturning moment at each floor level are determined accordingly. The shear walls are designed to provide sufficient resisting capacity against all postulated combinations of load effects (axial force, shear force, moment, etc.). The cross section and reinforcement arrangement of the shear wall are shown in Fig. 3-2. The barbell shape shear wall is composed of the web wall and two end columns (boundary elements). The thickness of the wall is 5 in. and one layer of No. 3 rebars with 5 in. spacing is used in both horizontal and vertical directions. The end columns are 22 in.  $\times$  22 in. for first and second stories, 20 in.  $\times$  20 in. for third through fifth stories, and 16 No. 9 rebars are used for all end columns.

### 3.2 Modeling of Structure

The shear wall structure is modeled as an MDF stick model with one degree of freedom per story. The stick model consists of lumped masses connected by beam elements. The convention of numbering nodes and elements is depicted in Fig. 2-2. Table 3-I lists the

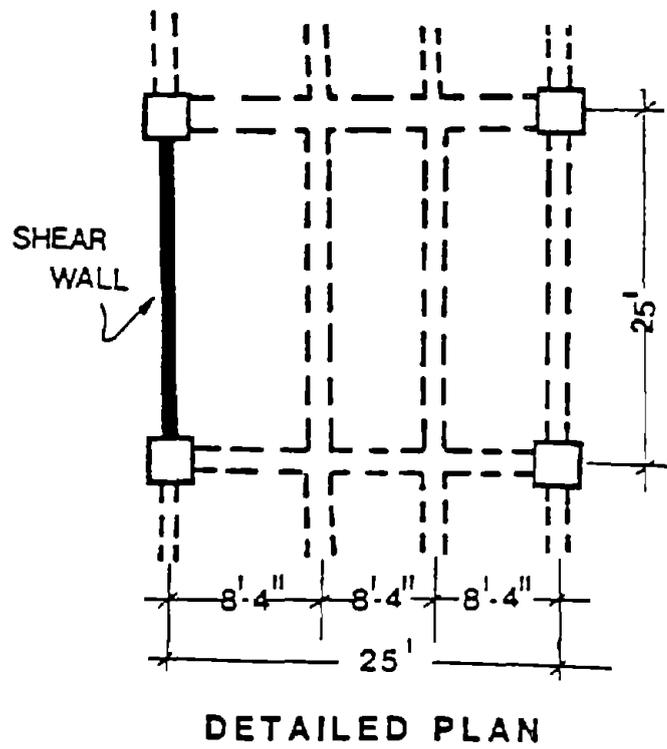
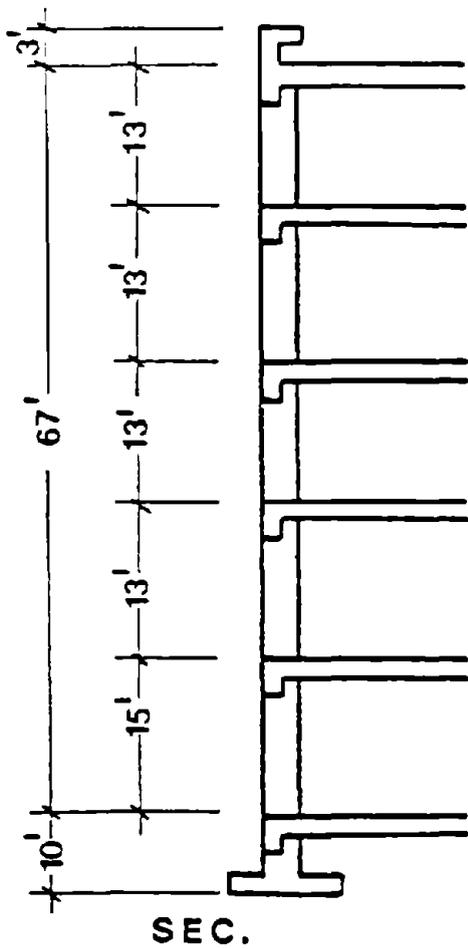
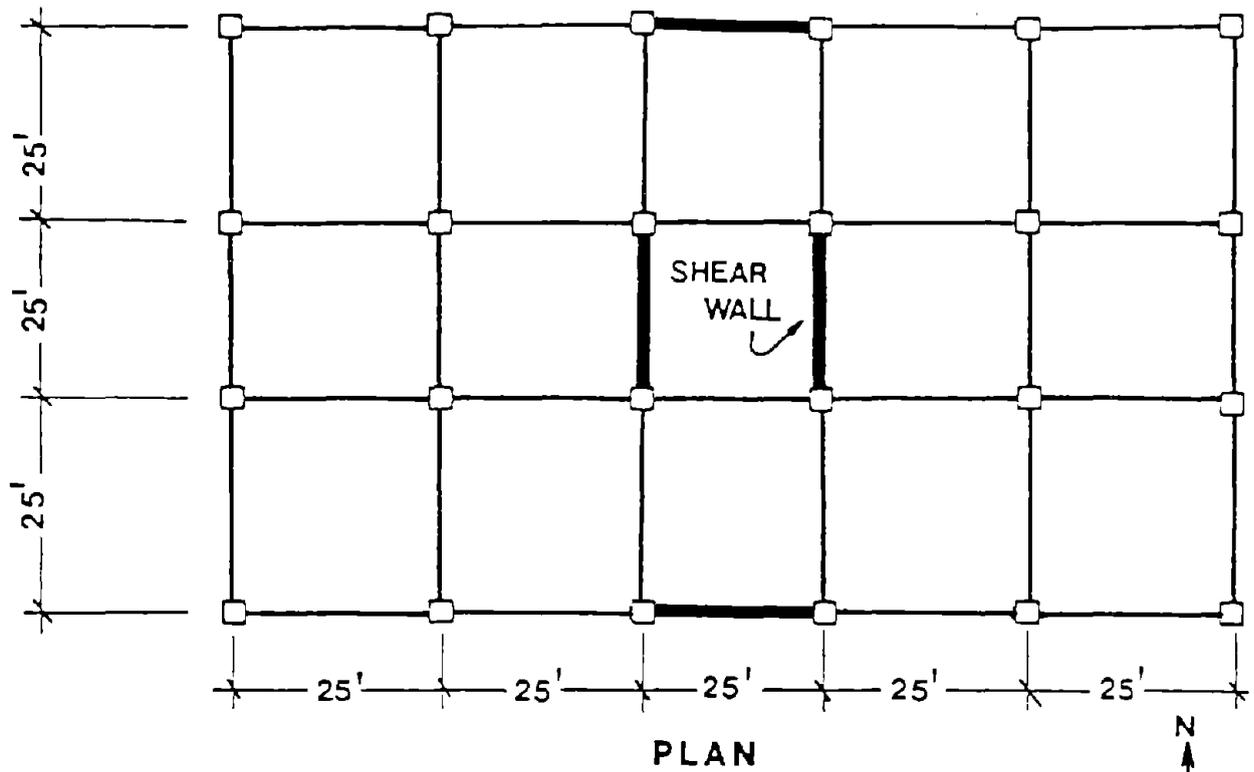


Fig. 3-1 Plan and Section of Office Building

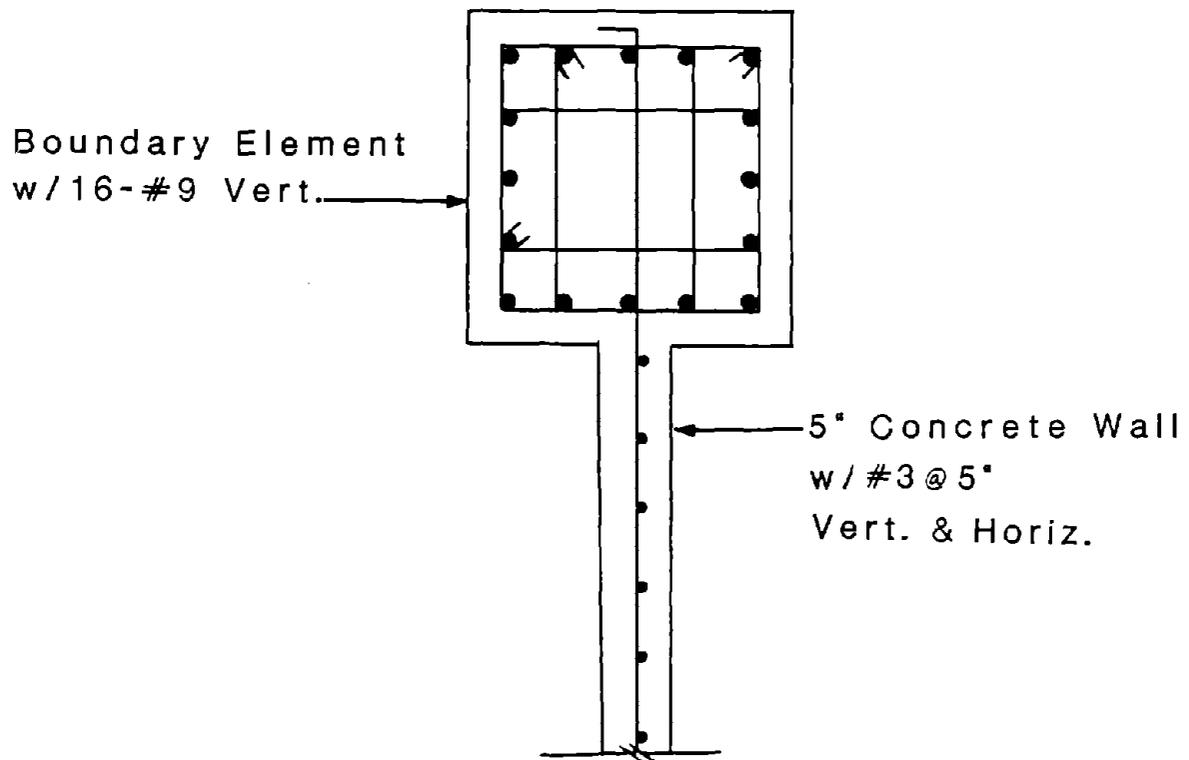


Fig. 3-2 Detail of Shear Wall

**Table 3-I Stick Model Properties**

Node or Element No.	Mass (kips-sec <sup>2</sup> /in)	Element Height (in)	Shear Area (in <sup>2</sup> )
5	1.817	156	1400
4	2.105	156	1400
3	2.105	156	1400
2	2.134	156	1390
1	2.199	180	1390

lumped mass at each floor level. The height and effective shear area of beam elements are also included in the table. For shear wall with two boundary columns, the effective shear area is the web area.

The structure dissipates the input seismic energy by structural viscous damping and hysteretic behavior. The structural viscous damping is assumed to represent the energy dissipated within the range of linear elastic response. It has been recommended that the critical damping ratio ranges from 2 to 5 percent for reinforced concrete structures [24]. Thus, three representative values of the critical damping ratio are selected as 2, 4, and 6 percent.

### 3.3 Hysteretic Model

In this study, the shear force-displacement relationship for each beam element follows the modified Takeda hysteretic model. The parameters defining the hysteretic model are: initial stiffness  $k_e$ , post-yielding stiffness  $k_p$ , yielding displacement  $U_y$ , and pinching factor  $\alpha_p$ . These parameters are determined as follows.

Experimental studies of shear walls have indicated that the initial stiffness  $k_e$  is significantly less than the uncracked stiffness  $k_0$  due to the existence of the shear cracks. Thus, the initial stiffness  $k_e$  can be expressed as the fraction of the uncracked stiffness.

$$k_e = \alpha_g k_0 \quad (3.1)$$

where  $\alpha_g$  is the stiffness ratio and the uncracked stiffness  $k_0$  is computed as

$$k_0 = \frac{G_0 A_s}{h} \quad (3.2)$$

in which  $A_s$  and  $h$  are the shear area and the height of beam element, respectively;  $G_0$  is the shear modulus of the uncracked concrete which is determined from the Young's modulus  $E_c$  and the Poisson's ratio  $\nu$  of concrete.

$$G_0 = \frac{E_c}{2(1 + \nu)} \quad (3.3)$$

The stiffness ratio  $\alpha_g$  can be deduced from the available experimental results. Bennett et al. [25] summarized the results of both static and dynamic tests for low-rise isolated

and box-like shear walls. The parameter  $\alpha_g$ , ranging from 0.25 to 0.33 were reported in their investigation. Morgan et al. [26] tested an isolated shear wall under reversing static loads. On the basis of load-deflection diagram from the test as well as concrete cross section and material properties of the wall specimen,  $\alpha_g$  is determined to be approximately 0.17. Oesterle et al. [27] conducted an experimental investigation of isolated shear walls subjected to cycling loads. Based on properties of test specimens and envelope curves of measured shear force versus shear distortion,  $\alpha_g$  is computed to be 0.16. Tohma and Hwang [28] studied the hysteretic behavior of reinforced concrete containment under cyclic loading. By comparison of the simulated and experimental results,  $\alpha_g$  is determined to be 0.07. This relatively low value of  $\alpha_g$  is due to the significant shear deformation. Compiling the values of  $\alpha_g$  presented above, three values of  $\alpha_g$ , namely 0.1, 0.17 and 0.25, are chosen to represent the variation in  $\alpha_g$ .

The post-yielding stiffness  $k_p$  is expressed as a product of post-yielding slope factor  $\alpha_s$  and initial stiffness  $k_e$ . The value of  $\alpha_s$  is determined empirically by measuring the post-yielding slopes of load-deformation envelopes of two shear wall experiments [26, 27].  $\alpha_s$  is approximately 0.02 for the shear wall considered in Ref. 26 and 0.03 from the test result presented in Ref. 27. It is not uncommon to find the value of  $\alpha_s$ , ranging from 0 (elasto-plastic system) to five percent is used in many analytical studies. Thus, based on the foregoing data, three values of  $\alpha_s$ , i.e., 0.01, 0.03 and 0.05, are chosen to characterize the variation in  $\alpha_s$ .

In this study, the yielding displacement  $U_y$  of the shear beam is obtained from multiplying the yielding shear strain  $\gamma_y$  by the element height  $h$ . The yielding shear strains can be measured from the hysteretic curves. From the hysteretic curves shown in Refs. 26 and 27, three values, i.e. 0.002, 0.0025 and 0.003, are selected as representative values.

The pinching factor  $\alpha_p$  needs to be determined so that the hysteretic model could be described completely. The pinching of the hysteretic loops is caused by the opening and closing of the shear cracks during the cyclic loadings. Tohma and Hwang [28] simulated the experimental results to examine the effect of pinching. The pinching factor of 0.3 was suggested to be an appropriate value. The degree of pinching in hysteretic loops has a significant effect on the area of hysteretic curve which is related to the amount of energy dissipated under cyclic loading. However, the pinching may have less effect on the maximum deformation of the structure. In this study, the maximum ductility ratio, which

is closely related to maximum deformation of the structure, is used to represent structural response. Thus, the pinching factor is assumed as deterministic and set to be 0.3.

### 3.4 Ensemble of Structures

The four parameters describing the model of the structure, which are treated as random variable, are: structural viscous damping, stiffness ratio, post-yielding stiffness, and yielding displacement. The uncertainty in each parameter is represented by 3 values as summarized in Table 3-II. From the combinations of three representative values of these four parameters, a total of 81 structural models can be established.

To illustrate how to construct the structural model from the parameter values taken from Table 3-II, a set of parameters values, e.g. 0.04 for critical damping ratio, 0.17 for stiffness ratio, 0.03 for post-yielding slope factor and 0.002 for yielding shear strain, is utilized. For concrete compressive strength of 3000 psi and the Poisson's ratio of 0.2 as assumed in design [21], the shear modulus of the uncracked concrete  $G_0$  is determined to be  $3.1 \times 10^6$  psi (Eq. 3.3). Using physical properties of beam elements as shown in Table 3-I, the uncracked stiffness  $k_0$  and initial stiffness  $k_e$  of beam elements can be determined from Eqs. 3.2 and 3.1, respectively. Then, the post-yielding stiffness  $k_p$  of beam elements are obtained from multiplying initial stiffness by the post-yielding slope factor. From the specified yielding shear strain, the yielding displacement  $U_y$  of the element can then be determined from multiplying yielding shear strain by the element height. Once the initial stiffness  $k_e$ , the post-yielding stiffness  $k_p$ , and the yielding displacement  $U_y$  are determined as well as the pinching factor  $\alpha_p$  is specified, the hysteretic model for beam elements is established. Table 3-III summarizes the hysteretic model for all the elements of the structure.

The Rayleigh damping is used in this study, which is the combination of the mass and stiffness matrices of the structure, as described by Eq. 2.2. The mass matrix can be constructed from the individual mass values listed in Table 3-I. The stiffness matrix of the structure is formed by assembling the appropriate element initial stiffness given in Table 3-III. From the free vibration analysis of this structural system, the natural frequencies of the first two modes are 8.680 rad/sec and 25.274 rad/sec, respectively. Assuming the critical damping ratio of 4% for these two modes, the coefficients of damping matrix,  $a_0$  and  $a_1$  (Eq. 2.3), are computed as 0.5168 and 0.002356, respectively.

**Table 3-II Representative Values of Structural Parameters**

Structural Parameter	Representative Values
Critical Damping Ratio $\zeta$	0.02, 0.04, 0.06
Stiffness Ratio $\alpha_g$	0.10, 0.17, 0.25
Post-yielding Slope Factor $\alpha_s$	0.01, 0.03, 0.05
Yielding Shear Strain $\gamma_y$	0.002, 0.0025, 0.003

**Table 3-III Values of Hysteretic Model**

Element No.	Uncracked Stiffness $k_0$ (kips/in)	Initial Stiffness $k_e$ (kips/in)	Post-Yielding Stiffness $k_p$ (kips/in)	Yielding Displacement $U_y$ (in)	Pinching Factor $\alpha_p$
5	11674	1985	60	0.312	0.3
4	11674	1985	60	0.312	0.3
3	11674	1985	60	0.312	0.3
2	11591	1970	59	0.312	0.3
1	10045	1708	51	0.360	0.3

### 3.5 Ensemble of Earthquake Time Histories

The earthquake ground motion used in this study is represented by an ensemble of artificial acceleration time histories generated from Kanai-Tajimi (K-T) power spectra. For each power spectrum, two parameters, i.e.,  $\omega_g$  and  $\zeta_g$  need to be determined. These parameters are dependent on the site soil conditions. The statistics of  $\omega_g$  and  $\zeta_g$  for different soil conditions has been reported in several studies [13-15]. Typically, for sites with soft soil condition,  $\omega_g$  is estimated in the range of  $2.4\pi$  to  $3.5\pi$  [14, 15], whereas for rock sites,  $\omega_g$  is ranging from  $8\pi$  to  $10\pi$  [15, 29]. Furthermore, for the stiff soil condition,  $\omega_g$  is between the values estimated for rock and soft soils. The general soil conditions ranging from soft soil to rock type are reported in the metropolitan area near New York City, where the shear wall structure is assumed to be located. Thus, three values of  $\omega_g$ , namely,  $3\pi$ ,  $6\pi$  and  $9\pi$  are selected as representative values. For the value of  $\zeta_g$ , it is estimated that the mean value is about 0.6 and coefficient of variation (*COV*) is about 0.4 [13, 15]. Thus, three values of  $\zeta_g$ , i.e. 0.6, 0.36 and 0.84 are chosen. These values are corresponding to mean, mean minus and plus one standard deviation of  $\zeta_g$ . Another parameter in the description of earthquake ground motion is the strong motion duration. Based on the statistics of strong motion duration presented in Refs. 13 and 14, three values of strong motion duration, namely 5, 10, and 15 seconds are chosen as representative values in the present study. The values of ground motion parameters used in this study are listed in Table 3-IV.

From the combinations of three values of  $\omega_g$  and  $\zeta_g$ , nine power spectra are obtained. Figure 3-3 shows a power spectrum with  $\omega_g$  of  $6\pi$  and  $\zeta_g$  of 0.36. For each power spectrum, three stationary time histories are generated by utilizing Eq. 2.4. Thus, 27 stationary time histories are produced. It is noted that 27 different sets of random phase angles are used to generate these time histories. An envelope function is applied to a stationary time history to generate a nonstationary ground acceleration (Eq. 2.6). The envelope function used in this study is a trapezoidal shape as illustrated in Fig. 3-4. The rise and decay time of the envelope function are taken as 2.5 seconds. The strong motion duration, which is the time between rise and decay time, is treated as random and three representative values are given in Table 3-IV. By applying the three envelope functions mentioned above to each stationary time history, three normalized nonstationary time histories are generated. Thus, for this study, 81 normalized earthquake acceleration time histories are generated. A sample of generated acceleration time histories is plotted in Fig. 3-5. Using the Latin hypercube

**Table 3-IV Representative Values of Ground Motion Parameters**

Ground Motion Parameter	Representative Values
$\omega_g$ (rad/sec)	$3\pi, 6\pi, 9\pi$
$\zeta_g$	0.36, 0.60, 0.84
Strong Motion Duration (sec)	5, 10, 15

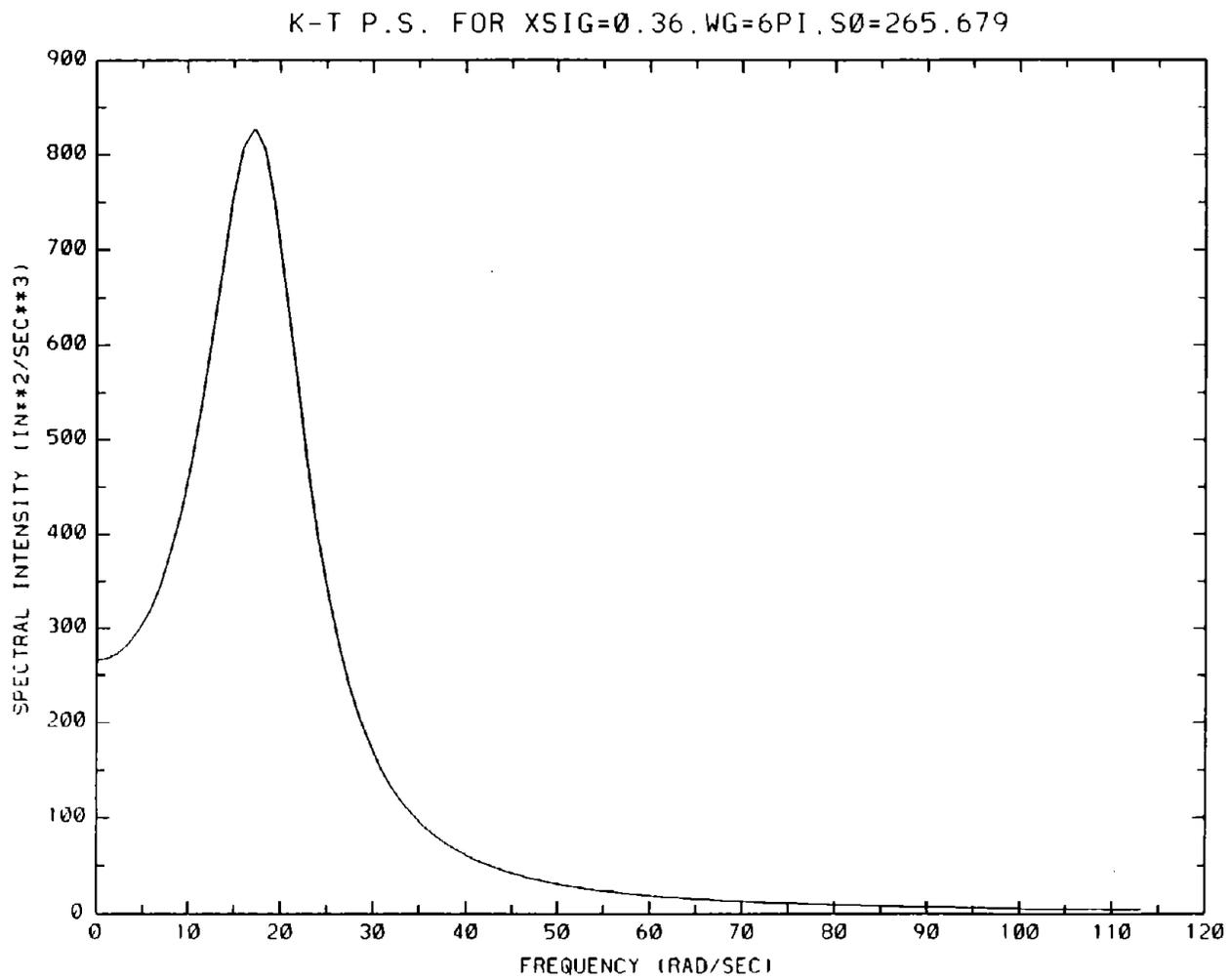


Fig. 3-3 An Example of Power Spectrum

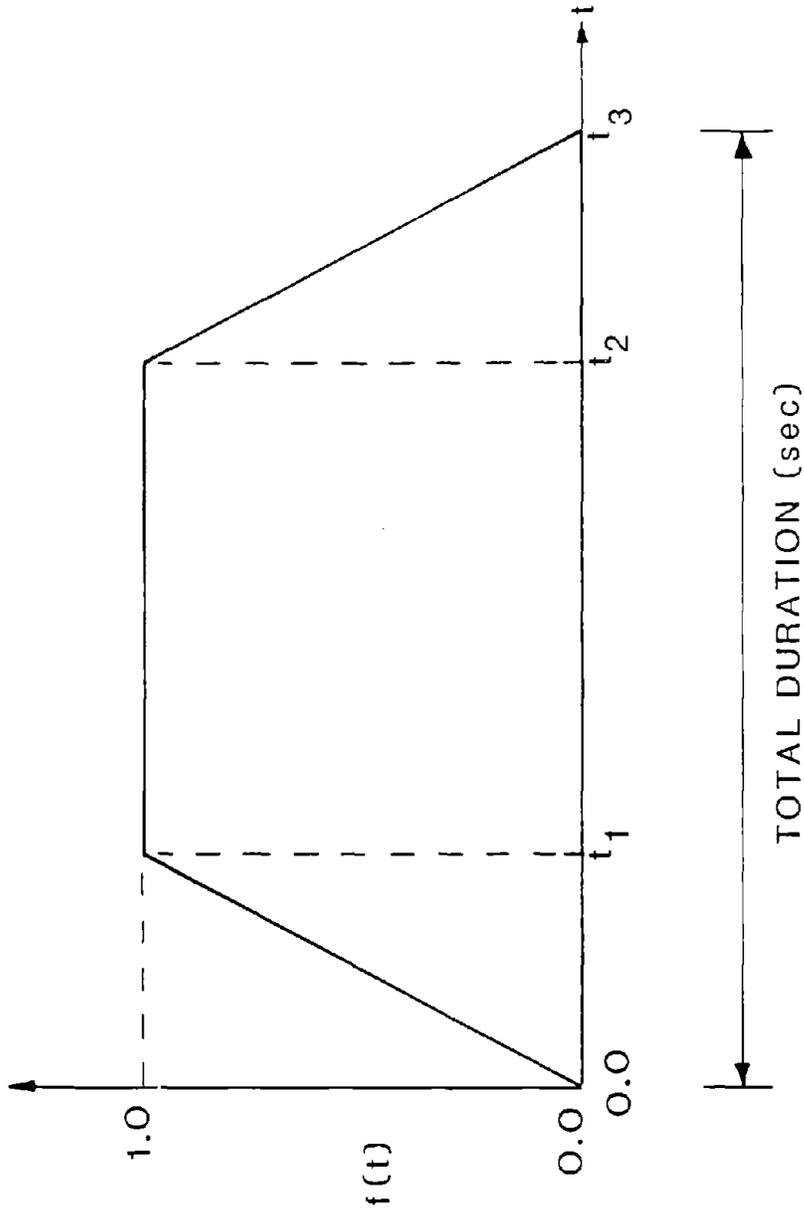


Fig. 3-4 Envelope Function

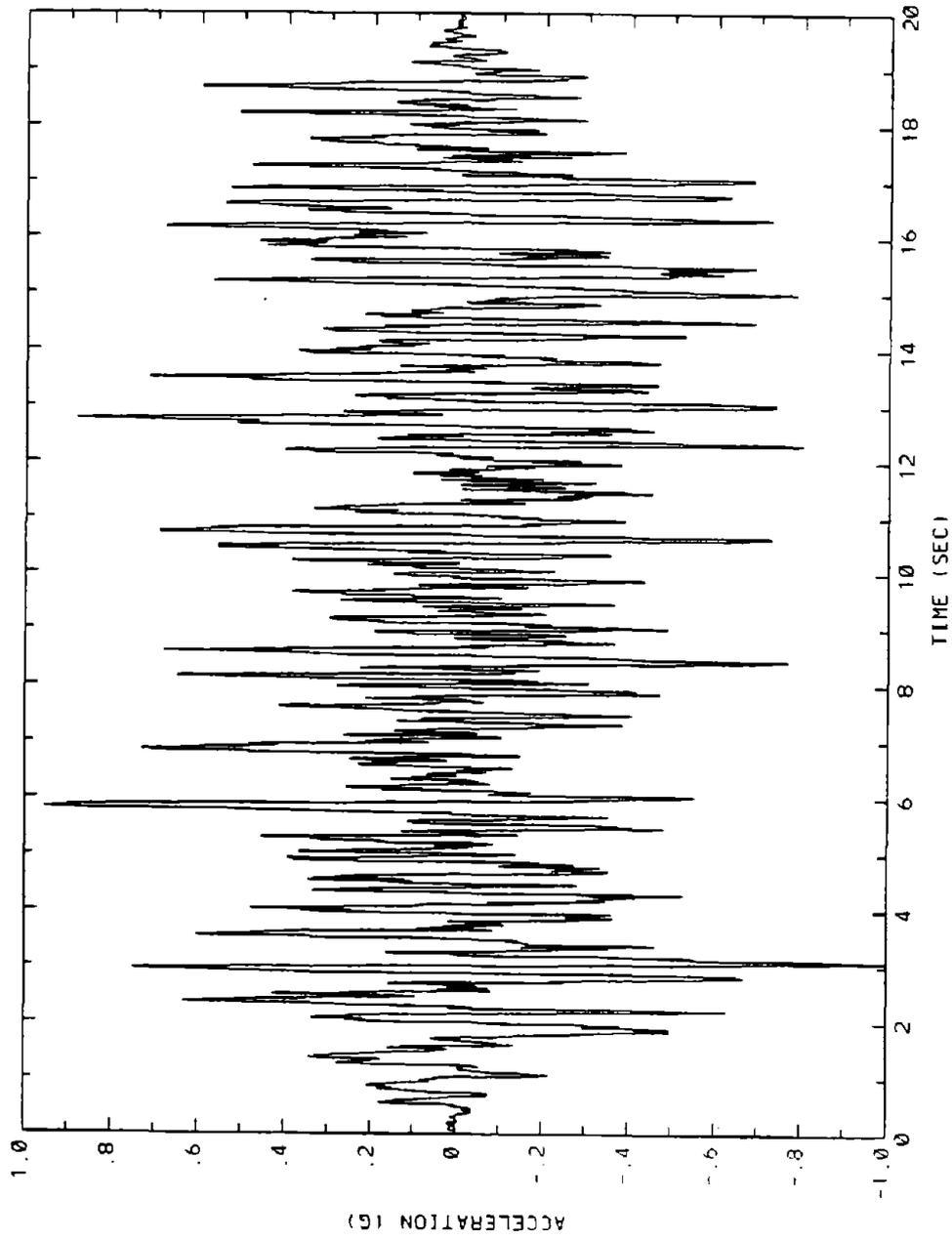


Fig. 3-5 A Sample of Earthquake Time Histories

sampling technique, these earthquake time histories are then matched to the structural models so that 81 samples of the earthquake load-structure system are constructed for seismic response analyses.

### 3.6 Statistical Analysis of Responses

For a specified PGA level, nonlinear time history analysis is performed for each sample of earthquake load-structure system to evaluate required structural responses. In this study, the maximum ductility ratio is chosen to represent structural responses. Thus, 81 maximum ductility ratios are obtained and then statistically analyzed to evaluate sample mean and sample *COV*. The 81 samples are also plotted in the probability papers for the lognormal and the extreme Type I distributions. Figures 3-6 and 3-7 show the plots of probability papers with sample data obtained from PGA equal to 0.2*g*. From these figures, it can be seen that both distributions fit the data reasonably well. Thus, both lognormal and extreme Type I distributions are utilized to describe the distribution of structural responses. The parameters of the extreme Type I distribution are  $\alpha$  and  $u$ . For the lognormal distribution, the median  $\bar{\mu}_E$  and logarithmic standard deviation  $\beta_E$  are the parameters of the distribution. The parameters of these two distributions can be determined from the sample mean and the sample *COV* [20]. For the purpose of constructing fragility curve for the structure, the structural responses corresponding to various levels of PGA need to be evaluated. In this study, 6 levels of PGA ranging from 0.045*g* to 0.6*g* are used. Table 3-V summarizes the statistics of maximum ductility ratios and the parameters of two distributions for all levels of PGA considered.

### 3.7 Structural Capacity

In the present study, five limit states representing nonstructural damage, slight structural damage, moderate structural damage, severe structural damage, and collapse are established to characterize the degree of damage incurred in buildings during earthquakes. The ductility capacity  $\mu_R$  associated with a particular limit state is assumed to be lognormal distributed. For the limit state corresponding to collapse of the structure, the median capacity  $\bar{\mu}_R$  and the logarithmic standard deviation  $\beta_R$  are determined from analyzing test data of shear wall specimens [30]. The values of  $\bar{\mu}_R$  and  $\beta_R$  for the other four limit states are assigned based on engineering judgement. Values of  $\bar{\mu}_R$  and  $\beta_R$  for five limit states are given in Table 3-VI.

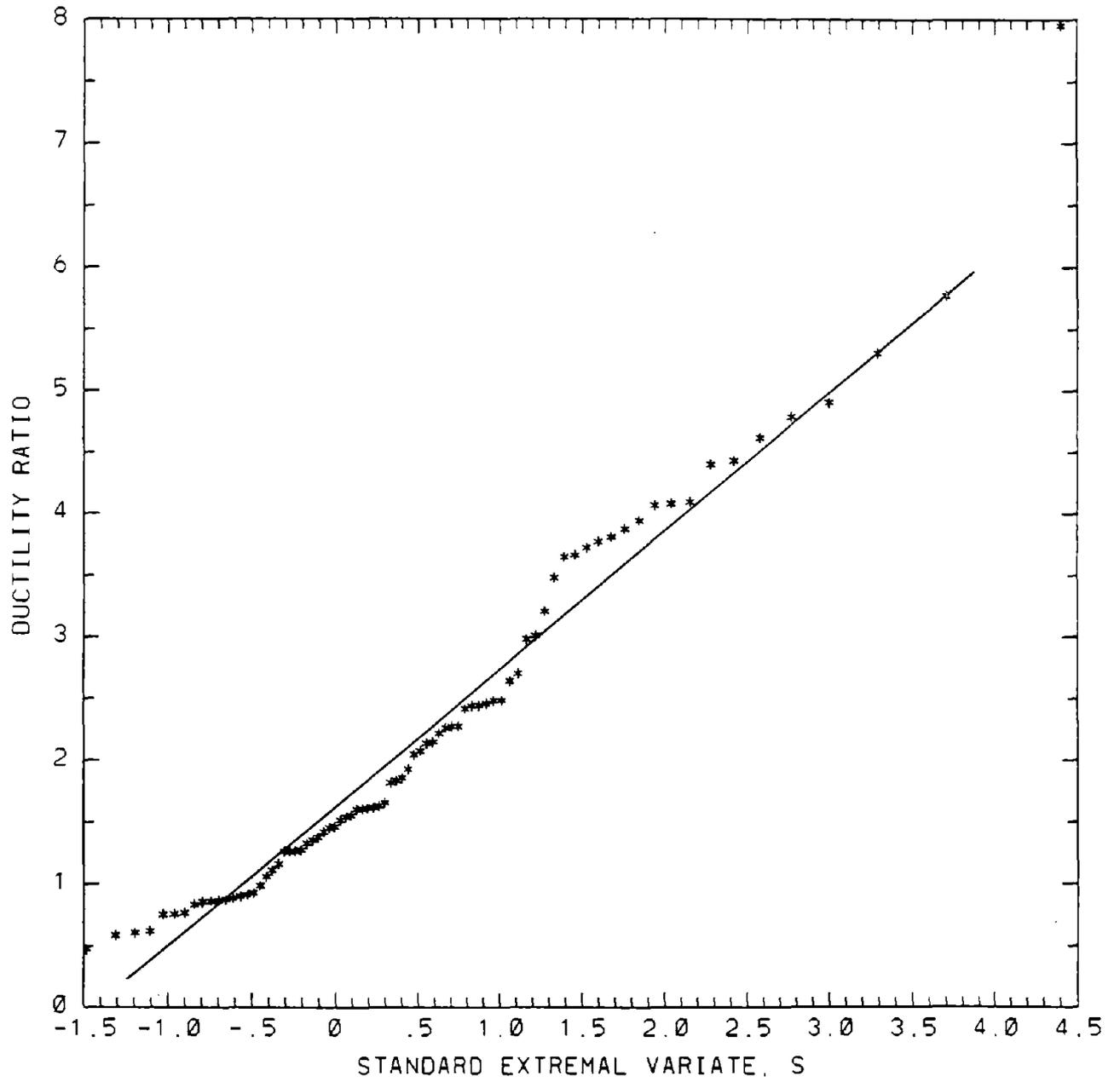


Fig. 3-6 Distribution of Maximum Ductility Ratios (Extreme Type I)

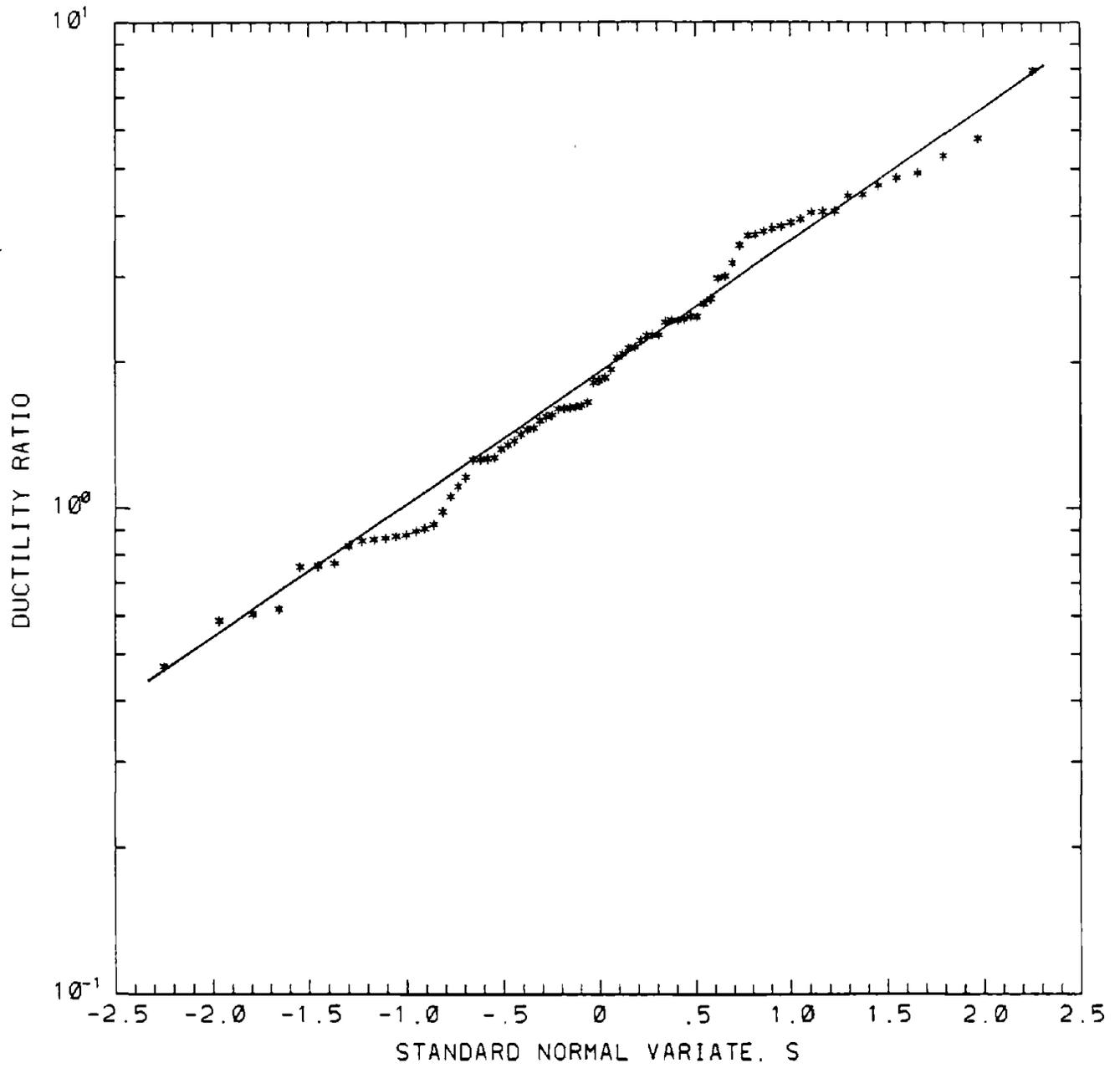


Fig. 3-7 Distribution of Maximum Ductility Ratios (Lognormal)

**Table 3-V Statistics of Maximum Ductility Ratios**

PGA (g)	Mean	COV	Extreme Type I		Lognormal	
			$\alpha$	$u$	$\bar{\mu}_E$	$\beta_E$
0.045	0.408	0.51	6.154	0.314	0.363	0.48
0.075	0.701	0.56	3.250	0.524	0.611	0.52
0.1	0.983	0.63	2.084	0.706	0.833	0.58
0.2	2.259	0.64	0.889	1.609	1.903	0.58
0.4	6.688	0.76	0.253	4.409	5.332	0.67
0.6	12.374	0.69	0.150	8.525	10.179	0.62

**Table 3-VI Ductility Capacity**

Limit State	$\bar{\mu}_R$	$\beta_R$
Nonstructural Damage	1.0	0.3
Slight Structural Damage	2.0	0.3
Moderate Structural Damage	4.0	0.3
Severe Structural Damage	6.0	0.3
Collapse	7.5	0.3

### 3.8 Fragility Evaluation

The fragility curve for the structure is the limit state probabilities with respect to a particular limit state at various levels of PGA. The limit state probability for a particular limit state and a specified level of PGA is evaluated from Eq. 2.11. This procedure is carried out for all five limit states and different levels of PGA. For the case (Case I) that the structural responses are described by the extreme Type I distribution, the fragility data are tabulated in Table 3-VII, and fragility curves are plotted in Figs. 3-8 and 3-9. As shown in Fig. 3-8, the fragility data are plotted on semi-logarithmic scale so that the lower tails of the fragility curves can be displayed. Conventionally, the fragility data are displayed on an arithmetic plot as shown in Fig. 3-9 in which the fragility data at higher accelerations are clearly depicted. For the case (Case II) that the structural responses are described by the lognormal distribution, the fragility data are shown in Table 3-VIII and plotted in Fig 3-10. On the basis of these fragility data, several observations are discussed as follows:

- (1) For a specified limit state under consideration, the limit state probability generally increases as the PGA value increases. From Table 3-VII, for example, the probability that the shear wall structure may incur moderate structural damage is about  $2.50 \times 10^{-6}$  for PGA of  $0.045g$ , while it reaches  $5.63 \times 10^{-3}$  for PGA of  $0.1g$ .
- (2) At a particular PGA level, the probability that the structure will damage decreases with the increasing severity of damage level. For instance, at the peak ground acceleration of  $0.1g$ , the probability of the shear wall building incurring different degrees of damage is in the range of 0.42 (nonstructural damage) to  $9.31 \times 10^{-5}$  (collapse). Thus, the fragility data, such as those shown in Table 3-VII, depict the likelihood that shear wall structures will sustain various degrees of damage at each level of ground shaking induced by earthquakes.
- (3) From the fragility data shown in Tables 3-VII and 3-VIII, it is observed that the structure suffers minor damage under small earthquakes and severe damage under larger earthquakes.
- (4) The extreme Type I and lognormal distributions are utilized to describe the structural responses. The fragility data obtained from the use of these two distributions

**Table 3-VII Fragility Data (Case I)**

Limit State	Peak Ground Acceleration (g)					
	0.045	0.075	0.1	0.2	0.4	0.6
Nonstructural Damage	3.65 E-2	0.22	0.42	0.80	0.90	0.95
Slight Structural Damage	8.51 E-4	2.32 E-2	9.53 E-2	0.50	0.83	0.93
Moderate Structural Damage	2.50 E-6	4.63 E-4	5.63 E-3	0.14	0.65	0.85
Severe Structural Damage	2.61 E-8	1.83 E-5	4.83 E-4	4.00 E-2	0.48	0.75
Collapse	1.40 E-9	2.19 E-6	9.31 E-5	1.60 E-2	0.37	0.67

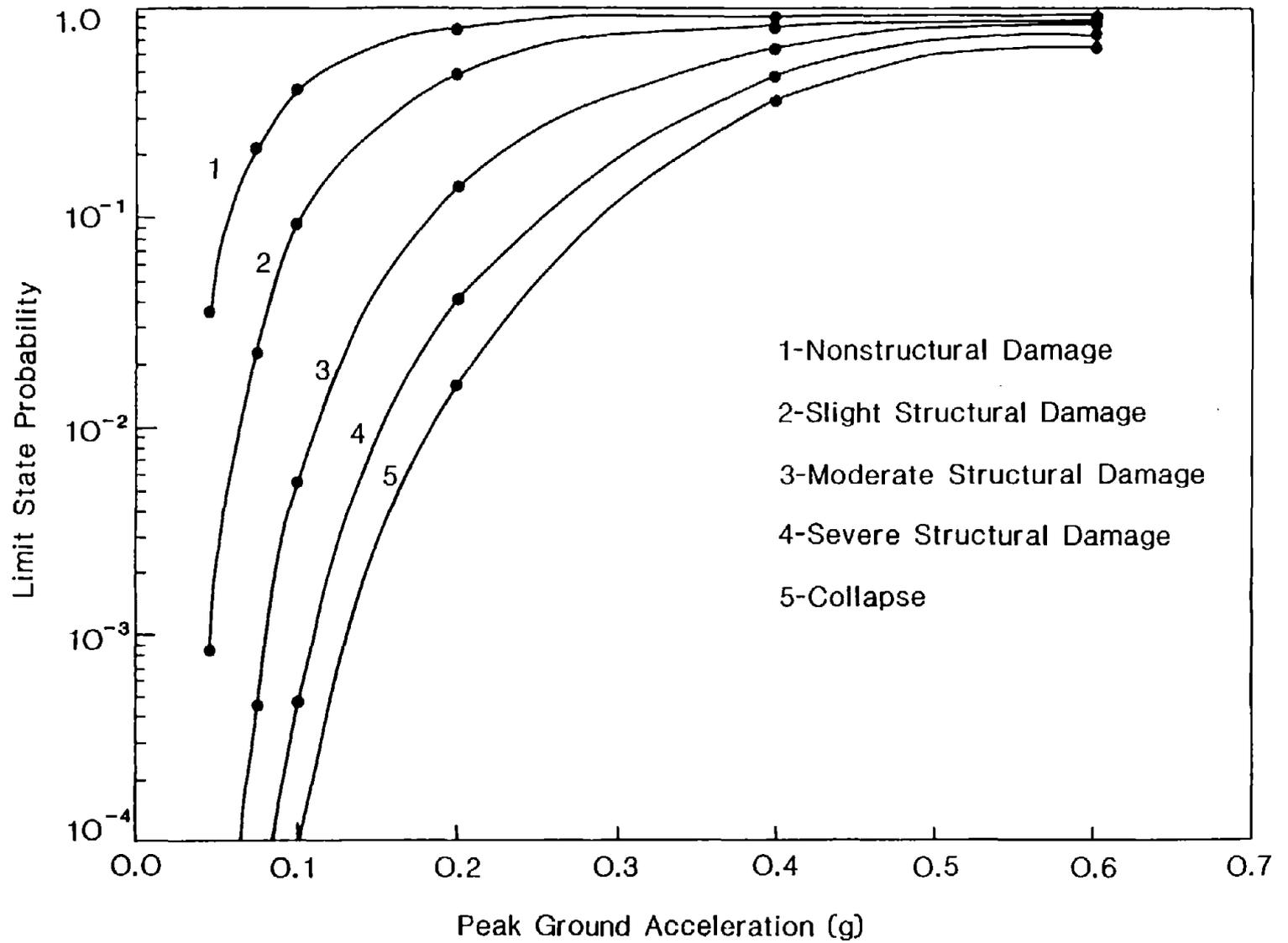


Fig. 3-8 Fragility Curves (Case I, Semi-Log Scale)

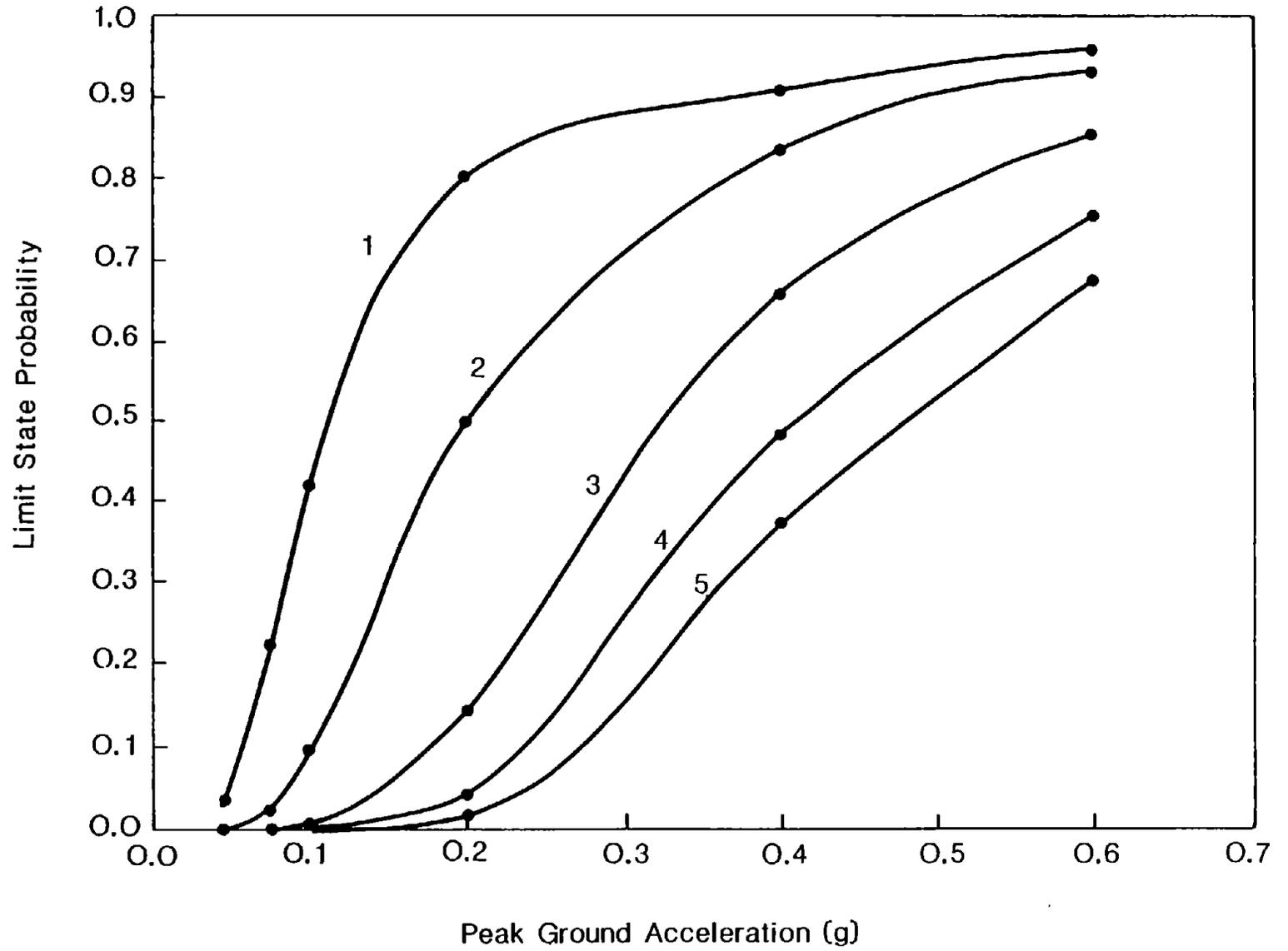


Fig. 3-9 Fragility Curves (Case I, Arithmetic Scale)

**Table 3-VIII Fragility Data (Case II)**

Limit State	Peak Ground Acceleration (g)					
	0.045	0.075	0.1	0.2	0.4	0.6
Nonstructural Damage	3.71 E-2	0.21	0.39	0.84	0.99	1.0
Slight Structural Damage	1.32 E-3	2.49 E-2	8.85 E-2	0.47	0.91	0.99
Moderate Structural Damage	1.18 E-5	9.38 E-4	7.79 E-3	0.13	0.65	0.91
Severe Structural Damage	3.86 E-7	7.84 E-5	1.17 E-3	4.04 E-2	0.44	0.78
Collapse	4.76 E-8	1.67 E-5	3.52 E-4	1.85 E-2	0.32	0.67

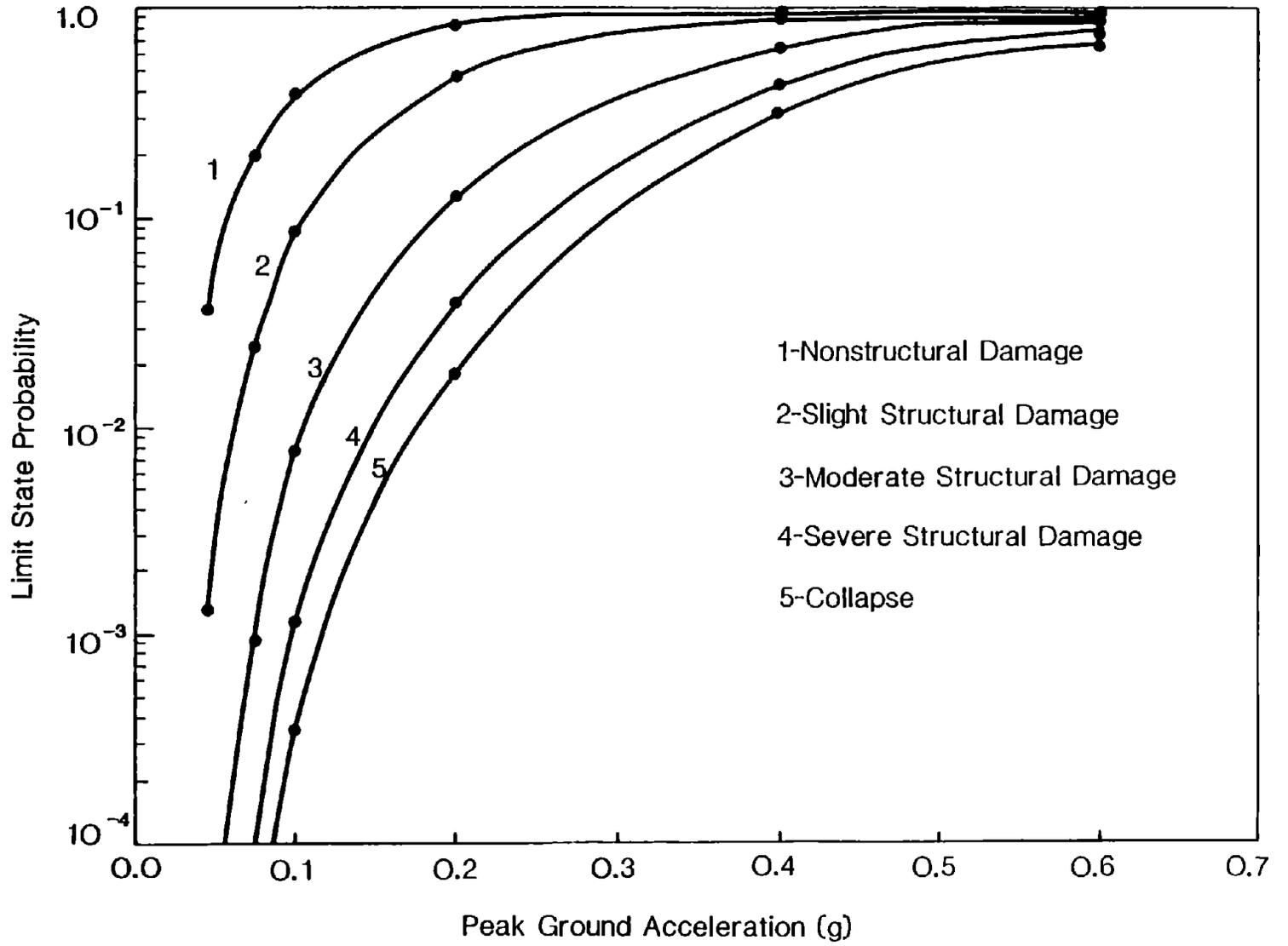


Fig. 3-10 Fragility Curves (Case II)

are shown in Tables 3-VII and 3-VIII, respectively. From these two tables, it is clearly indicated that the limit state probabilities are compatible with each other.

- (5) In order to ensure the safety of structures, the conservatism is built in at each step of the design process. As a result, the actual structural capacity is usually larger than the design capacity, however, the actual capacity is unknown to the engineers. For the practical purpose, engineers are interested in the minimum actual capacity. It is recommended that the minimum actual capacity with respect to a specified limit state is set as the PGA value with the limit state probability of one percent. This minimum capacity is equivalent to the HCLPF value used in the margin studies for nuclear structures [2]. For the moderate damage limit state, the minimum capacity of the shear wall structure considered in this study is estimated as  $0.113g$ . This means that if an  $0.1g$  earthquake occurs, the engineers are sure that the structure will not sustain any moderate damage. Furthermore, the minimum safety factor can be defined as the ratio of the minimum actual capacity in terms of PGA level to the design peak ground acceleration. Since the structure is designed for about  $0.045g$  [21], the minimum safety factor for this shear wall structure is about 2.5 against moderate damage due to  $0.1g$  earthquakes.

## SECTION 4 CONCLUSIONS

This report presents a fragility analysis method for the generation of seismic fragility curves for structures, in particular, shear wall structures. The important features of the proposed method are as follows

- (1) Uncertainties including randomness and modeling uncertainty in earthquake ground motion and structure are quantified by evaluating uncertainties in pertinent parameters which define the analytical model of the earthquake load-structure system. The advantage of this approach is that the assessment of uncertainty can be easily verified independently. As a result, the fragility data are more reliable.
  
- (2) The nonlinear structural response is explicitly included in the fragility estimation by using the Latin hypercube sampling technique and appropriate hysteretic model. The utilization of the Latin hypercube sampling technique makes the probabilistic nonlinear time history analysis economic and feasible.

The fragility curves generated by the proposed method can be utilized in the seismic risk study to determine potential earthquake-induced loss of life and damage of properties, then the economic and societal risk can be estimated. In addition, the fragility data can be used by the authority to develop emergency response plan.



**SECTION 5**  
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16. Abstract (Limit: 200 words) This report presents a fragility analysis method to generate seismic fragility curves for shear wall structures. Uncertainties including randomness and modeling uncertainty in earthquake ground motion and structure are quantified by evaluating uncertainties in pertinent parameters which define earthquake load-structure system. The uncertainty in each parameter is characterized by several representative values to construct samples of earthquake load-structure system, and then the Latin hypercube sampling technique is utilized to combine these values to construct samples of earthquake load-structure system. For the response analysis, the modified Takeda hysteretic model is utilized to describe the nonlinear structural behavior. The nonlinear seismic analyses are performed in time domain for all samples of earthquake load-structure system to obtain an ensemble of structural responses, which are then statistically analyzed. Five limit states representing various degrees of structural damage due to earthquake are established. Then, the statistics of the structural capacity corresponding to each limit state probability is evaluated on the basis of statistics of response and capacity for each limit state. The fragility curve is generated by evaluating the limit state probabilities at different levels of peak ground acceleration.			
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