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**EVALUATION OF SEISMIC DAMAGE INDICES FOR  
REINFORCED CONCRETE STRUCTURES**

by

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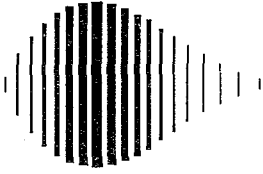
Abstract: The report presents some new information about the correlation between various local and global damage indices and the damage level. The information is obtained by analyzing the results of numerical simulations of the seismic response of three code-designed reinforced concrete frames subjected to a set of artificially generated and recorded earthquakes. The results were computed by using an improved version of the computer code SARCF-II (Seismic Analysis of Reinforced Concrete Frames-Version II). The new version is tested by comparing computed results to experimental ones obtained from a reinforced concrete model tested at the University of Illinois at Urbana-Champaign. The maximum softening as a global damage index is compared to weighted averages of local damage indices and to traditional measures of damage such as the maximum interstory drift, the permanent interstory drift and the maximum ductility ratio for beams and columns. The maximum softening index is also compared to the final softening one. The global softening indices are helpful for identifying structures that need careful

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## PREFACE

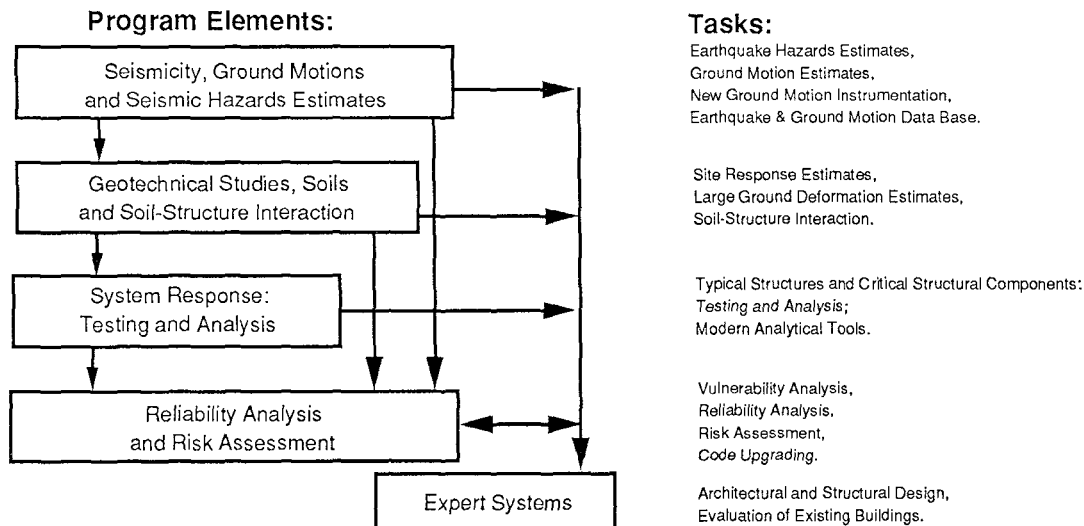
The National Center for Earthquake Engineering Research (NCEER) is devoted to the expansion and dissemination of knowledge about earthquakes, the improvement of earthquake-resistant design, and the implementation of seismic hazard mitigation procedures to minimize loss of lives and property. The emphasis is on structures and lifelines that are found in zones of moderate to high seismicity throughout the United States.

NCEER's research is being carried out in an integrated and coordinated manner following a structured program. The current research program comprises four main areas:

- Existing and New Structures
- Secondary and Protective Systems
- Lifeline Systems
- Disaster Research and Planning

This technical report pertains to Program 1, Existing and New Structures, and more specifically to reliability analysis and risk assessment.

The long term goal of research in Existing and New Structures is to develop seismic hazard mitigation procedures through rational probabilistic risk assessment for damage or collapse of structures, mainly existing buildings, in regions of moderate to high seismicity. This work relies on improved definitions of seismicity and site response, experimental and analytical evaluations of systems response, and more accurate assessment of risk factors. This technology will be incorporated in expert systems tools and improved code formats for existing and new structures. Methods of retrofit will also be developed. When this work is completed, it should be possible to characterize and quantify societal impact of seismic risk in various geographical regions and large municipalities. Toward this goal, the program has been divided into five components, as shown in the figure below:



Reliability analysis and risk assessment research constitutes one of the important areas of Existing and New Structures. Current research addresses, among others, the following issues:

1. Code issues - Development of a probabilistic procedure to determine load and resistance factors. Load Resistance Factor Design (LRFD) includes the investigation of wind vs. seismic issues, and of estimating design seismic loads for areas of moderate to high seismicity.
2. Response modification factors - Evaluation of RMFs for buildings and bridges which combine the effect of shear and bending.
3. Seismic damage - Development of damage estimation procedures which include a global and local damage index, and damage control by design; and development of computer codes for identification of the degree of building damage and automated damage-based design procedures.
4. Seismic reliability analysis of building structures - Development of procedures to evaluate the seismic safety of buildings which includes limit states corresponding to serviceability and collapse.
5. Retrofit procedures and restoration strategies.
6. Risk assessment and societal impact.

Research projects concerned with reliability analysis and risk assessment are carried out to provide practical tools for engineers to assess seismic risk to structures for the ultimate purpose of mitigating societal impact.

*This report presents new information about the correlation between various local and global damage indices, and the damage level. This information is obtained by analyzing the results of numerical simulations of the seismic response of reinforced concrete frames. The Maximum Softening as a global damage index is compared to weighted averages of local damage indices and to traditional measures of damage such as the maximum interstory drift, the permanent interstory drift and the maximum ductility ratio for beams and columns. The Maximum Softening is also compared to the Final Softening. These different measures of damage are herein evaluated.*



## ABSTRACT

This report presents some new information about the correlation between various local and global damage indices, and the damage level. This information is obtained by analyzing the results of numerical simulations of the seismic response of reinforced concrete frames.

The seismic response of three code-designed reinforced concrete frames subjected to a set of artificially generated and recorded earthquakes is computed by using an improved version of the computer code SARCF-II, described herein. This new version is tested by comparing computed results to experimental ones obtained from a reinforced concrete model tested at the University of Illinois at Urbana-Champaign.

The Maximum Softening as a global damage index is compared to weighted averages of local damage indices and to *traditional measures of damage* such as the maximum interstory drift, the permanent interstory drift and the maximum ductility ratio for beams and columns. This Maximum Softening index is also compared to the Final Softening one.

These discussed global softening indices are helpful for identifying structures that need careful inspection after an earthquake and are applicable to reinforced concrete structures with/without shear walls.



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# SECTION 1

## INTRODUCTION

### 1.1 Statement of the Problem

In the current practice of earthquake engineering, reinforced concrete structures are designed in such a way that only minor to moderate earthquakes can be withstood within the elastic range. The safeguard against large earthquakes relies on the inelastic response of the structural elements, which provides a mechanism for the dissipation of the earthquake energy. When the inelastic response takes place, the seismic forces are considerably reduced compared to the internal forces that an elastic structure would sustain. This is considered in the structural design practice by the use of a Response Modification Factor. Thus, it is important to know which is the degree of damage for structures that undergo inelastic deformations and dissipate the earthquake energy.

In the classical structural design for static loads, the structural safety is attained by keeping the stresses well below the material yield limit. This simple definition of safety is too conservative for the evaluation of the state of a structural system after earthquakes. Even moderate earthquakes may produce yielding in some of the structural members without producing a dangerous situation. Since the beginning stages of the earthquake engineering practice, both the expected performance of structures subjected to earthquakes, and the state of damage after actual seismic events have been characterized using indicators other than the stress level. The width and distribution of cracks, the interstory or global drift and the ductility ratio have been used as *traditional* or *engineering* measures of seismic damage. On the other hand, many local and global damage indices have been created as an indication of the remaining capacity after earthquakes.

The objective of this report is to evaluate and compare the traditional measures of seismic damage and the available local and global damage indices, studying their relationship

and correlation. These measures of damage can be used in three main fields: after earthquake evaluation of damaged structures, performance prediction in the design stage, and reliability studies of existing facilities.

This evaluation has to be done by means of numerical simulations, due to the scarcity of experimental data and because this is the only option available for the computation of some of the damage indices that have been considered. The response of several building frames subjected to a set of artificially generated and recorded earthquakes has been obtained by using the computer code SARCF-II. Then the damage indices were computed. This report presents the results of these numerical simulations and analyzes the resulting database in order to draw conclusions about the correlation between different damage indices and their applicability. In particular, two different damage indices, Maximum Softening and Final Softening as defined by DiPasquale and Cakmak [10] are discussed in some details. These global softening indices are helpful for identifying structures that need careful inspection after an earthquake and they are applicable to reinforced concrete structures with/without shear walls.

## **1.2 Organization of the Work**

The local and global damage indices that have been utilized are described in Section 2. It is also explained how the damage indices are computed. A new way of computing the global damage index defined by DiPasquale and Cakmak [10] from the instantaneous natural period is presented.

The computer code SARCF-II, used to simulate the seismic response of the building frames, is introduced in Section 3. The modifications to this program, carried out for the purpose of making possible this research, are also described. The computer program SARCF-II has been validated by comparing its results to the experimental results on a reinforced concrete model tested at the University of Illinois at Urbana-Champaign

(UIUC) by Sozen and his associates [5]. SARCF-II has also been compared to another similar program, IDARC, developed at State University of New York at Buffalo by Y. J. Park *et al.* [18].

Section 4 is devoted to the numerical simulations that have been carried out. A description of the building frames and input ground motions is included.

Section 5 presents an analysis of the results obtained. First, the two available procedures for the computation of the Maximum Softening are compared. Secondly, the Maximum Softening as a global damage index, is compared to the traditional measures of damage and to the weighted averages of the local damage indices.

The final conclusions are included in Section 6.



## SECTION 2

### LOCAL AND GLOBAL DAMAGE INDICES

Many damage models have been proposed to characterize the state of reinforced concrete structures after earthquakes. A very extensive review of the different definitions of damage indices was made by Chung *et al.* [6]. They divided the damage indices for reinforced concrete into three different groups: empirical damage definitions, normalized dissipated energy indices, and damage indices developed for reinforced concrete structures on the basis of theoretical principles.

Another review of the methods to quantify seismic damage can be found in Reference [9]. Most of the definitions for damage consider the damage of simple elements and are based on the ductility ratio or on dissipated energy. Global damage indices that give information about the state of complex structural systems are usually defined as a weighted average of the local damage in the simple structural elements that form the system. A different approach for the definition of global damage indices was proposed by DiPasquale and Cakmak [9]. They base their global damage indices on the vibrational parameters of the structure.

In this section, the local and global damage indices utilized in this report will be described.

#### 2.1 Local Damage Indices

Two of the most recent definitions of local damage indices have been used, the one proposed by Chung, Meyer and Shinozuka [6], and the definition by Park and Ang [15] with the modifications described below.

### 2.1.1 Chung, Meyer and Shinozuka's Local Damage Index

Chung, Meyer and Shinozuka's local damage index combines a modified version of Miner's Hypothesis with damage acceleration factors that reflect the effect of the loading history. In Reference [6] it is defined as

$$D_e = \sum_i \left( \alpha_i^+ \frac{n_i^+}{N_i^+} + \alpha_i^- \frac{n_i^-}{N_i^-} \right) \quad (2.1)$$

where

$i$  : indicator of different displacement or curvature levels

$N_i = \frac{M_i - M_{fi}}{\Delta M_i}$  : number of cycles up to curvature level  $i$  to cause failure

$\Delta M_i$  : strength drop in one load cycle up to curvature level  $i$ , figure 2 – 1.

$n_i$  : number of cycles up to curvature level  $i$  actually applied

$\alpha_i$  : damage modifier

+, – : indicator of loading sense

The effect of the loading history is captured by introducing the damage modifier ,  $\alpha_i$ , which for positive moment loading, is defined as

$$\alpha_i^+ = \frac{\frac{1}{n_i^+} \sum_{j=1}^{n_i^+} k_{ij}^+}{\bar{k}_i^+} \cdot \frac{\phi_i^+ + \phi_{i-1}^+}{2\phi_i^+} \quad (2.2)$$

where

$$k_{ij}^+ = \frac{M_{ij}^+}{\phi_i^+} \quad (2.3)$$

is the stiffness during the  $j$ -th cycle up to load level  $i$  and,

$$\bar{k}_i^+ = \frac{1}{N_i^+} \sum_{j=1}^{N_i^+} k_{ij}^+ \quad (2.4)$$

is the average stiffness during  $N_i^+$  cycles up to load level  $i$ .



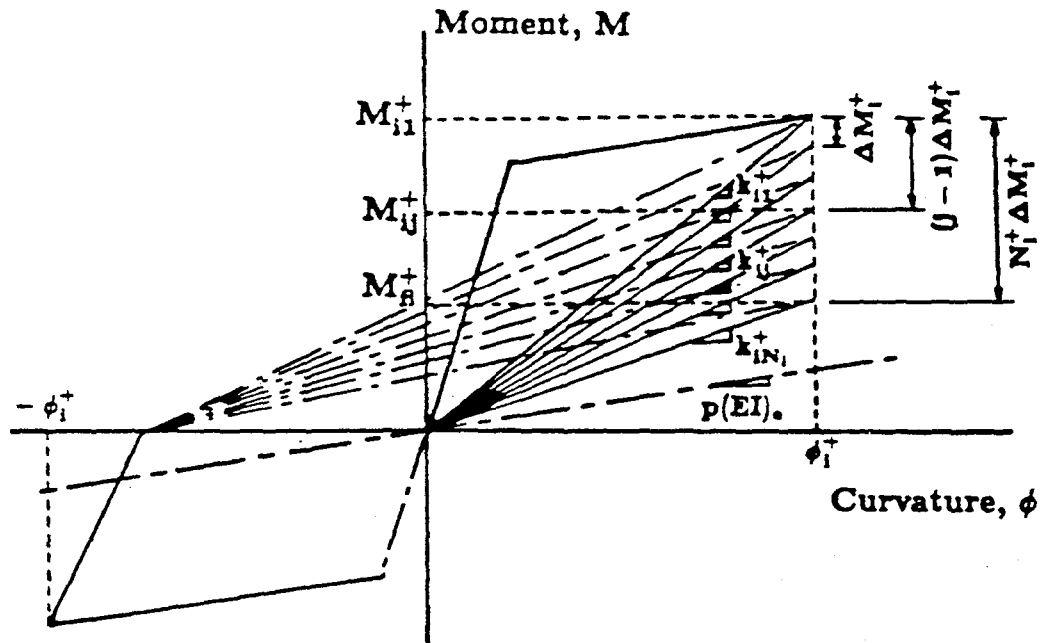


FIGURE 2-1 Strength Drop Due to Cycling Loading [7]

### 2.1.2 Park and Ang's Local Damage Index

Park and Ang's local damage index includes two terms that reflect the influence of the maximum deformation and the absorbed hysteresis energy [15]

$$D = \frac{\delta_m}{\delta_u} + \frac{\beta}{\delta_u P_y} \int dE \quad (2.5)$$

where,

$\delta_m$  : Maximum deformation

$\delta_u$  : Ultimate deformation under monotonic loading

$P_y$  : Yield strength

$dE$  : Dissipated energy increment

The strength deterioration parameter  $\beta$  has to be found experimentally. According to Y. J. Park *et al.* [18]  $\beta$  was found using a regression equation obtained from experimental results with 400 reinforced concrete columns and beams. The values of  $\beta$  for the usual reinforced concrete sections are small. In the example of Appendix B of Reference [18] the greatest value of  $\beta$  is 0.06. In Reference [17] Y. J. Park *et al.* established that the value of  $\beta$  is of the order of 0.05 for reinforced concrete members. Since the second term of Equation (2.5) is a normalized term always smaller than one, it can be neglected for practical purposes, given the small value of  $\beta$ .

The displacement and the ultimate displacement of Equation (2.5) are clearly defined only for the case of a cantilever beam fixed at one end. The computation of  $\delta_m$  and  $\delta_u$  for the case of beams or columns, for which bending moments, shear and axial forces are considered, is not well defined. When the structural damage is due to bending, it seems more appropriate to substitute curvature for displacement in the first term of Equation (2.5).

A modified Park and Ang's Damage Index based on curvature instead of displacement neglecting the energy term is given by:

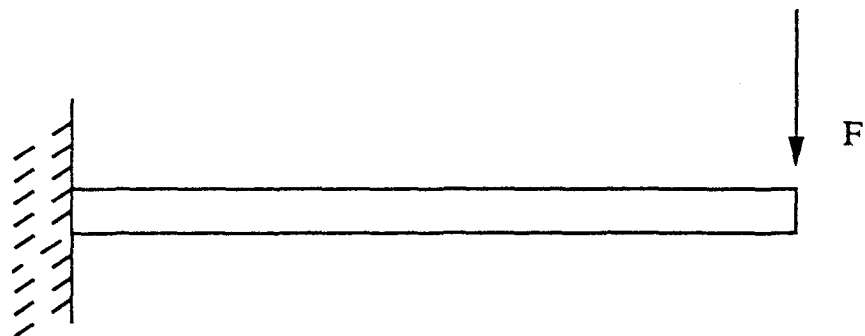
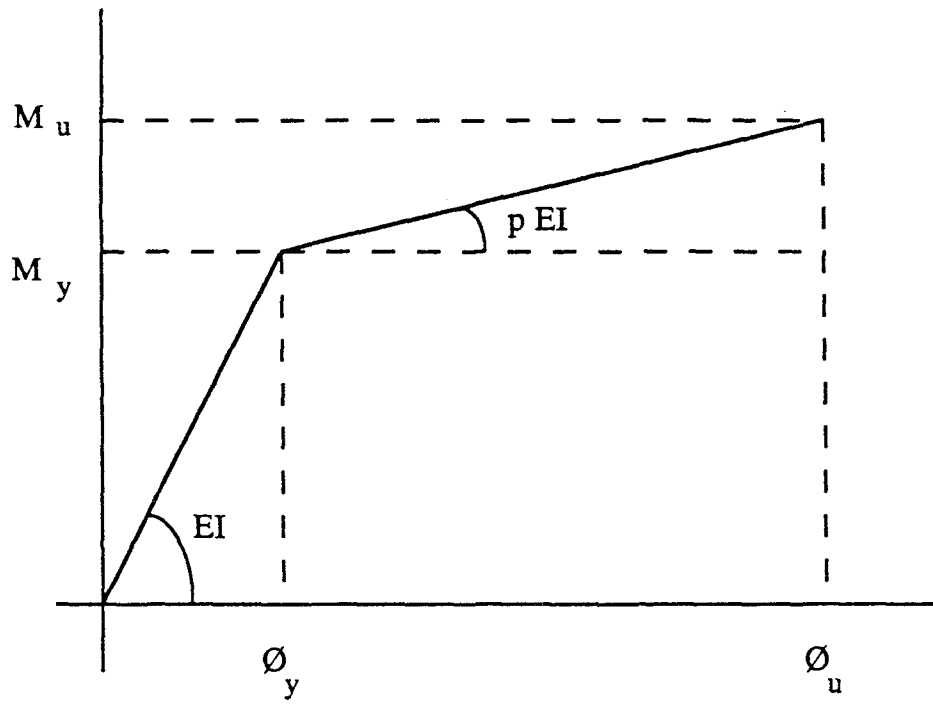
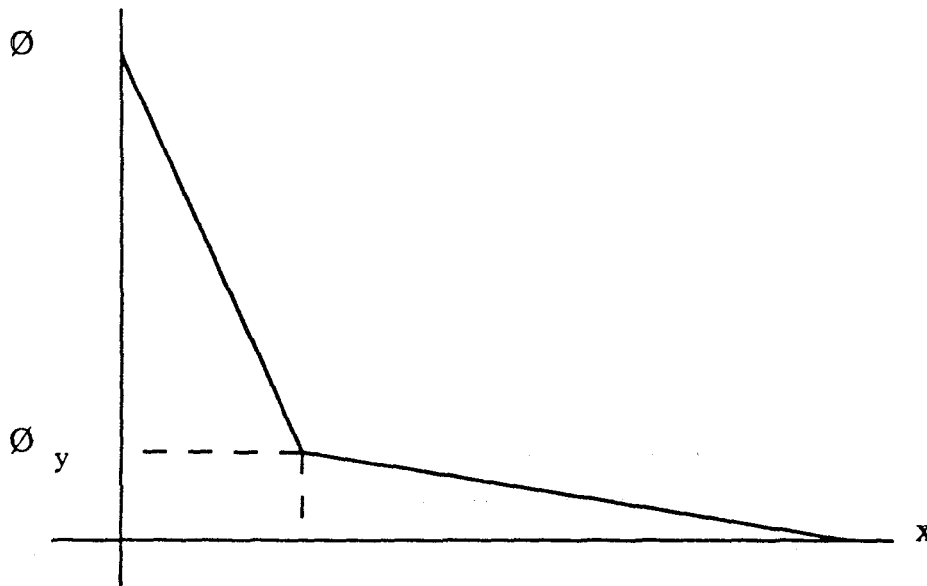
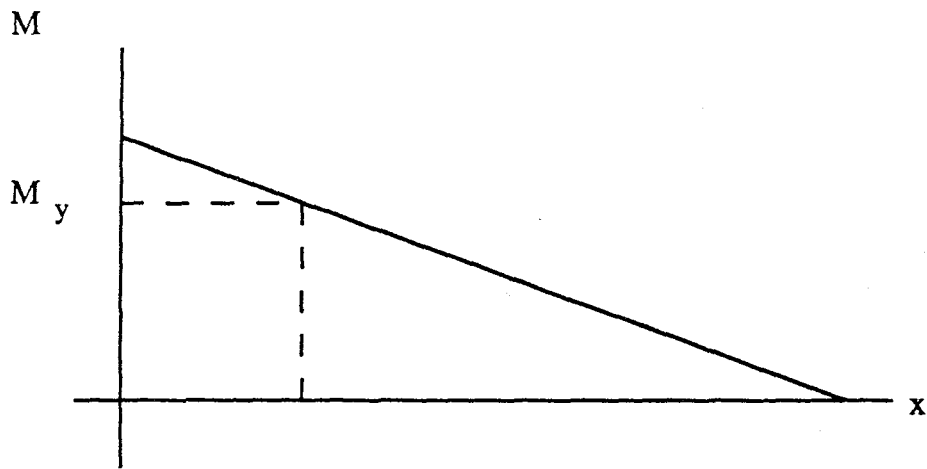


FIGURE 2-2 Cantilever Beam and Moment Curvature Diagram



**FIGURE 2-3 Curvature and Bending Moment Diagram for a Cantilever Beam**

$$D = \frac{\phi_m}{\phi_u} \quad (2.6)$$

where,

$\phi_m$  : Maximum curvature

$\phi_u$  : Ultimate or failure curvature under monotonic loading

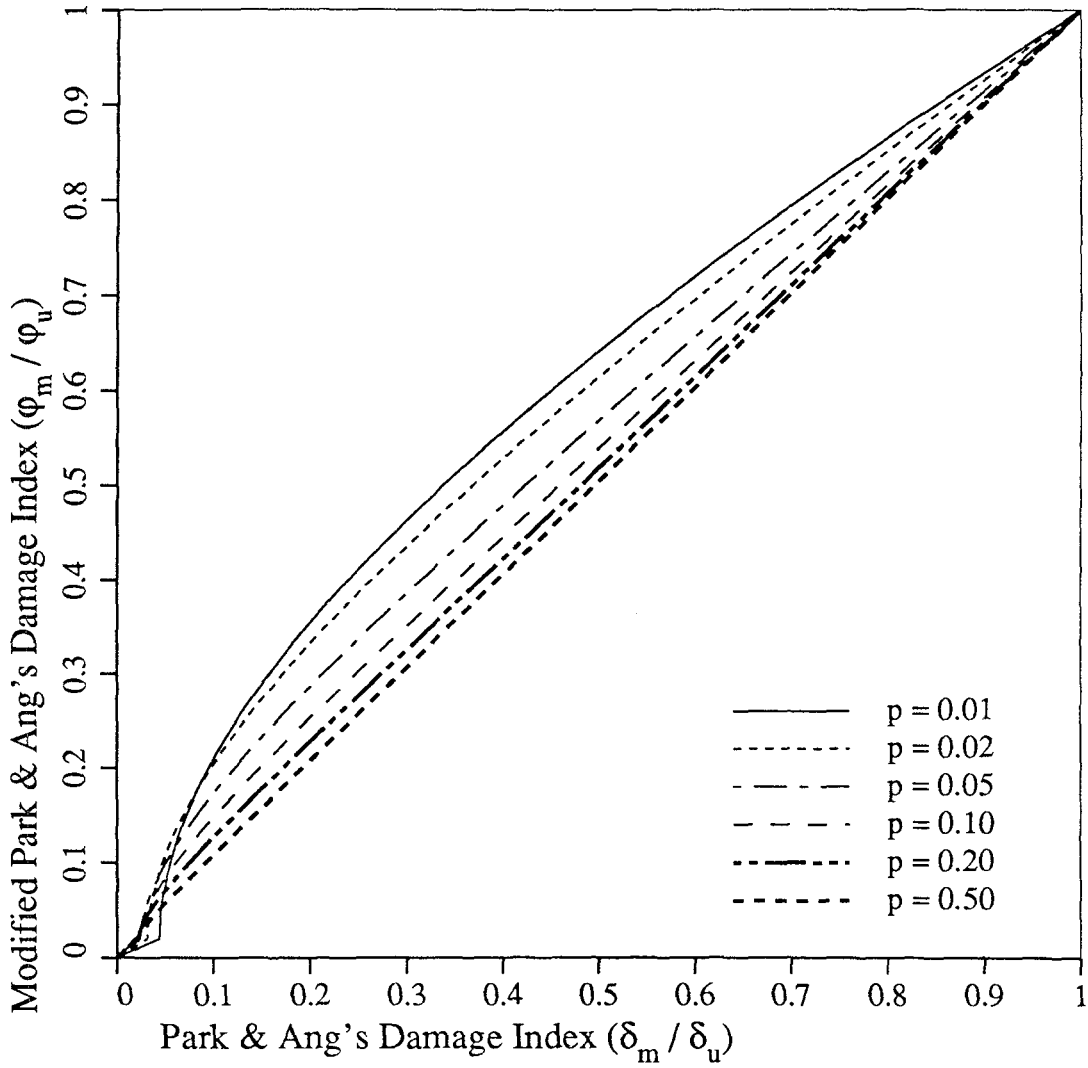
This modified Park and Ang's damage index, has been compared to the the first term of the original definition (Equation 2.5) for the cantilever beam in figure 2-2, assuming the bilinear moment curvature relationship of the same figure. Since the bending moment diagram is a straight line, the curvature is a bilinear function (See figure 2-3). The first term of Equation (2.5) can be computed by integrating twice the curvature diagram for a given load. The modified index given by Equation (2.6) can be directly obtained as a function of the applied load.

The relationship between the modified and the original definition of Park and Ang's damage index, depends on two parameters, i.e.  $p$ , the ratio between the post-yielding stiffness and the elastic stiffness (See figure 2-2), and the ratio between the failure curvature and the yielding curvature.

Figure 2-4 shows the value of the modified Park and Ang's damage index as a function of the first term of the original definition (Equation 2.5) for the case of a failure curvature 50 times greater than the yielding curvature and for various values of the  $p$  parameter. The reinforced concrete sections found in building frames usually have an approximate ratio between failure curvature and yielding curvature of 50 with the value of  $p$  being approximately 0.15. The value for  $p$  depends mainly on the kind of reinforcing steel used.

One can see by looking at figure 2-4 that the difference between these two definitions is small for important damage and for high values of the  $p$  parameter. For the worst cases,

$$\varphi_f = 50 \varphi_y$$



**FIGURE 2-4 Original vs. Modified Park & Ang's Damage Index**

the difference between the two indices is of 0.1. In any case, the modified Park and Ang's damage index should be seen as an alternative definition that will not always yield the same results as the original.

## 2.2 Global Damage Indices

Two kinds of global damage indices have been considered: weighted averages of the local damage indices described in the previous section, and the global damage indices based on the vibrational parameters of the structure as defined by DiPasquale and Cakmak [10].

### 2.2.1 Weighted Average of the Local Damage Indices

Seismic damage in reinforced concrete structures is usually concentrated in small areas. Even in the case of important damage, only a few joints are affected. Hence, if a global damage index is to be obtained as an average of the local damage, it is necessary to first define the locations at which the local damage will be evaluated and then, to use an appropriate weighting function so that more weight is given to the more damaged areas.

In this report, the definitions of global damage as a weighted average of the local damage have been taken from the authors that defined the local damage indices. For both Chung, Meyer and Shinozuka's and Park and Ang's damage indices, the global damage is obtained as a weighted average of the local damage at the ends of each element, with the energy dissipated as the weighting function [7 and 18].

The definition of the energy average of the local damage is given by

$$D_g = \frac{\sum_{i=1}^n D_i E_i}{\sum_{i=1}^n E_i} \quad (2.7)$$

where,

$D_g$  : Global damage index

- $D_i$  : Local Damage at the location  $i$
- $E_i$  : Energy dissipated at location  $i$
- $n$  : Number of locations at which the local damage is computed

This definition is used as a global damage index by Park *et al.* [18].

Chung *et al.* used the same definition as a story damage index given by

$$D_{S_k} = \frac{\sum_{i=1}^n D_i^k E_i^k}{\sum_{i=1}^n E_i^k} \quad (2.8)$$

where,

- $D_{S_k}$  : Story damage index for story  $k$
- $D_i^k$  : Local damage at the location  $i$  on story  $k$
- $E_i^k$  : Energy dissipated at location  $i$  on story  $k$
- $n$  : Number of locations at which the local damage is computed for story  $k$

The global or structural damage index for building frames is obtained as a weighted average of the story damage indices using a triangular shape, with the maximum at the base, as the weighting function [7]

$$D_g = \sum_{k=1}^N D_{S_k} I_k \quad (2.9)$$

where,

- $I_k = \frac{N + 1 - k}{N}$  : Weighing factor for story  $k$
- $N$  : Number of stories

According to this definition, the structural damage index has a maximum value of two when all the Story Damage Indices have a value of one, whereas Park's definition of global damage has a value between zero and one.



The plain energy average has also been utilized in this study for Chung, Meyer and Shinozuka's Local Damage Index as a means of comparison with the definition of Park and Ang's Global Damage Index.

It is important to note that a weighted average of the local damage could be computed in many different ways. Weighting functions other than the energy dissipated could be defined. The most crucial elements should have greater weight since their failure implies a global failure. Therefore, the appropriate definition of the weighting function depends on the structural configuration.

Importance factors that adapt the weighting function to the particular structural configuration have also been proposed. These importance factors would give more weight to some of the elements known to be important for the structure's performance. The disadvantage of this approach is that a subjective judgement is introduced, making it difficult to compare the damage sustained by different structural configurations if different importance factors are used. This disadvantage is overcome by the global damage indices in the next subsection described.

### 2.2.2 Global Damage Indices Based on the Vibrational Parameters

The damage indices based on the vibrational parameters avoid the averaging procedure of the local damage indices. DiPasquale and Cakmak [10] developed a damage model based on the evolution of the natural period of a time-varying linear system equivalent to the actual nonlinear system for a series of non-overlapping time windows. They used a *maximum likelihood criteria* for the identification of the time-varying equivalent linear system from the acceleration records at the top and at the base of the structure.

Their global damage index, named Maximum Softening, is given by

$$\delta_M = 1 - \frac{T_0}{T_{max}} \quad (2.10)$$

where,

$\delta_M$  : Maximum Softening

$T_0$  : Initial natural period

$T_{max}$  : Maximum natural period of an equivalent linear system

It has been shown that the Maximum Softening depends on a combined effect of stiffness degradation and plastic deformations [11]. In order to compute the Maximum Softening the response of the structure under study must be known. It is necessary to have the input ground acceleration and the acceleration at another location such as at the top of the structure.

The Final Softening is given by

$$\delta_F = 1 - \frac{T_0^2}{T_{final}^2} \quad (2.11)$$

where,

$\delta_F$  : Final Softening

$T_0$  : Initial natural period

$T_{final}$  : Final natural period

The Final Softening has been shown to be approximately equal to a weighted average of the local damage when the mode shape does not change significantly after damage [11]. It is related to the global stiffness degradation. The Final Softening will also be considered because if the initial natural period is known, it can be computed from the results of post-earthquake vibration testing. Thus, it is not necessary to know what the actual structural response was like.

DiPasquale and Cakmak [9, 10 and 11], proposed computing these damage indices from the acceleration records at the base and at the top of a structure, dividing the records in a series of time windows and computing the natural period of the equivalent linear system for each of those windows. The equivalent linear system was to be found by

using Maximum Likelihood estimators by means of a System Identification Computer Program named MUMOID [9].

In this study, numerical simulations of the seismic response of buildings have been created. Therefore, besides the acceleration records at the base and at the top of the building, information about the instantaneous natural period is available.

A new procedure for the computation of the damage indices based on vibrational parameters from the instantaneous natural period has been developed. This procedure is described in the next subsection.

### **2.2.3 Computation of the Maximum Softening by Averaging the Instantaneous Natural Period**

If the Global Damage Index defined by DiPasquale and Cakmak [10], is to be applied to the instantaneous natural period computed by a nonlinear dynamic analysis program, the instantaneous natural period has to be smoothed out in some way. The instantaneous natural period is computed from the first eigenvalue of the instantaneous tangent stiffness matrix. The natural period computed for each time step of a dynamic analysis presents a high variability. The maximum values are usually reached when some structural members yield; and the slope of the hysteresis loop is small before the next load reversal occurs. The duration of these maximum values is very short, and therefore, their influence in the natural period of an equivalent linear system is not significant. A more meaningful indication of the change in the natural period can be obtained by observing a moving average of the instantaneous natural period.

In figure 2-5 one can see a typical plot of the instantaneous natural period and several local averages with different averaging windows. The maximum and final natural periods, used for the computation of the damage indices, depend on the length of the averaging window. In this section, a criterion for the definition of the appropriate length of the averaging time window for the instantaneous natural period will be established.

If the instantaneous natural period ( $T$ ), is known at intervals  $\Delta t$ ,  $T$  is a discrete function of the time step  $i$ .

$$T = T(i) \quad i = 1, \dots, n \quad (2.12)$$

where,

$n$  = Number of time intervals  $\Delta t$  (Assumed to be an even number)

The averaged instantaneous natural period over  $j$  time steps ( $T_{av\ j}$ ) is also a discrete function of the time step  $i$ , and is defined as,

$$T_{av\ j}(i) = \frac{1}{j} \left[ \frac{1}{2} T\left(i - \frac{j}{2}\right) + \frac{1}{2} T\left(i + \frac{j}{2}\right) + \sum_{k=i-\frac{j}{2}+1}^{i+\frac{j}{2}-1} T(k) \right] \quad (2.13)$$

where,

$$j = 2, 4, 8, \dots, n$$

$$\frac{j}{2} \leq i \leq n - \frac{j}{2}$$

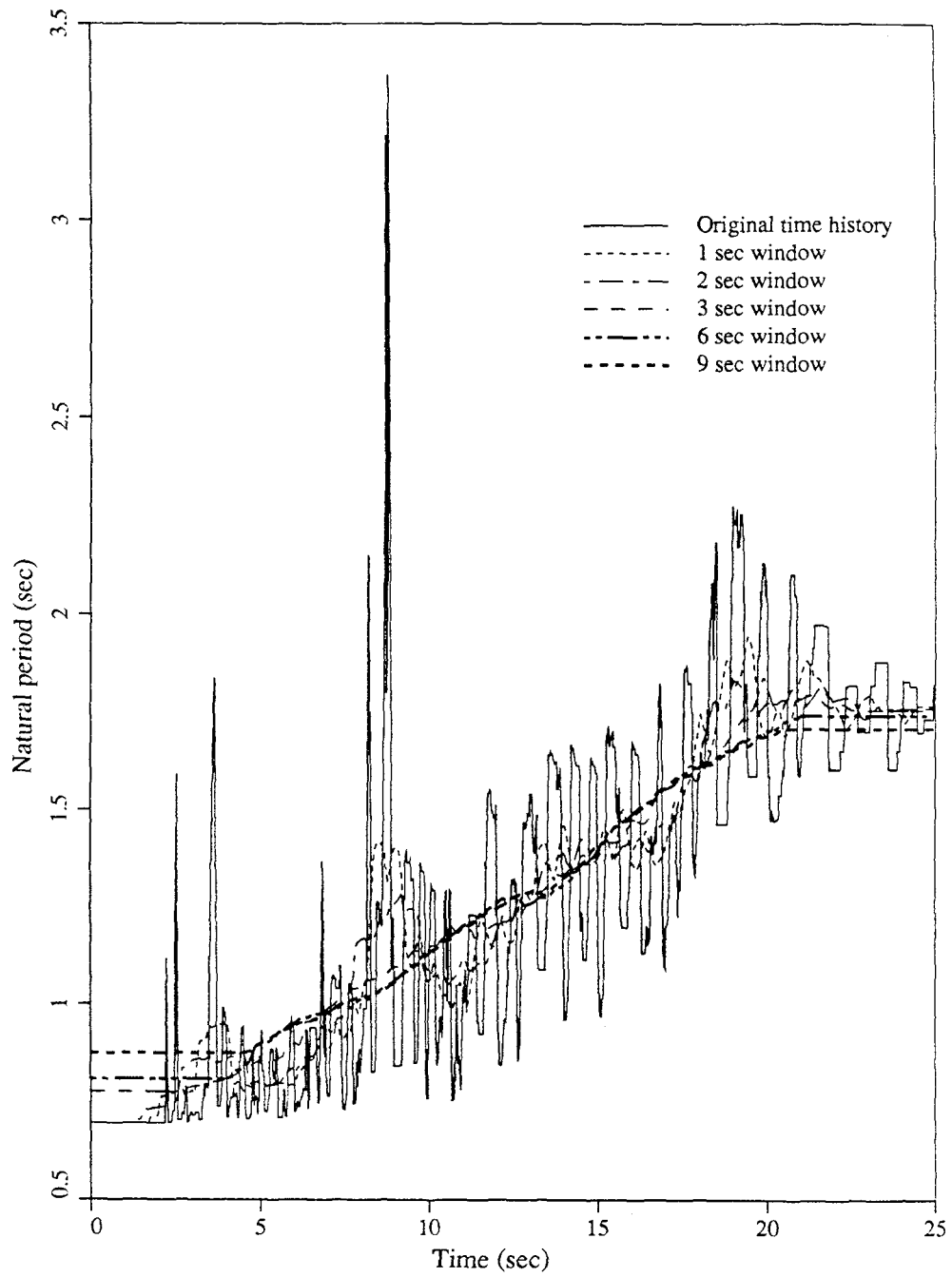
The variance function,  $\gamma$ , is defined as the ratio of the variance of a local average and the variance of the original process [26].

$$\gamma(j\Delta t) = \frac{\sigma_{T_{av\ j}}^2}{\sigma_T^2} \quad (2.14)$$

The variance of a local average process can be expressed as

$$\sigma_{T_{av\ j}}^2 = \sigma_T^2 \int_{j\Delta t}^{n\Delta t} -\frac{d\gamma(t)}{dt} dt \quad (2.15)$$

This equation shows that the variance of a local average process is directly proportional to the area under the absolute value of the derivative of the variance function between the value of the length of the averaging window, and the total length of the record. The variance reduction due to the averaging procedure is the value of the variance function



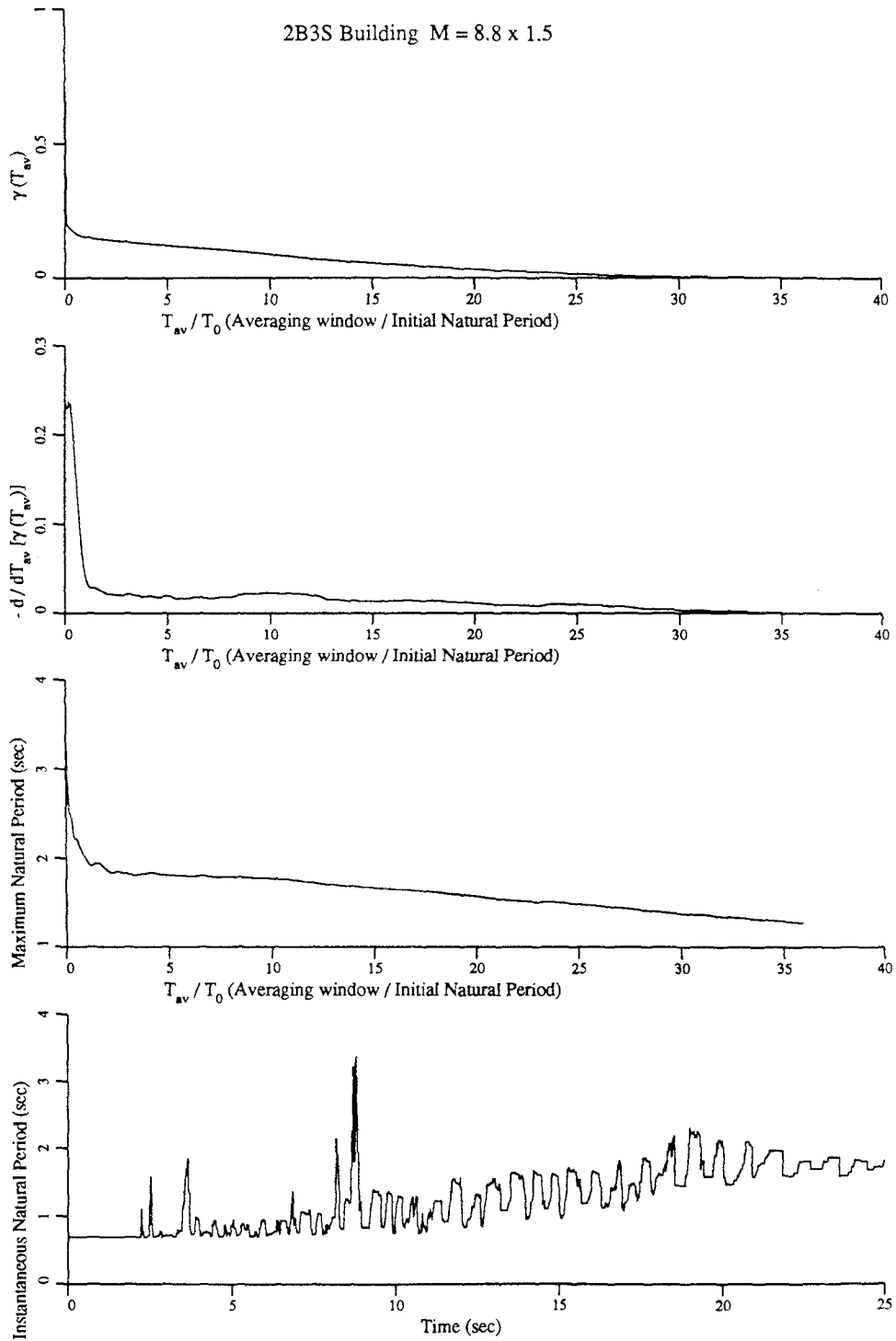
**FIGURE 2-5 Averaged Instantaneous Natural Period for Different Averaging Windows**

for the time window used. This variance reduction is also proportional to the area under the absolute value of the derivative of the variance function between a time window of zero (no averaging) and the time window used to get the local average.

Looking at figure 2-5 it is clear that the instantaneous natural period can be split into components with different scales of fluctuation [26]. The components with smaller scale of fluctuation will be the *random* deviation from a *deterministic* trend that has a larger scale of fluctuation. This deterministic trend is an indication of the global stiffness of the structure, therefore, it is the component that should be used for the computation of the global damage indices.

When a structure is subjected to an earthquake with a wide band frequency content, the oscillations of the structure will have a narrow frequency content around its natural frequency. For each cycle some structural members can go through a hysteresis loop, changing their stiffness according to the slope of the moment-curvature trajectory. The fluctuations of the instantaneous natural period around the main trend will have a frequency related to the natural frequency of the structure. The scale of fluctuation will also be related to the natural period of the structure. In the case of nonlinear behavior, the frequency content of the response will change according to the damage sustained, but the deviation of the instantaneous natural period from the deterministic trend will still have a scale of fluctuation related to the time-varying natural period of the structure.

If the scales of fluctuation of the different components are different enough, it is possible to separate the component with the largest scale of fluctuation by averaging the instantaneous natural period using a time window greater than the scale of fluctuation of the random deviations and smaller than the scale of fluctuation of the deterministic trend. In order to find the value of the averaging window that separates the main trend from the local deviation, a set of plots like the one of figure 2-6 can be obtained for each case.



**FIGURE 2-6 Variance Function and Maximum Natural Period as a Function of the Length of the Averaging Window**

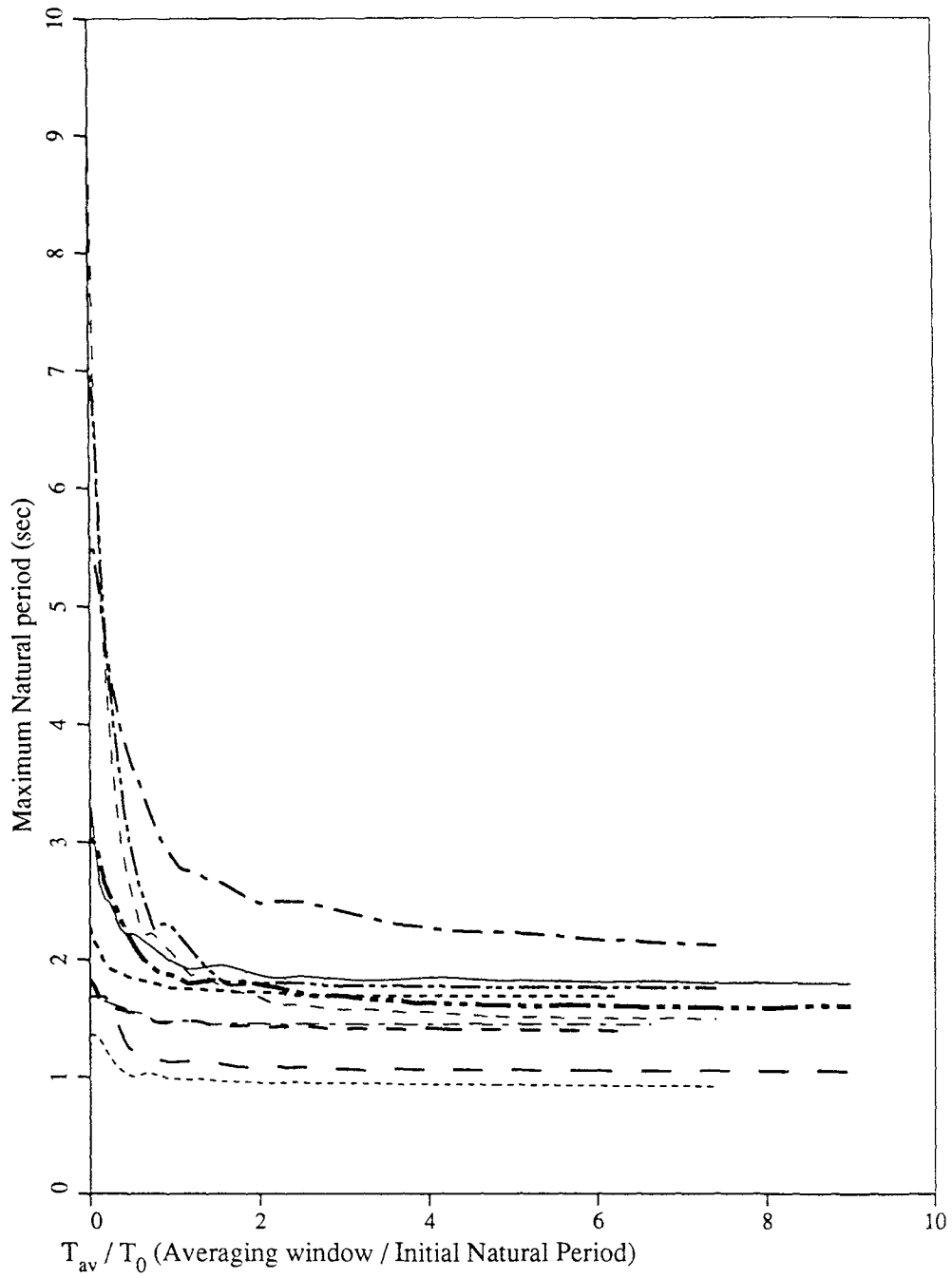
The first plot of figure 2-6 shows the variance function (Equation 2.14) as a function of the normalized length of the averaging window. The variance function has a value of one when the length of the averaging window is zero and then decreases to a value of zero when the length of the averaging window is equal to the record's length. The variance function has three parts with very different slopes that suggest that the instantaneous natural period has three components with different scales of fluctuation. The first component, with a very small scale of fluctuation, causes the variance function to decay very rapidly for very small values of the averaging window. This component is due to the variations in the instantaneous natural period from one time step to the following. The second component has a cyclic appearance, with a natural frequency similar to the natural frequency of the structure. This component is due to the oscillations of the structural stiffness about its main trend. Finally, the third component is considered to be the *deterministic* trend that indicates how the natural period evolves.

In figure 2-6, there is also a plot with the maximum natural period as a function of the averaging window. One can observe that the maximum period decreases rapidly until the averaging window is between 2 and 2.5 times the initial natural period and then is stabilized and decreases slowly tending to the average value when the averaging window is equal to the length of the record. In figure 2-7 the maximum natural period as a function of the length of the averaging window is shown for some of the numerical simulations that will be described later.

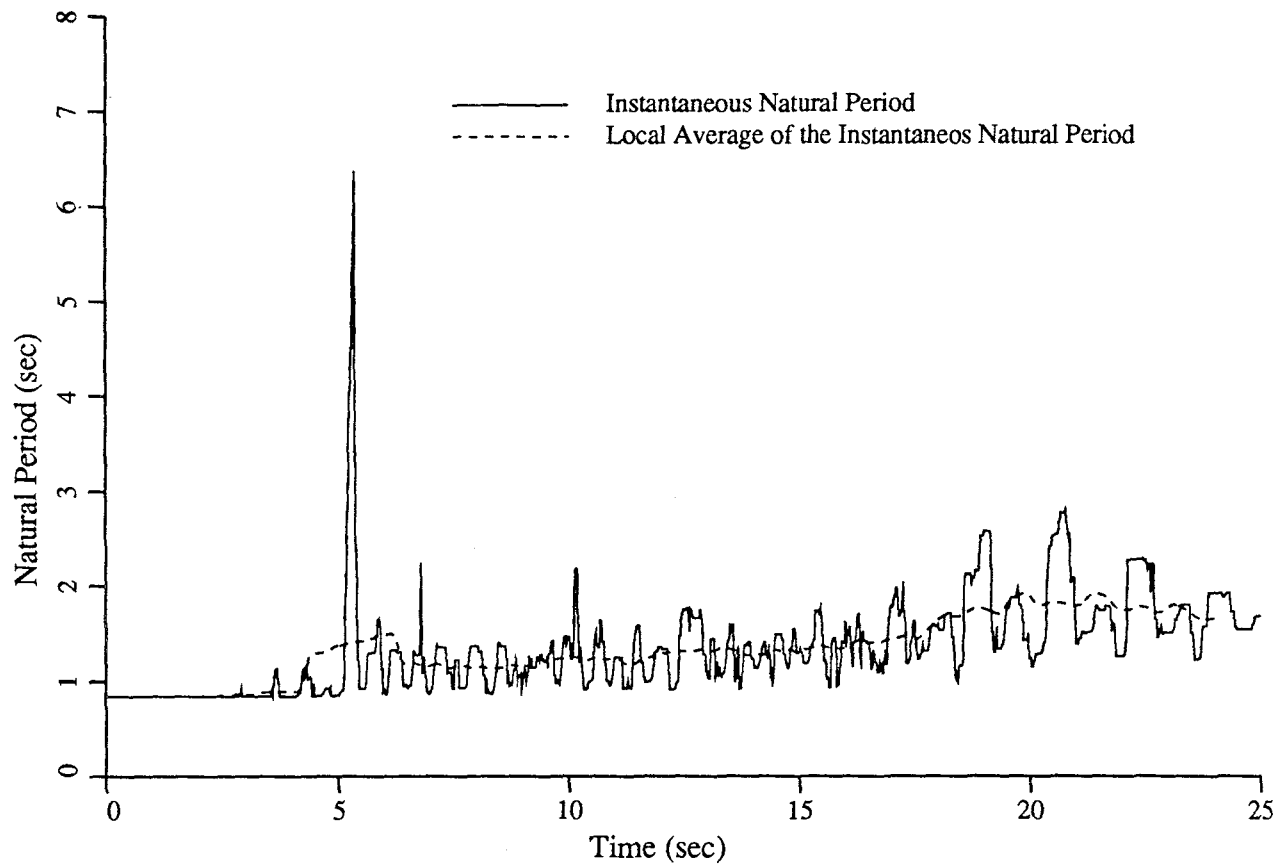
Using averaging windows between 2 and 2.5 times the initial natural period the results obtained for the maximum natural period are similar, but it is desirable to use a value close to the upper limit in order to allow for an increase in the natural period produced by softening. In this study an averaging window 2.4 times the initial natural period has been used.

Figure 2-8 shows an example of the instantaneous natural period as a function of time, plus the local average computed with a time window 2.4 times the initial natural period.



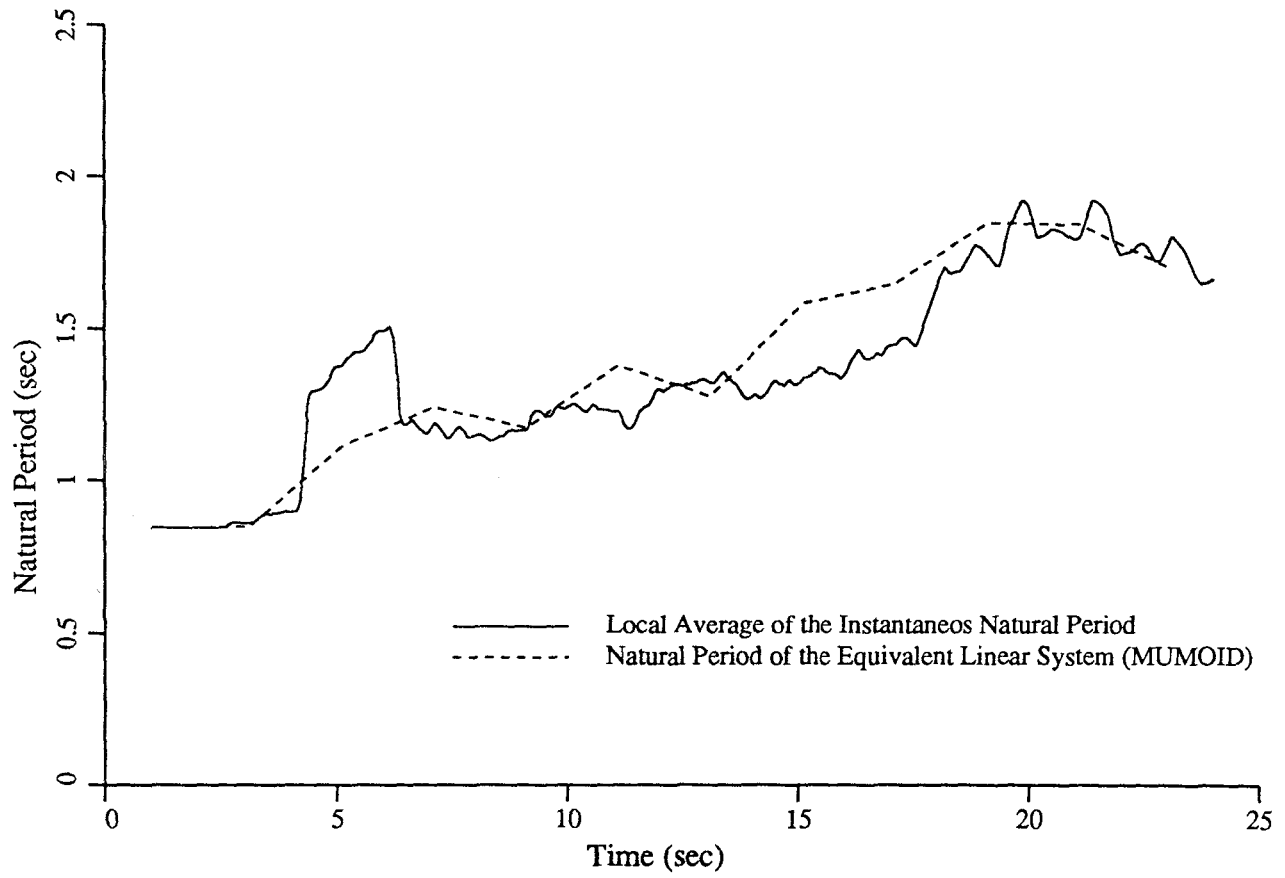


**FIGURE 2-7 Maximum Natural Period as a Function of the Length of Averaging Window**



**FIGURE 2-8 Instantaneous Natural Period and Local Average**

In figure 2-9 the local average is compared to the natural period of the time-varying linear equivalent system obtained by using the program MUMOID [9]. It can be seen how the two curves are close enough with a small difference between maximum values.



**FIGURE 2-9 Local Average of the Instantaneous Natural Period and Natural Period of an Equivalent Linear System**

## SECTION 3

### COMPUTER PROGRAM SARCF-III

#### 3.1 General Description

SARCF-III is a computer program for the seismic analysis of reinforced concrete frames which can simulate the strength and stiffness degradation observed in experimental tests under strong load reversals. A general description of the initial version of this program can be found in References [7] and [8]. The most important characteristics will be summarized now.

The structure is idealized as an assembly of one dimensional beam or column elements which interconnect the nodes or joints. Loads are applied to the nodes.

The stiffness and strength degradation parameters are determined internally from the basic material and section properties. In figure 3-1 one can see the shape of the hysteresis loops that define the moment curvature relationship.

The failure moment level is related to the member's actual strength reserve or residual strength, which is a function of the load history and maximum experienced curvature level,  $\phi$ . The failure moment is proposed as a function of the normalized curvature level (See figure 3-2), given by

$$M_{fi} = M_f \cdot \frac{2\Phi_i}{\Phi_i + 1.0} \quad (3.1)$$

where

$M_{fi}$  : Failure moment for given curvature level  $\phi_i$

$M_f$  : Failure moment for monotonic loading

$\Phi_i = \frac{\phi_i}{\phi_f}$  : Curvature ratio

$\phi_f$  : Failure curvature for monotonic loading

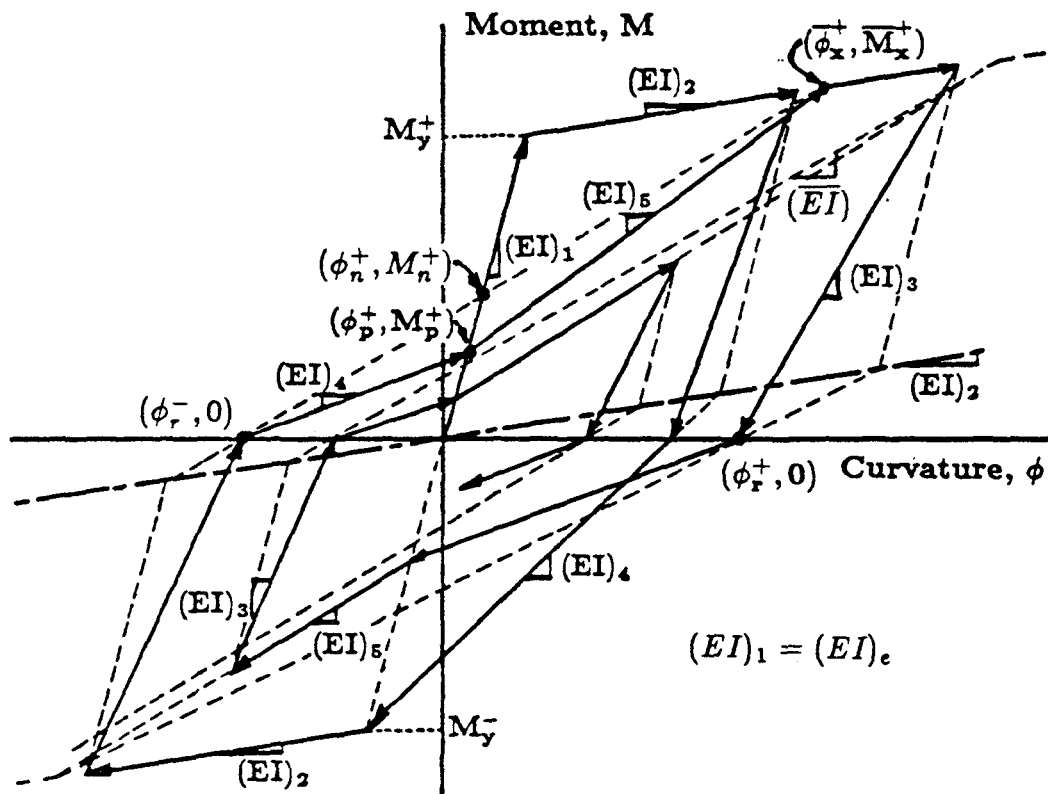


FIGURE 3-1 Hysteretic Moment–Curvature Relationship [8]

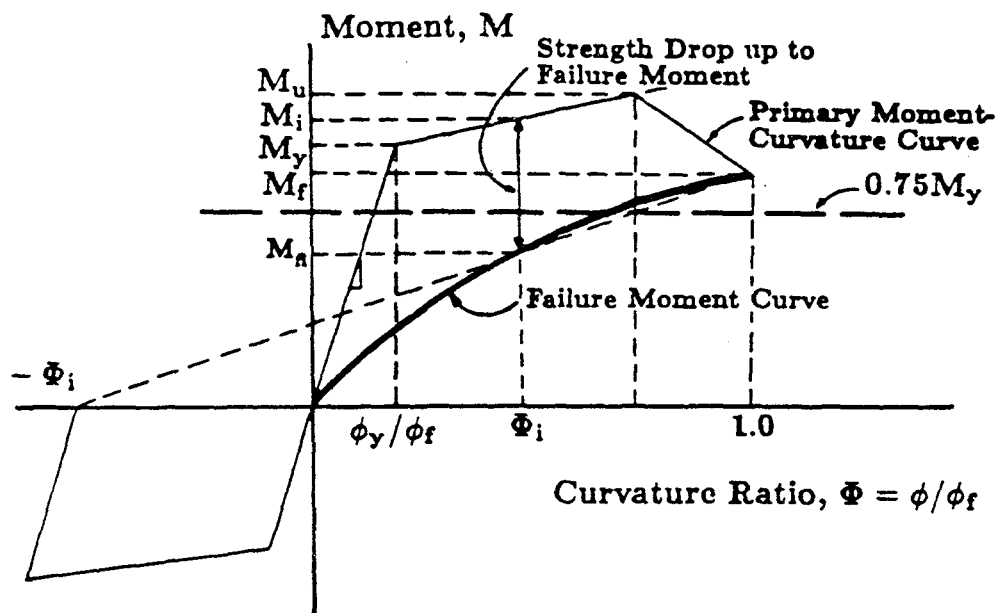


FIGURE 3-2 Definition of Failure [7]

This failure moment is used for the definition of the local damage index of Equation (2.1) proposed by Chung *et al.* [6].

The strength deterioration is initiated as soon as the yield load level is exceeded, and the strength deterioration accelerates as the critical load level is reached. As shown in figure 3-3, the amount of strength deterioration given a load level,  $\Delta M$ , is represented by

$$\Delta M = \Delta M_f \left( \frac{\phi - \phi_y}{\phi_f - \phi_y} \right)^\omega \quad (3.2)$$

where

$\Delta M_f$  : Moment capacity (strength) reduction in a single load cycle  
at failure curvature

$\phi_y, \phi_f$  : Yield and failure curvature, respectively

$\omega$  : Strength degradation parameter with a value between 1.5 and 2.5

The pinched shape of the hysteresis loops is simulated as a function of the shear span.

The point  $(M_n^+, \phi_n^+)$ , (figure 3-1) will be introduced with the following coordinates

$$\phi_n^+ = \phi_r^- \frac{(\overline{EI})}{(\overline{EI}) - (EI)_e} \quad M_n^+ = (EI)_e \phi_n^+ \quad (3.3)$$

where

$$(\overline{EI}) = \frac{\overline{M}_x}{\phi_x^+ - \phi_r^-} \quad (3.4)$$

The coordinates of the crack-closing point can be expressed as [6]

$$M_p^+ = \alpha_p M_n^+ \quad \phi_p^+ = \alpha_p \phi_n^+ \quad (3.5)$$

where

$$\alpha_p = \begin{cases} 0 & \text{if } \frac{a}{d} \leq 1.5 \\ \sqrt{0.4 \frac{a}{d} - 0.6} & \text{if } 1.5 < \frac{a}{d} \leq 4.0 \\ 1 & \text{if } \frac{a}{d} > 4.0 \end{cases}$$



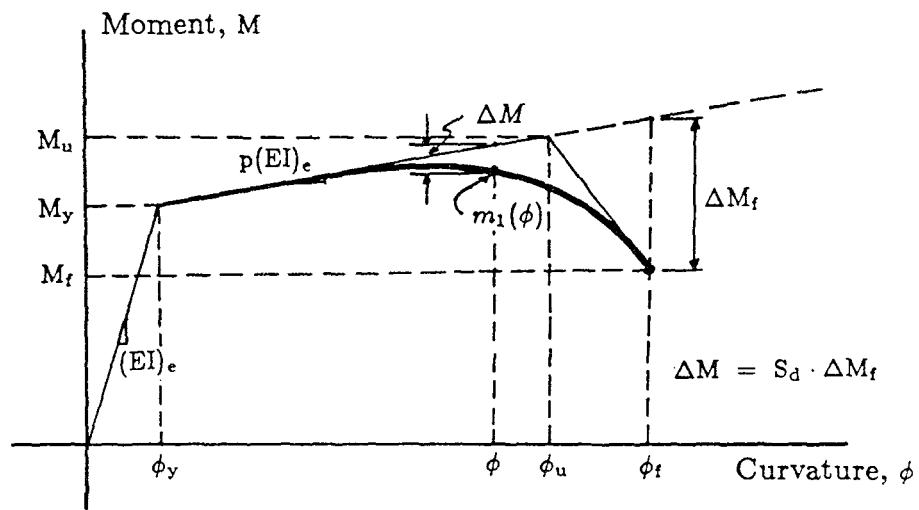


FIGURE 3-3 Strength Deterioration Curve [7]

$\frac{a}{d}$  : Shear span ratio

$a$  : Shear span, assumed to be equal to  $\frac{l}{2}$

$l$  : Clear span length

$d$  : Cross-sectional depth

The “pinching factor”,  $\alpha_p$ , is such that  $\alpha_p$  is equal to one if the shear effect is negligible, and  $\alpha_p$  is equal to zero if the shear effect completely controls the load-deformation behavior.

The reinforced concrete element model takes into account the finite size of the plastic regions. The structure is idealized as a plane frame ignoring out-of-plane motion. All the mass of the structure is assumed to be lumped at the nodes.

The  $P - \Delta$  effect is taken into account by adding the geometric stiffness to the columns stiffness, using the axial forces produced by the static loads.

The shear deformation of the elements is not taken into consideration. The frame is assumed to be fixed at a infinitely rigid foundation.

In the following section the modifications that have been carried out on the original program will be described.

### **3.2 Improvements of the Program**

The program SARCF-III includes the following modifications from the original version:

1. Computation of the initial internal forces by means of a static analysis

The internal forces, shear, bending moments, and axial forces due to the dead loads, can be computed using a linear static analysis prior to the nonlinear dynamic analysis.

2. Correction of the length of the plastic hinges

Plastic hinges are considered to extend on the part of the elements which has experienced a bending moment larger than the yield moment, according to the original definition found in Reference [8].

3. Computation of the interstory drift and ductility ratio

4. Computation of the modified Park and Ang's Damage Index (Equation 2.6)

5. Preparation of data for the computation of the Maximum Softening

Files with the acceleration at the base and the acceleration at the top are created to be used with the System Identification Program, MUMOID. Another file with the history of the instantaneous natural period is created to be used for the computation of the moving average of the instantaneous natural period.

6. Analysis of damaged structures

The state of damage and the internal forces in all the elements are saved at the end of each dynamic analysis so that it is possible to study the response of a damaged structure to a second earthquake.

7. Failure of elements

When the curvature exceeds the failure curvature, the bending stiffness is made equal to a very small number. The failure curve described above was used in the original program only for the definition of the strength drop for each cycle and for the computation of the local damage index. In this new version, a limit to the maximum curvature is introduced to avoid results with a very large curvature without physical meaning.

8. Generation of artificial earthquakes using ARMA model

The procedure proposed by Ellis and Cakmak [12 and 13] is followed. Single and double peak earthquakes, statistically equivalent to the ones that take place in Japan, can be generated given the duration, magnitude, and distance from the source or sources, and the soil parameters.

### 3.3 Remaining Limitations

The computer program used for the numerical simulations, even after the improvements that were carried out, presents limitations that should not be forgotten in the analysis of the results.

1. Nonstructural elements, such as cladding, partitions, etc, are not included in the structural model.
2. Shear deformations are neglected. It is assumed that the amount of shear reinforcement is enough to prevent shear failure. The failure due to shear is not considered.
3. The bending capacity of the elements is computed taking into consideration the initial axial forces, but that capacity does not change with the axial forces during the dynamic analysis.
4. The axial stiffness of the columns is computed assuming that they are under compression. The reduction in the axial stiffness due to the cracking produced by tensile forces is not taken into consideration.

### 3.4 Comparison between Computed and Experimental Results

In order to assess the ability of the program SARCF-III to predict the seismic response of reinforced concrete structures, computed results using the computer program have been compared to the results of experimental tests on a reinforced concrete model carried out at the University of Illinois at Urbana-Champaign (UIUC) by Sozen and his associates [5].

The results computed using the program IDARC, Inelastic Analysis of Reinforced Concrete Structures, developed at State University of New York at Buffalo by Y. J. Park *et al.* [18], have also been included in the comparison. The program IDARC has the same

purpose as the program SARCF-III, but contains a more general hysteresis rule which includes the cracking of the concrete before yielding.

As one can see in figure 3-4, the test structure consisted of two ten story, three bay frames working in parallel with ten story weights attached in between. The test structure had a uniform distribution of the story heights. Nonstructural elements were not modeled. The out-of-plane motion was impeded. The simulated earthquake runs had base motions that were patterned after the North-South component of the acceleration history measured at El Centro during the Imperial Valley Earthquake of 1940. The original earthquake time scale was compressed by a factor of 2.5.

The same test structure, named H1 [5], was subjected to three runs of scaled El Centro Earthquake with increasing peak acceleration. Hence, the second and third runs affected a damaged structure.

For this model, all the dimensions and material properties were known with a higher degree of accuracy than is usual in reinforced concrete construction. An idealized computer model was constructed using the average actual properties of the microconcrete and reinforcing wires. A damping of 3.5% of the critical was used.

The digitalized time history of the measured acceleration at the base of the test structures was utilized as the base input acceleration. Since the test structures were subjected to three different artificial earthquakes, the computer response was calculated using a time history of the base acceleration obtained by appending the second and third runs to the first one. In this way, at the beginning of the second and third runs, the model of the structure had degraded its properties like the actual structure.

Since the general shapes for the response of the test structures were dominated by the first mode, the time history of the displacement of the top floor was used for the comparison between the experimental and the computed results.

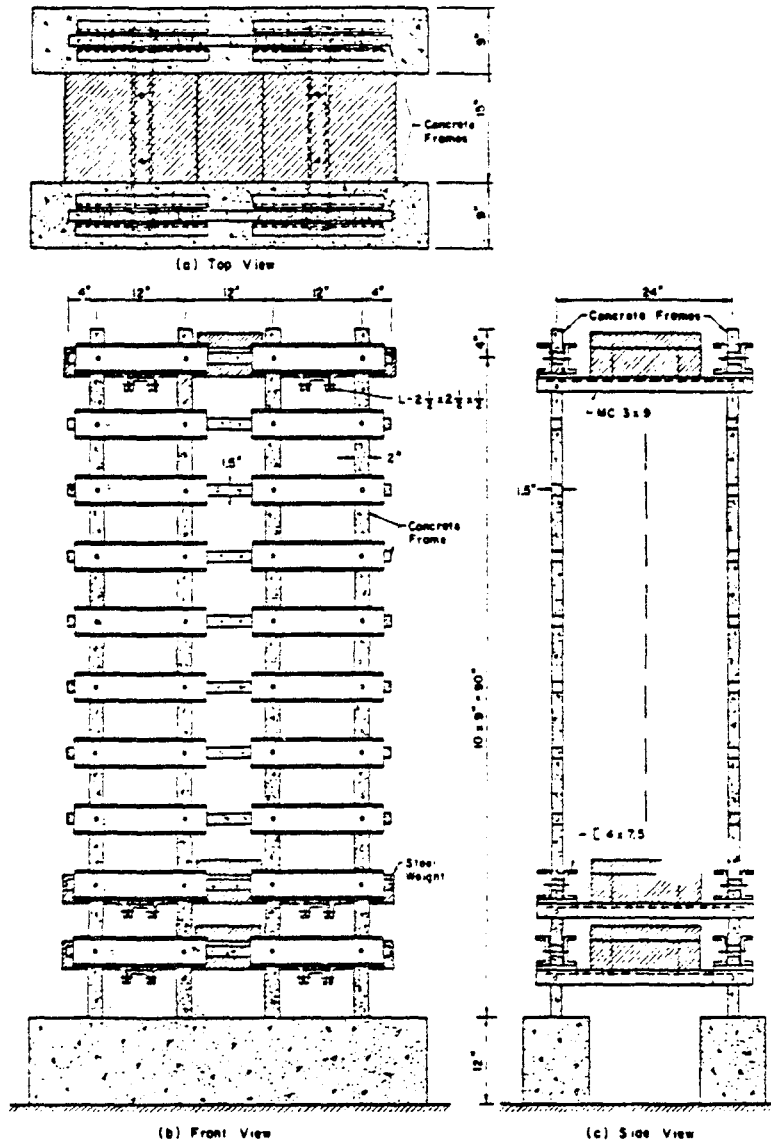


FIGURE 3-4 Test Structure Used for the Comparison [5]

Both computer models for the computer programs SARCF-III and IDARC were developed without using the information that could have been drawn from the experimental results. In both computer programs there are parameters whose value could have adjusted the computed results to the experimental results. Nevertheless, the average values recommended by the authors of the programs have been used. For instance, the strength degradation parameter,  $\omega$ , used in Equation (3.2), that defines the strength degradation curve in the program SARCF-III, was given the value of 1.5.

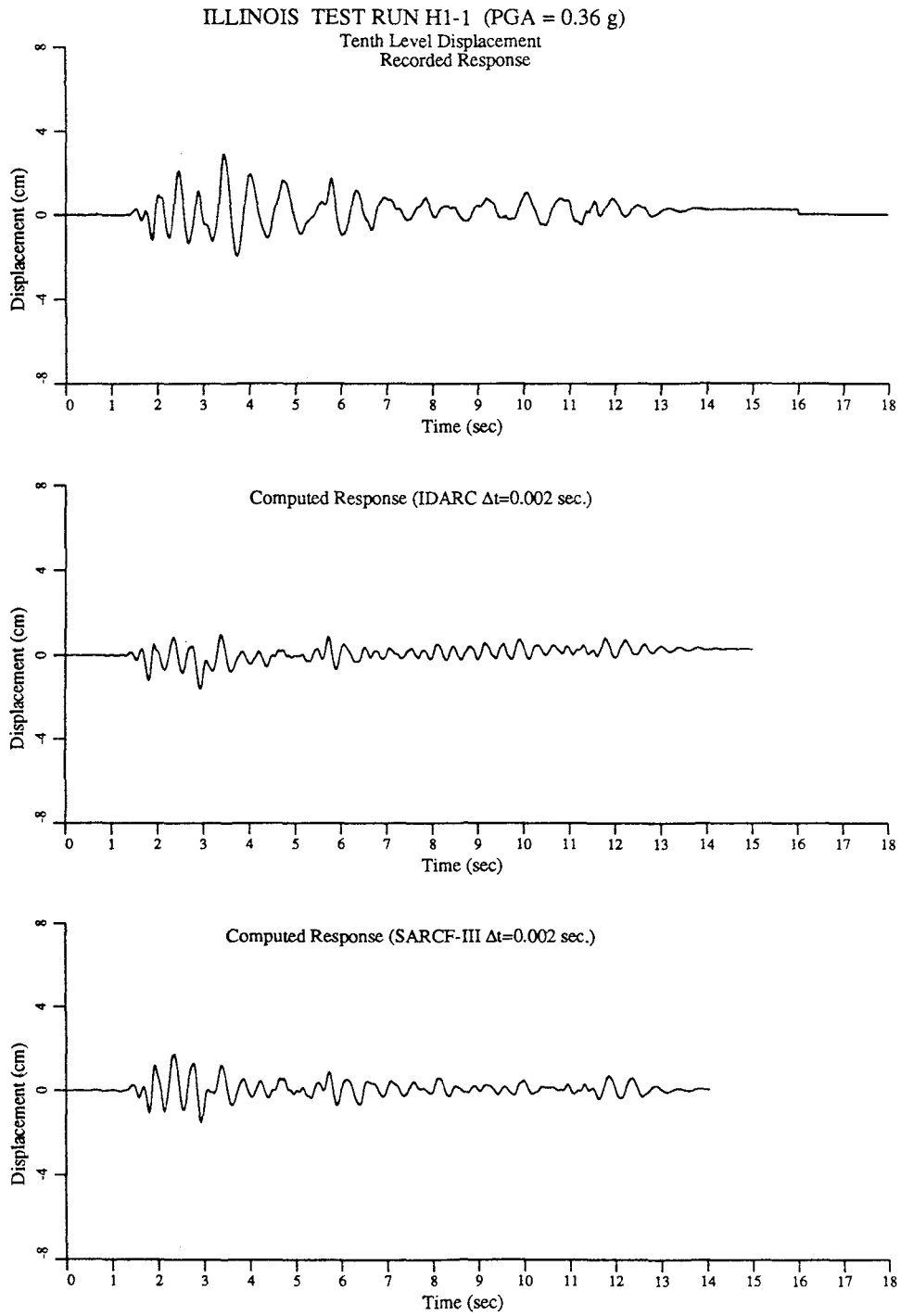
In the input for the program IDARC, the parameters  $\alpha$ , which defines the stiffness degradation, and the slippage or pinching coefficient,  $\gamma$ , [18], were given a value of 2 and 10 respectively. The rate of strength degradation,  $\beta$  and the post-yielding stiffness ratio, were computed internally by the computer program using correlation formulae [18].

The time step used for the numerical integration of the equations of motion was of 0.002 seconds in both cases. This small time step is required by the fact that both computer programs carry out only one iteration for each time step. In the program SARCF-III the unbalanced internal forces are applied to the following time step, thus correcting the tendency to drifting by modifying slightly the input ground motion. In the program IDARC the lack of correction for unbalanced internal forces makes an even smaller time step necessary in order to get the right solution.

An analysis of the results of the comparison between experimental and computed results for the three consecutive runs follows.

#### **3.4.1 First Run (Run H1-1)**

The maximum base acceleration was 0.36 g. The columns of test structure remained elastic, but several beams started to develop plasticity. At the beginning of the record shown in figure 3-5, the computed time history of the displacement of the tenth level using



**FIGURE 3-5 Comparison between Experimental and Computed Results (First Run)**



both computer codes is very close to the recorded time history. After the first 1.5 seconds of strong motion, the test structure experienced a slight increase in the natural period that the computer programs do not fully predict. Both computer programs underestimate the displacements. The computed maximum relative displacement is approximately 30% less than the recorded maximum for both programs.

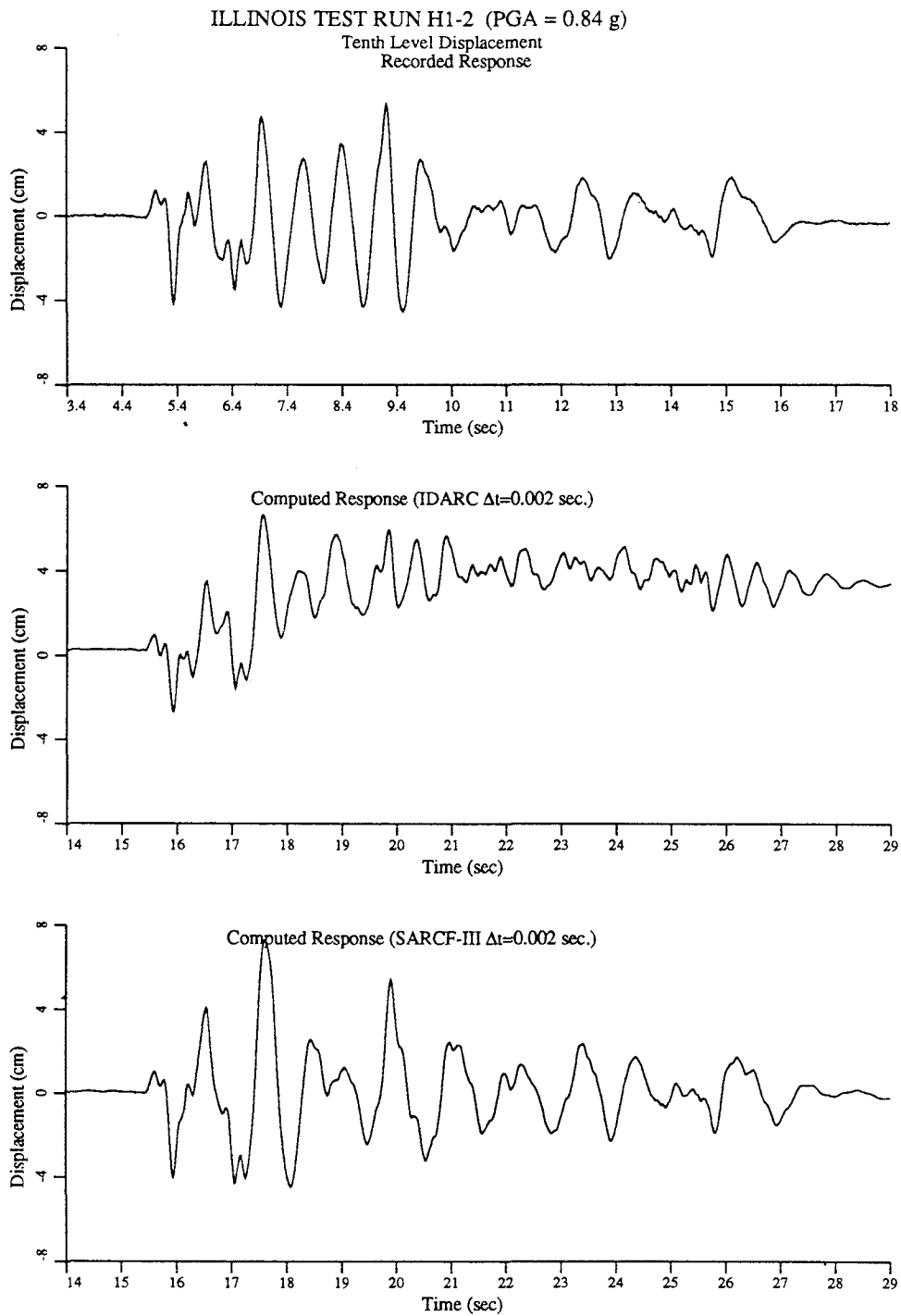
In the case of the program SARCF-III, this lack of agreement seems to be due to the nonlinear behavior of the reinforced concrete sections, even for bending moments below the defined yield moment. The experimental results shown in Reference [14] suggest that the stiffness of reinforced concrete sections after cracking decreases with cycling loading even when the load level is below the yield moment. In the computed results, the initial stiffness of the columns holds, whereas the experimental results suggest a reduction of the stiffness of the columns.

In the case of the program IDARC, the stiffness degradation after cracking is controlled by the stiffness degradation parameter  $\alpha$ . An  $\alpha$  parameter of 2, found to be appropriate for the post-yielding behavior of reinforced concrete, does not seem to produce a sufficient stiffness degradation for loads between the cracking and the yielding points. Test conducted with  $\alpha$  equal to 0.1 yielded results close to the experimental ones. However, using that value of  $\alpha$  would have been against the principle of not using information drawn from the experimental results when building the computer models.

### **3.4.2 Second Run (Run H1-2)**

The maximum base acceleration was 0.84 g. The columns of the test structure started to develop plasticity. Most of the beams had plastic hinges.

At the beginning of the record shown in figure 3-6, the computed time history of the displacement of the tenth level using SARCF-III is very close to the recorded time history. After the first second of strong motion, the test structure experienced an increase in



**FIGURE 3-6 Comparison between Experimental and Computed Results (Second Run)**

the natural period greater than that predicted by the computer program. The computed maximum relative displacement is 16% greater than the recorded maximum and it does not take place exactly at the same time. In the last five seconds of strong motion, the response computed with SARCF-III, and the recorded response are very close, both in frequency content and amplitude.

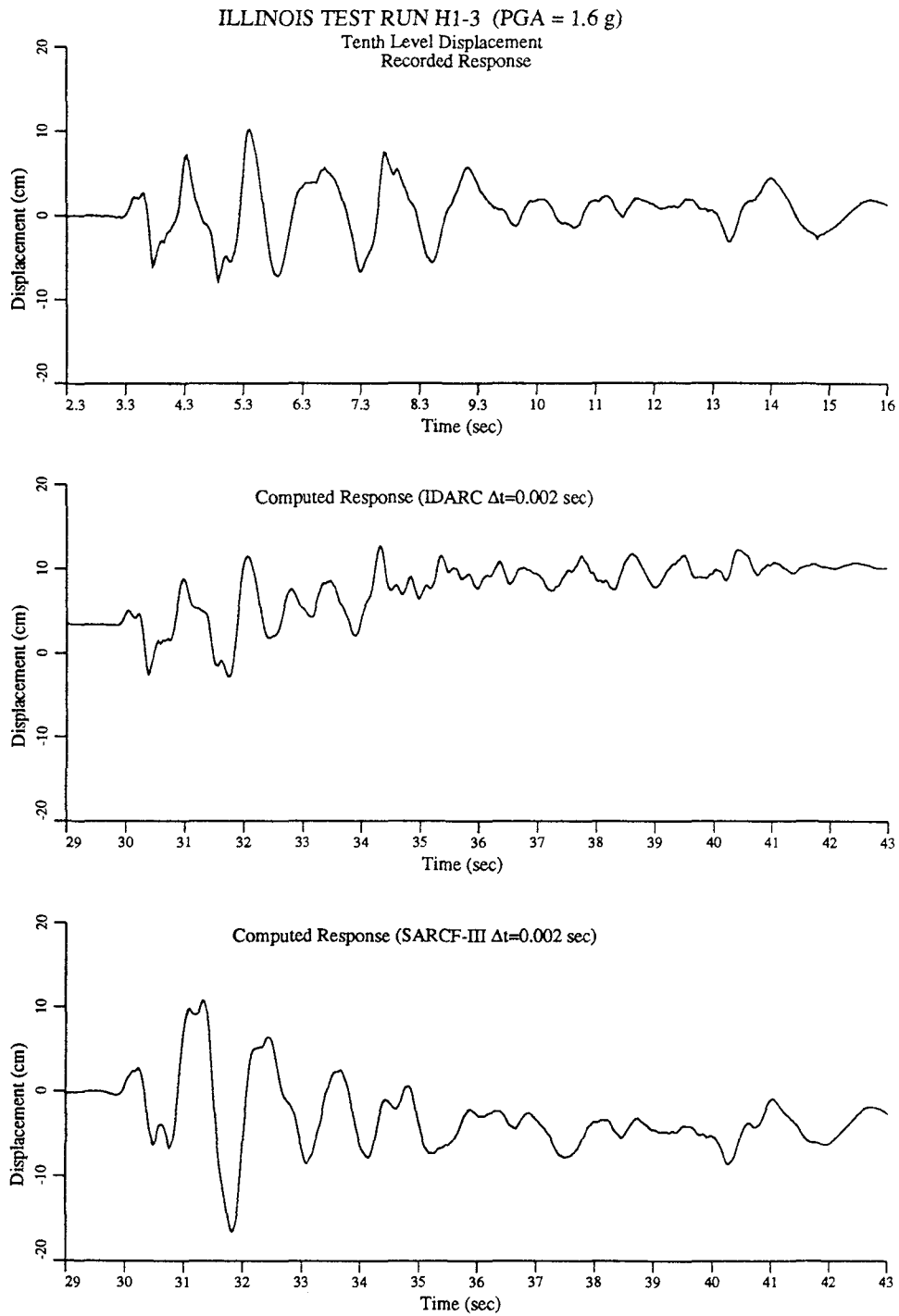
The response computed using IDARC presents a numerical drift because of the lack of correction of the unbalanced internal forces. The evolution of the zero crossings rate differs more than in the response computed with SARCF-III.

### **3.4.3 Third Run (Run H1-3)**

The maximum base acceleration was 1.60 g. The columns and the beams of test structure developed plasticity in most of the joints. Figure 3-7 shows the recorded and computed responses.

The tenth level displacement time history computed by using IDARC is very close to the recorded time history for the first two seconds of ground motion. After that, the computed results present a drift, and the natural period does not increase as in the recorded response. The computed maximum relative displacement is 18% smaller than the recorded maximum.

The the tenth level displacement computed using SARCF-III presents a maximum after about two seconds of ground motion, which is approximately 40% greater than the recorded maximum. However, the second half of the record is very close, both in frequency content and amplitude. SARCF-III predicts the increase in the natural period of the test structure.



**FIGURE 3-7 Comparison between Experimental and Computed Results (Third Run)**

### 3.4.4 Conclusions

The conclusion that can be extracted from the comparison of the recorded response to the computed response is that, given the uncertainties that exist in the description of the nonlinear behavior of reinforced concrete structures, a good approximation was obtained using the program SARCF-III. The response of structures clearly in the nonlinear range (test runs H1-2 and H1-3) is predicted with a higher degree of accuracy than that of structures that start to develop plasticity (test run H1-1).

The probability of damage, based on the global damage indices as defined by DiPasquale and Cakmak [10] was obtained for the experimental results and for the numerical simulations. For the experimental results the probabilities of damage were 0.5, 0.9998 and 1.0 for the test runs H1-1, H1-2 and H1-3, respectively. Whereas for the numerical simulations 0.02, 0.9999 and 1.0 were the probabilities obtained for the same runs H1-1, H1-2 and H1-3. One can see that the numerical simulation gives a good approximation for the damaged structures i.e. H1-2 and H1-3. For the test run H1-1, which is on the onset of the damage, the probability of damage obtained from the computed results differs more from the probability of damage obtained from the experimental results.

The program IDARC, although including a more complete hysteresis model, did not yield an approximation as good as SARCF-III. Its main problem was the drifting of the response, which could be reduced by using a smaller time step at the expense of longer computations. Since its hysteresis model includes more parameters, it is possible to do parametric studies in order to find the appropriate parameters to match the experimental results. In this case, the standard parameters were used, which did not produce the best possible results with IDARC.



## SECTION 4

### NUMERICAL SIMULATIONS FOR BUILDING STRUCTURES

#### 4.1 Description of the Buildings to Be Analyzed

The numerical simulations have been carried out on three low rise buildings designed according to the existing codes.

##### 4.1.1 Two Bay Three Story Building Frame

The building frame described in Reference [21] has been used. A brief description of its main characteristics taken from the already mentioned reference follows. The typical office building of figure 4-1 has been designed according to the ACI 318-83 code [1], to resist the equivalent static lateral loads specified in the Uniform Building Code [25].

The design base shear can be obtained by using

$$V = \frac{Z I C}{R_W} \times W \quad (4.1)$$

$Z = 0.4$  : for seismic zone 4

$I = 1.0$  : for occupancy importance factor

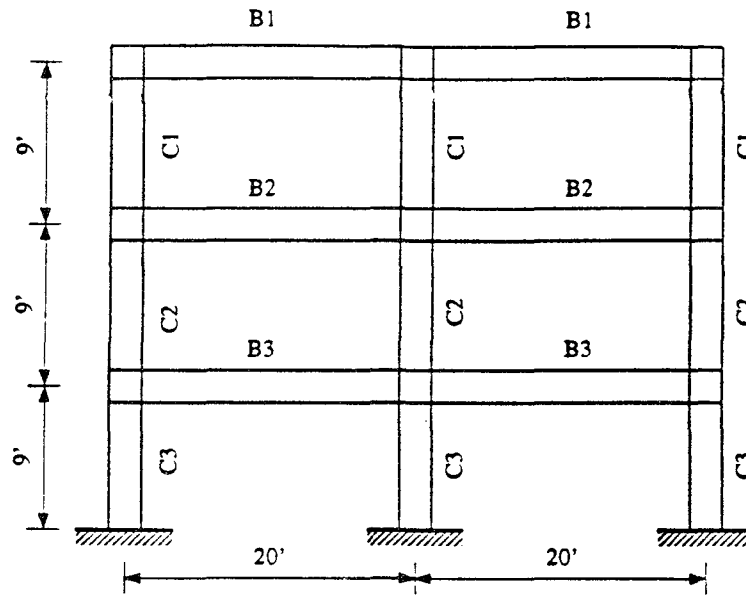
$R_W = 12$  : for special moment-resisting space frame

$C = 1.25S/T^{2/3}$  : for site coefficient and structural period

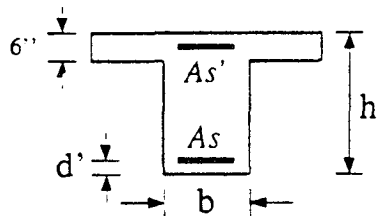
$S = 1.50$  : for soft to medium stiff clay

$W$  : is the dead weight

Details of this building frame, such as cross sections of the members and material properties, can be found in figure 4-1. The Rayleigh damping parameters have been chosen so that the damping is 8% of the critical. The dead load has been applied as static loads and fixed end bending moments on the nodes.



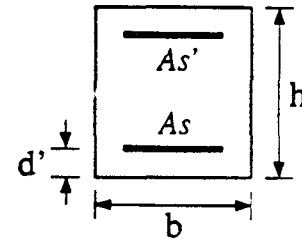
**ELEVATION**  
Frame spacing 20'



**B E A M**

$$f_{sy} = 60ksi$$

$$f'_c = 4ksi$$



**C O L U M N**

	d'	As	As'	b	h
	( in )	( in <sup>2</sup> )	( in <sup>2</sup> )	( in )	( in )
B1	2.0	1.760	2.540	12.0	20.0
B2	2.0	1.760	2.540	12.0	20.0
B3	2.0	1.760	2.540	12.0	20.0

	d'	As	As'	b	h
	( in )	( in <sup>2</sup> )	( in <sup>2</sup> )	( in )	( in )
C1	1.5	2.54	2.54	12.0	15.0
C2	1.5	2.54	2.54	12.0	15.0
C3	1.5	2.54	2.54	12.0	15.0

**FIGURE 4-1 Details of the Two Bay Three Story Building Frame**  
( 1 in = 2.54 cm ; 1 kip = 4.448 kN ) [21]



#### **4.1.2 Three Bay Four Story Buiding Frame**

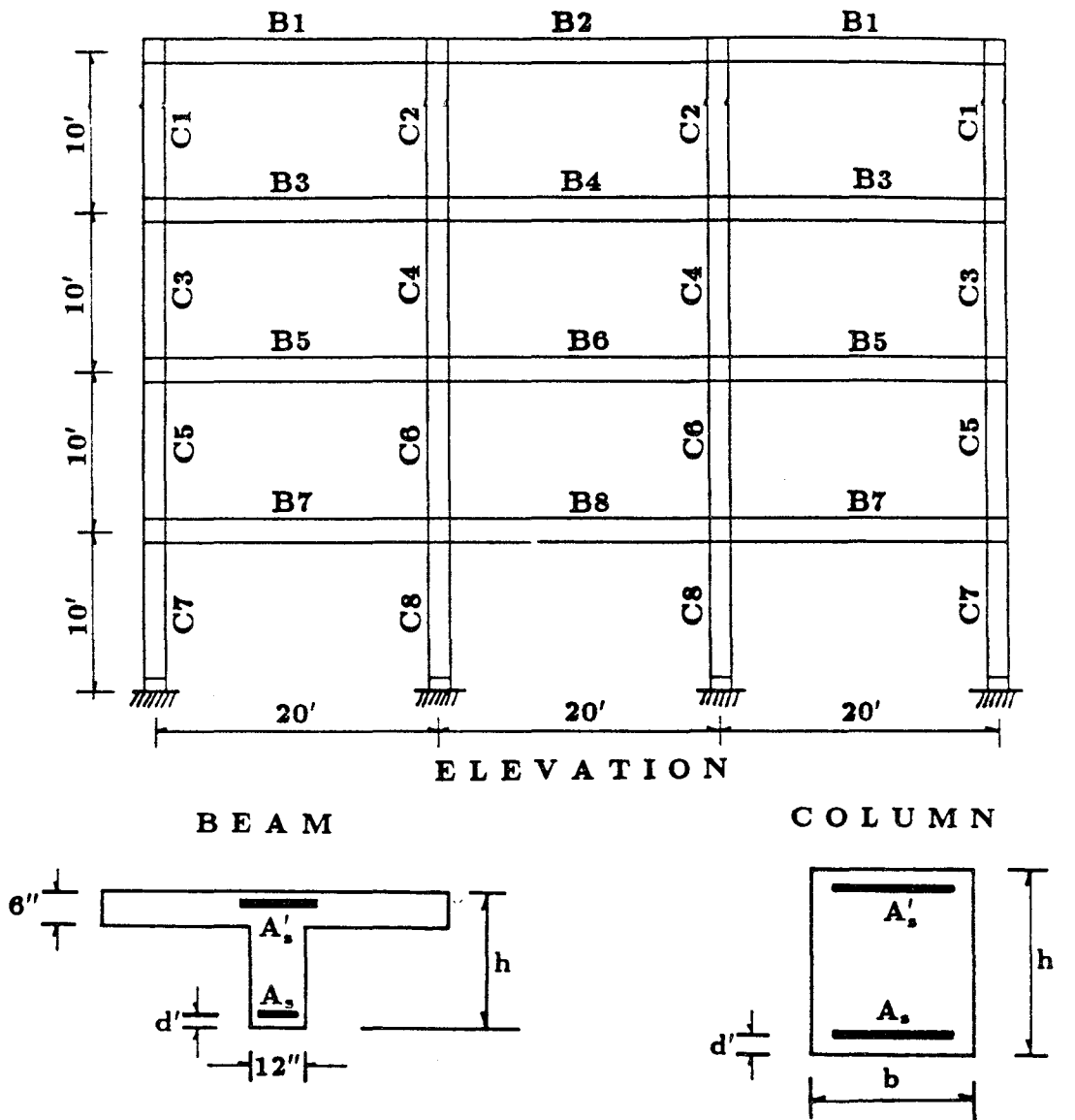
The building frame described in Reference [7] has been used. This typical office building was also designed according to the ACI 318-83 code [1], to resist the equivalent static lateral loads specified in the Uniform Building Code [25] for seismic zone 4. The occupancy importance factor was one. Figure 4-2 shows its dimensions, amount of reinforcement, and material properties. The Rayleigh damping parameters have been chosen so that the damping is 8% of the critical. The dead load has been applied as static loads and fixed end bending moments on the nodes.

#### **4.1.3 Three Bay Four Story Buiding Frame (Weak Columns)**

The three bay four story buiding frame described in the previous section, presents strong columns and weak beams. In order to extend the scope of this study to the case of frames with weaker columns, the same frame with the reinforcement of the columns reduced by 50% has also been considered. All the other dimensions and cross sections can be seen in figure 4-2.

### **4.2 Input Ground Acceleration**

Two types of input acceleration have been used: scaled versions of the N-S component of the acceleration history recorded at El Centro during the Imperial Valley Earthquake (1940), and artificially generated earthquakes using an ARMA model according to the method proposed by Ellis and Cakmak [12 and 13]. The parametric relationships between modeling parameters and physical variables were obtained from a set of strong motion accelerograms recorded from the following Japanese earthquakes: Tokachi-Ochi (1968), Miyagiken-Oki (1978), Nihonkai-Chubu (1983) and Michoacan (1985) [12]. Single event earthquakes have been generated using this capability of the program SARCF-III. The input parameters and their values used in this case are: an initial peak time of



	$d'$	$A_s$	$A'_s$	$h$
	(in)	(in <sup>2</sup> )	(in <sup>2</sup> )	(in)
B1,B2	2.0	1.596	1.596	18.0
B3,B4	2.0	2.400	2.400	20.0
B5,B6	2.0	2.622	2.622	22.0
B7,B8	2.0	2.736	2.736	22.0

	$d'$	$A_s$	$A'_s$	$b$	$h$
	(in)	(in <sup>2</sup> )	(in <sup>2</sup> )	(in)	(in)
C1	1.500	2.160	2.160	12.0	15.0
C2,C3	1.875	2.993	2.993	12.0	18.0
C4,C5,C7	1.875	3.135	3.135	12.0	18.0
C6,C8	1.875	3.260	3.260	12.0	18.0

**FIGURE 4-2 Details of the Three Bay Four Story Building Frame**  
 ( 1 in = 2.54 cm ; 1 kip = 4.448 kN ) [7]

two seconds, a duration of the earthquake of 20 seconds, a distance from the epicenter of 10 or 100 kilometers, different values of the earthquake magnitude, and a soil condition factor,  $\gamma_f$ , with a value of 0.10.

A total of 29 different earthquakes have been applied to the three structural models, a complete list of them with their peak ground accelerations follows. In order to study the onset of seismic damage, several quakes with a similar peak ground acceleration have been utilized.

1. 3 story building

a. ARMA method (D = 10 kilometers). PGA (g): 0.46, 0.50, 0.70, 0.71, 0.72, 0.72 and 0.82

b. ARMA method (D = 100 km.). PGA (g): 0.45, 0.69 and 0.81

2. 4 story building

a. El Centro. PGA (g): 0.25, 0.35, 0.50, 0.75 and 1.0

b. ARMA method (D = 10 km). PGA (g): 0.26, 0.40, 0.51, 0.70

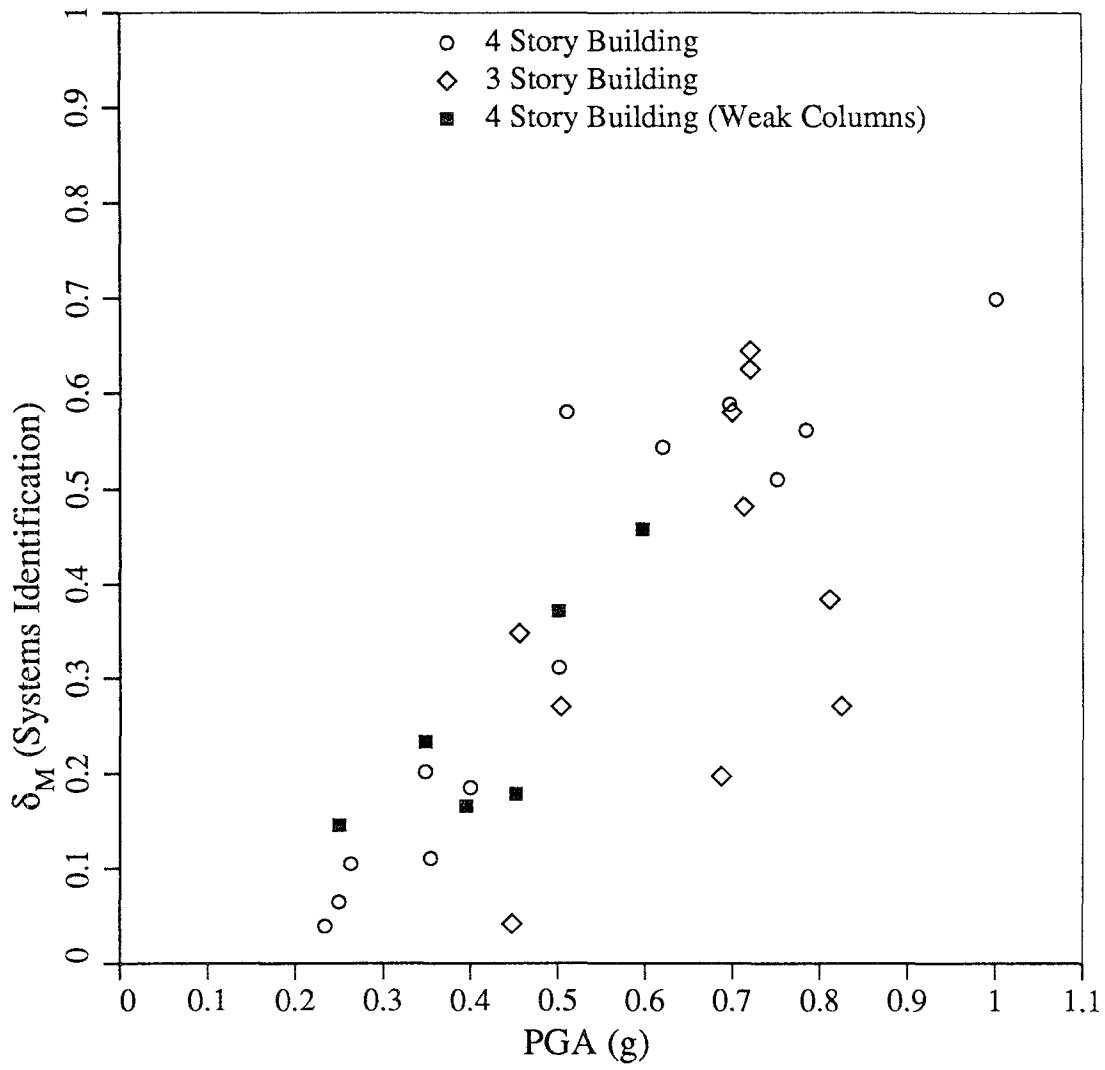
c. ARMA method (D = 100 km). PGA (g): 0.23, 0.35, 0.62, 0.78

3. 4 story building (weak columns)

a. El Centro. PGA (g): 0.25, 0.35, 0.50 and 0.60

b. ARMA method (D = 10 km). PGA (g): 0.40 and 0.45

Each building frame was subjected twice to these time histories. For the second occurrence of the same earthquake the damaged properties were utilized. Even in the case of artificially generated earthquakes, an identical repetition of the same earthquake was used.



**FIGURE 4-3 Maximum Softening vs. Peak Ground Acceleration**

Figure 4-3 shows the peak ground accelerations of the earthquakes that have been applied to each of the building structures that have been considered. The Maximum Softening is also shown. It can be seen how, when artificial earthquakes are used, there is not a clear correlation between the peak ground acceleration and the damage level, even for the same building structure.

### **4.3 Parameters to Be Computed**

For each of the nonlinear dynamic analysis that have been carried out, a vast amount of information can be obtained using the program SARCF-III. From all that information, parameters belonging to four groups have been selected: traditional measures of damage, local damage indices, global damage indices and parameters that characterize the response of the damaged structure to a second earthquake.

#### **4.3.1 Traditional Measures of Damage**

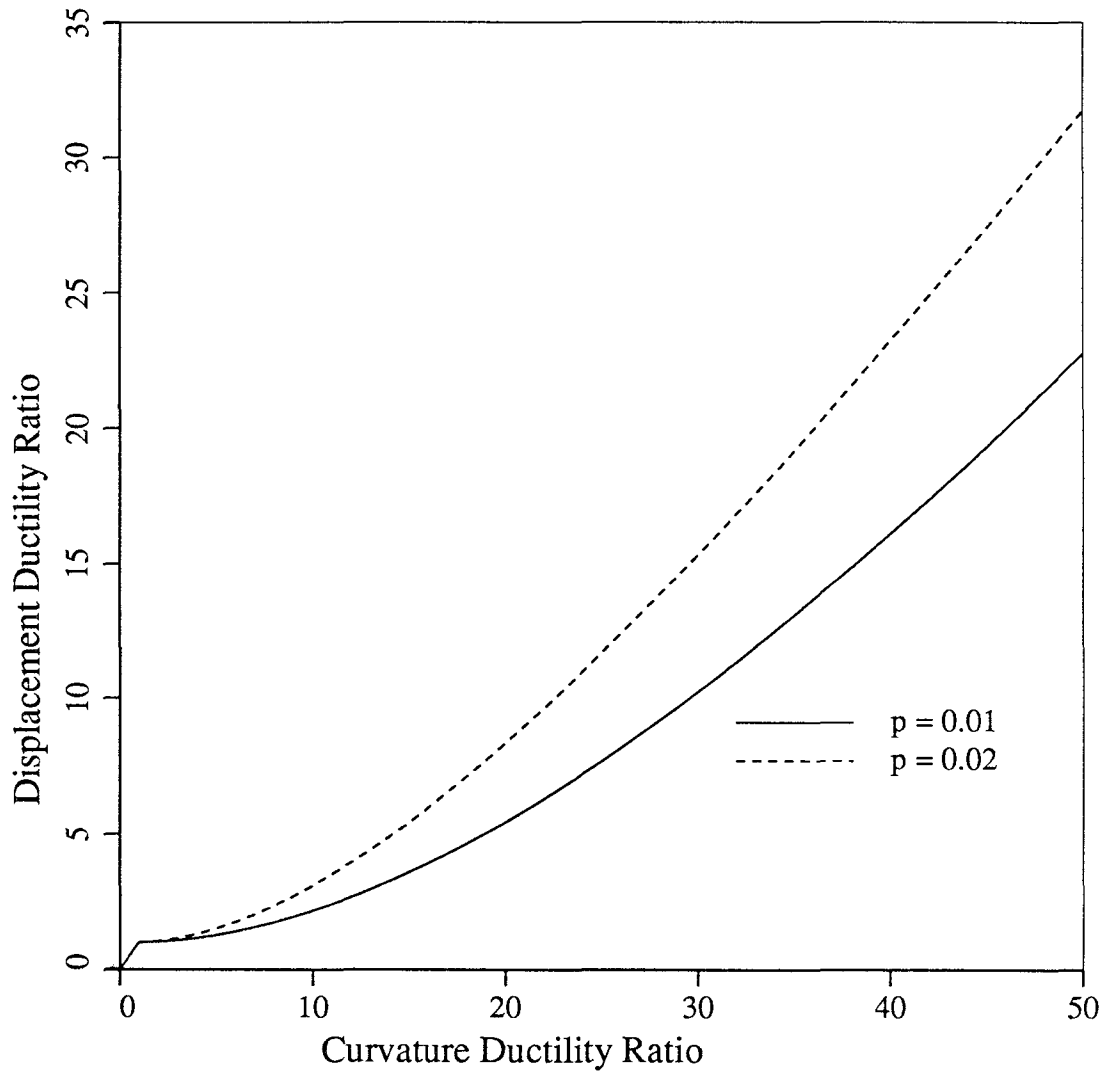
Among the *traditional* measures of damage the maximum interstory drift, the permanent interstory drift and the maximum ductility ratio for beams and columns, have been computed.

The interstory drift is defined as the the tangent of the angle between the original position and the deformed position of the columns. The interstory drift has been used as a measure of damage by M. A. Sozen [22].

The permanent drift is the interstory drift after the earthquake. The permanent drift has been used as an indication of damage by J. E. Stephens and J. P. T. Yao [23 and 24].

The ductility ratio which has been computed is a curvature ductility ratio, defined as the ratio between the curvature and the yield curvature. The relationship between the displacement ductility ratio and the curvature ductility ratio depends on the nonlinear

$$\phi_f = 50 \phi_y$$



**FIGURE 4-4 Curvature vs. Displacement Ductility Ratio**

moment-curvature relationship and the member geometry. For the cantilever beam in figure 2-2, with the bilinear moment-curvature relationship defined in the same figure, the plot in figure 4-4 was obtained. This plot was obtained for a failure curvature 50 times greater than the yield curvature and for a value of the parameter  $p$  (figure 2-2) of 0.01 and 0.02.

One can see in figure 4-4 how the curvature ductility ratio is always greater than the displacement ductility ratio. However, it is not possible to express one as a function of the other since the functional relationship between them depends on the section and on the material properties.

When the failure is controlled by bending moments, as it is for the moment resisting frames that have been analyzed, the use of the curvature ductility ratio seems to be more appropriate.

#### **4.3.2 Local Damage Indices**

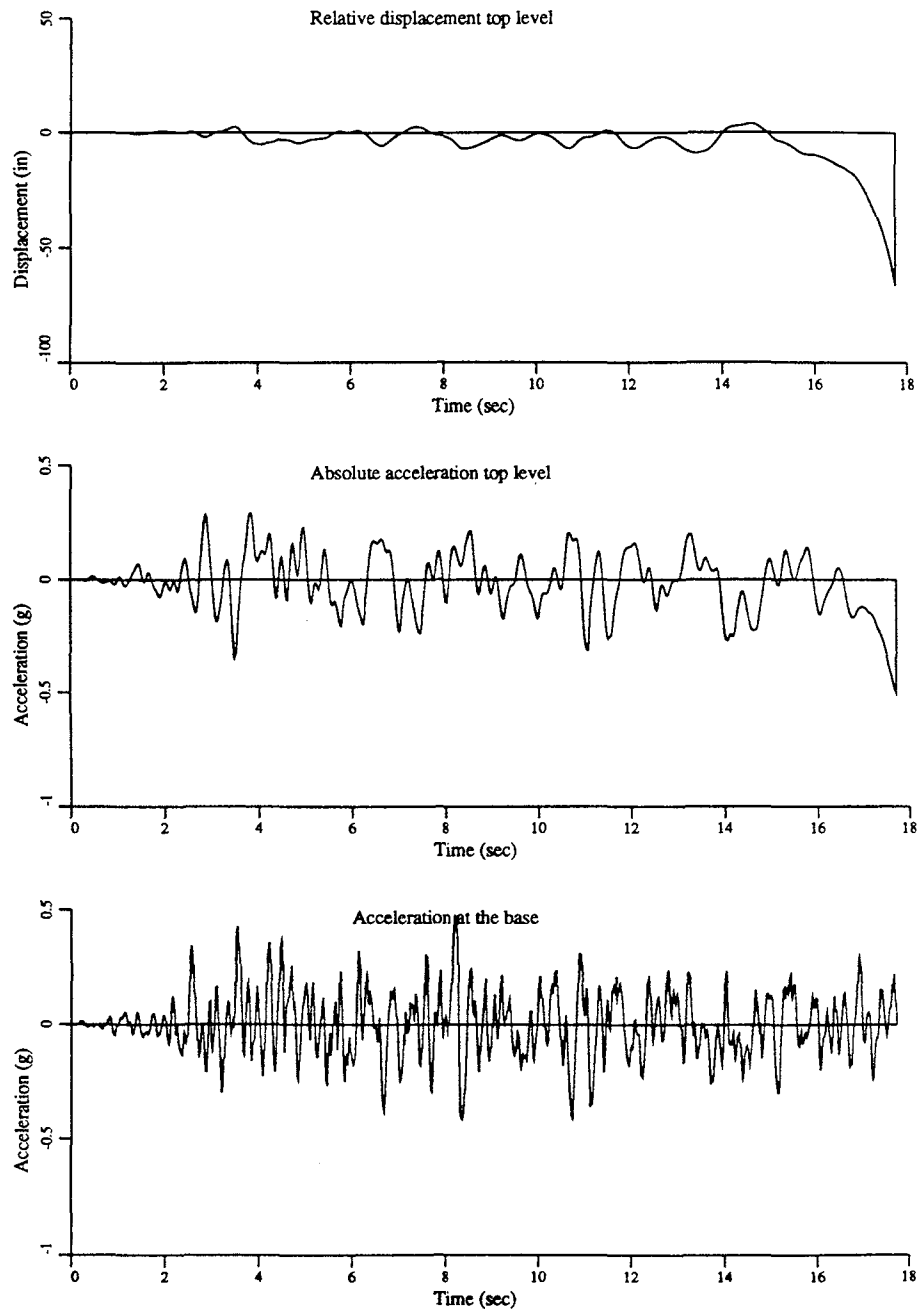
Chung, Meyer and Shinozuka's damage index and the modified Park and Ang's damage index have been computed at both ends of each beam or column. Both indices were described in Section 2.1.

#### **4.3.3 Global Damage Indices**

The global damage indices described in Section 2.2 have been calculated.

1. Energy average of Chung, Meyer and Shinozuka's Local Damage Index, defined by Equation (2.7).
2. Weighted average of Chung, Meyer and Shinozuka's Local Damage Index, using the triangular weighting function, defined by Equations (2.8) and (2.9).

3 BAYS 4 STORIES (weak columns)  $M = 8.5$   $D = 10$  km



**FIGURE 4-5** Acceleration and Displacement Time History in a Case Defined as Collapse



3. Energy Average of Park and Ang's damage index, defined by Equation (2.7).
4. Maximum and Final Softening defined by Equations (2.10) and (2.11). Both indices have been computed in two different ways, using the Systems Identification Program, MUMOID, and computing a moving average of the instantaneous natural period.

#### **4.3.4 Response of the Damaged Structure to a Second Earthquake**

The response of the building frames to a second identical earthquake is analyzed in order to obtain an objective measure of damage independent from all the damage indices which have been previously considered. The first concern in the post-earthquake evaluation of damaged structures is the assessment of the damaged structure's ability to safely withstand the occurrence of a similar future earthquake. The idea is to evaluate the damaged structure's performance for the second earthquake in a simple way, classifying the structure after the second quake as either a collapsed or a standing structure.

The failure of structural elements has been included in the computer code SARCF-III in such a way that when the failure curvature of a structural element is exceeded, its bending stiffness is reduced to a small number. When this happens to the most important elements of the system, the displacements increase monotonically. This situation can be observed in figure 4-5, where the acceleration and displacement history of the top level are shown for the second occurrence of an 8.5 magnitude artificial earthquake affecting a 3 bay 4 story building with weak columns. In a few cases, the deformations during the second earthquake were very large, but they were nevertheless periodic. For these few cases, an overall drift greater than 6% has been considered to be equivalent to a state of collapse. This being the definition of collapse used by Roufaiel and Meyer [20].



## SECTION 5

### ANALYSIS OF THE RESULTS

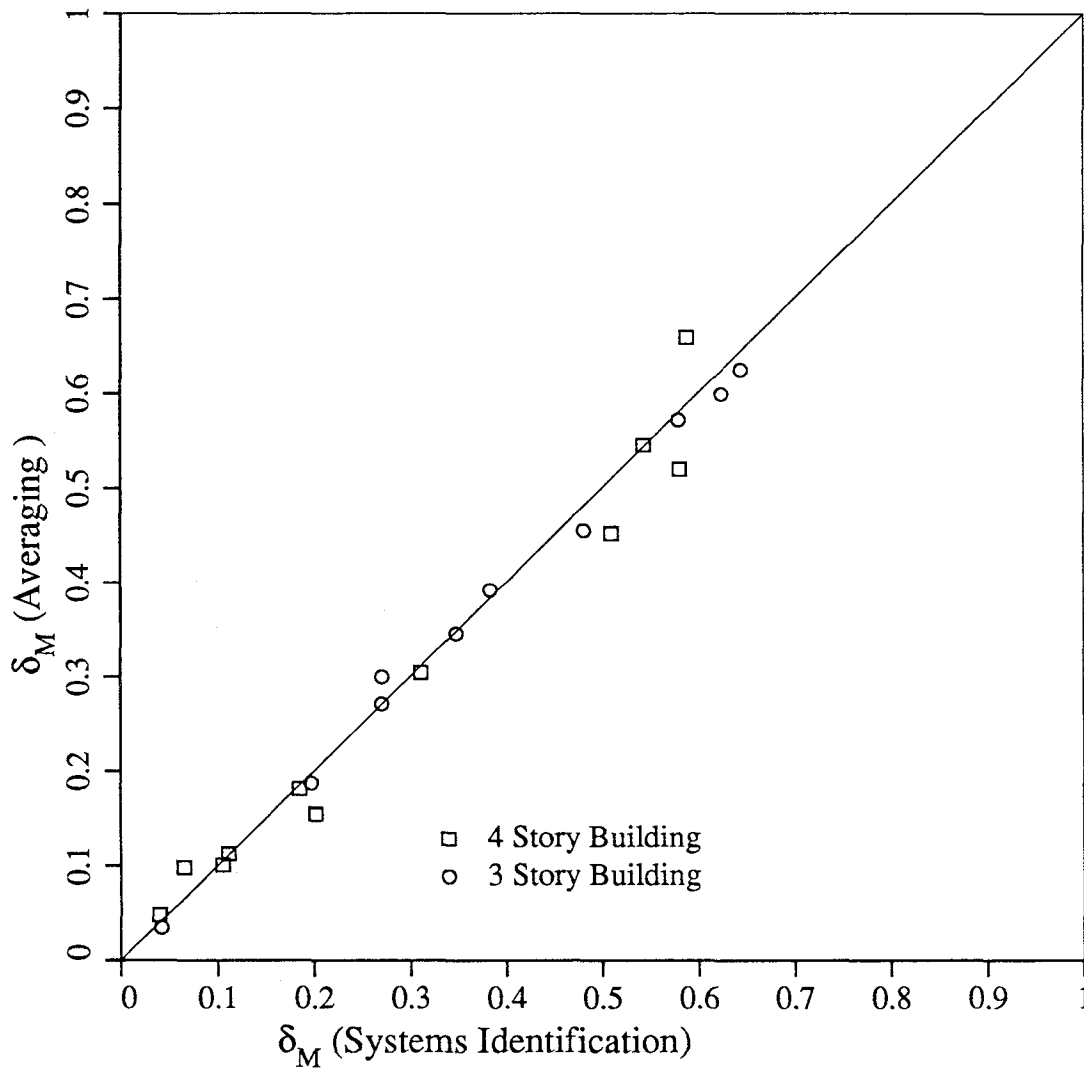
In this section the results of the numerical simulation of the earthquake response of the building structures will be analyzed.

#### 5.1 Systems Identification Program vs. Moving Average

As mentioned in Sections 4.3.2 and 4.3.3, two different methods have been used for the computation of the Maximum and Final Softening. The first one is the use of the systems identification program, MUMOID [9], and the second one is the computation of a moving average of the instantaneous natural period.

This second approach is more advantageous during the design stage, when only a computer model is available. It is also useful in reliability studies carried out by Monte Carlo simulations on computer models of structural systems. The instantaneous natural period can be easily computed from the first eigenvalue of the instantaneous tangent stiffness matrix.

On the other hand, when a damage analysis based on the acceleration recorded at the base and at the top of the building is carried out, the only method for the computation of the Maximum and Final Softening is the systems identification program. This program finds the natural period of an equivalent linear system for a series of non overlapping time windows. The previous work done by DiPasquale and Cakmak has related the value of the Maximum Softening, computed using the systems identification program, to the probability of damage [10]. It has also been shown, from a Continuum Mechanics approach, that the global damage indices based on the vibrational parameters are related to the local stiffness degradation through operations of averaging over the body volume.



**FIGURE 5-1 Maximum Softening. System Identification Program vs. Moving Average**

### Systems Identification Program vs. Moving Average

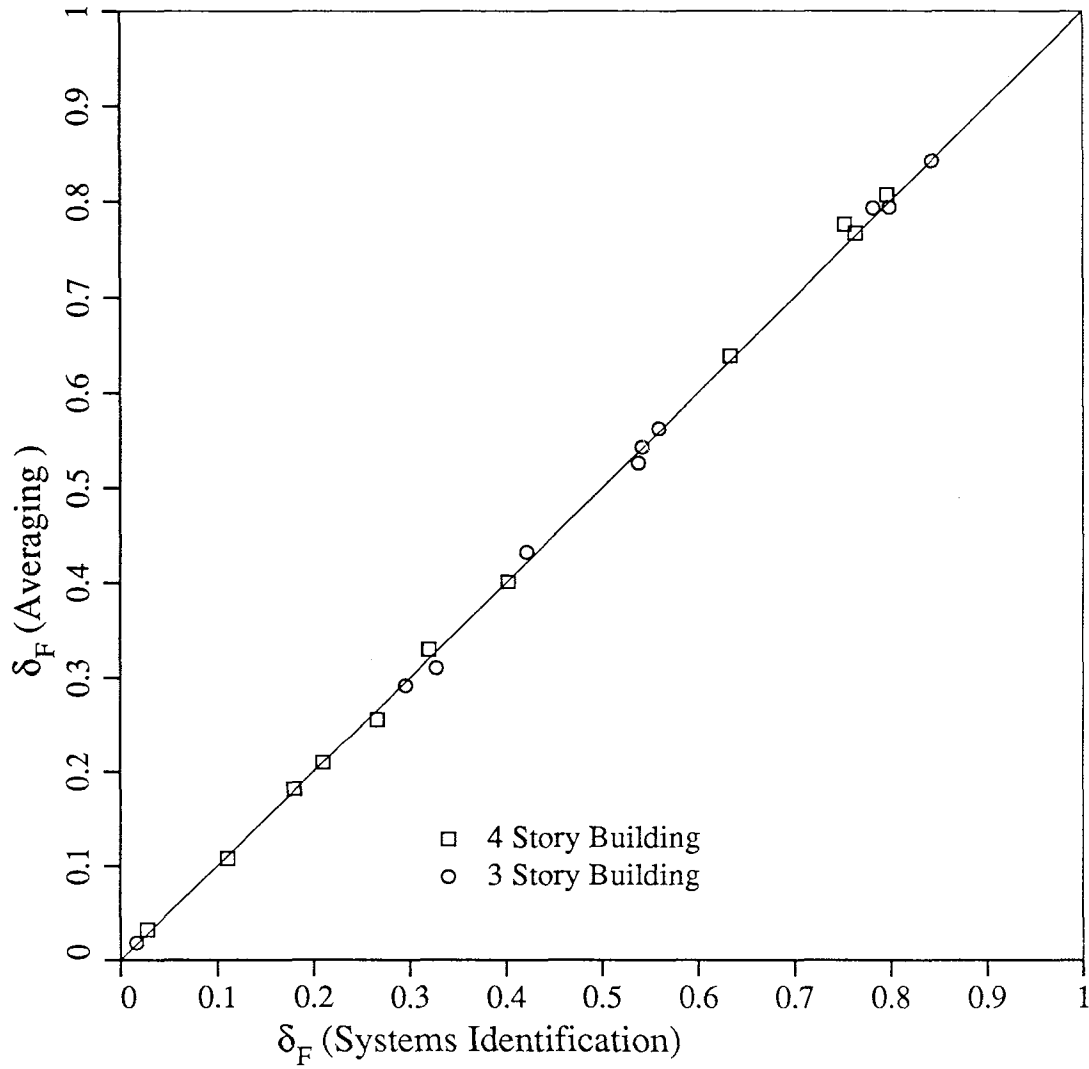


FIGURE 5-2 Final Softening. System Identification Program vs. Moving Average

These two methods for the computation of the Maximum and Final Softening come from different definitions and it is important to know what the relationship is between the results obtained by their usage.

Figure 5-1 shows the correlation between the Maximum Softening,  $\delta_M$ , obtained using these two methods, for the database created from the numerical simulations of the building frames earthquake response. One can see by looking at figure 5-1 that, from a practical point of view, these two methods for the computation of the Maximum Softening are equivalent. Greater differences between the two methods occur in the 3 bay 4 story building for values of the Maximum Softening greater than 0.5. As will be shown later, a value of the Maximum Softening greater than 0.5 implies a high degree of damage. Therefore, the exact value for a damage index greater than 0.5 it is not overly significant.

Figure 5-2 shows the correlation between the Final Softening,  $\delta_F$ , obtained by using the same two methods. Since the Final Softening depends only upon the initial and final natural periods, the results obtained by using these two methods are closer than in the case of the Maximum Softening. These two methods can be considered to be equivalent.

## 5.2 Maximum Softening vs. Traditional Measures of Damage

In this section, the Maximum Softening, as a global damage index, will be compared to four *traditional* measures of seismic damage. The *traditional* measures of seismic damage that have been considered are: the maximum interstory drift, the maximum permanent or final drift, and the maximum ductility ratio for beams and columns.

This comparison has been done by means of series of plots that show the value of the Maximum Softening as a function of the other damage indicator (See figure 5-3). Each point in the graphs has been obtained from the nonlinear dynamic analysis of any of the building frames described in Section 4.1, for the first occurrence of the input ground motions described in Section 4.2.

Percentage of damaged structures =  $(2\gamma - 1)/0.04$  (Sozen, 1981)

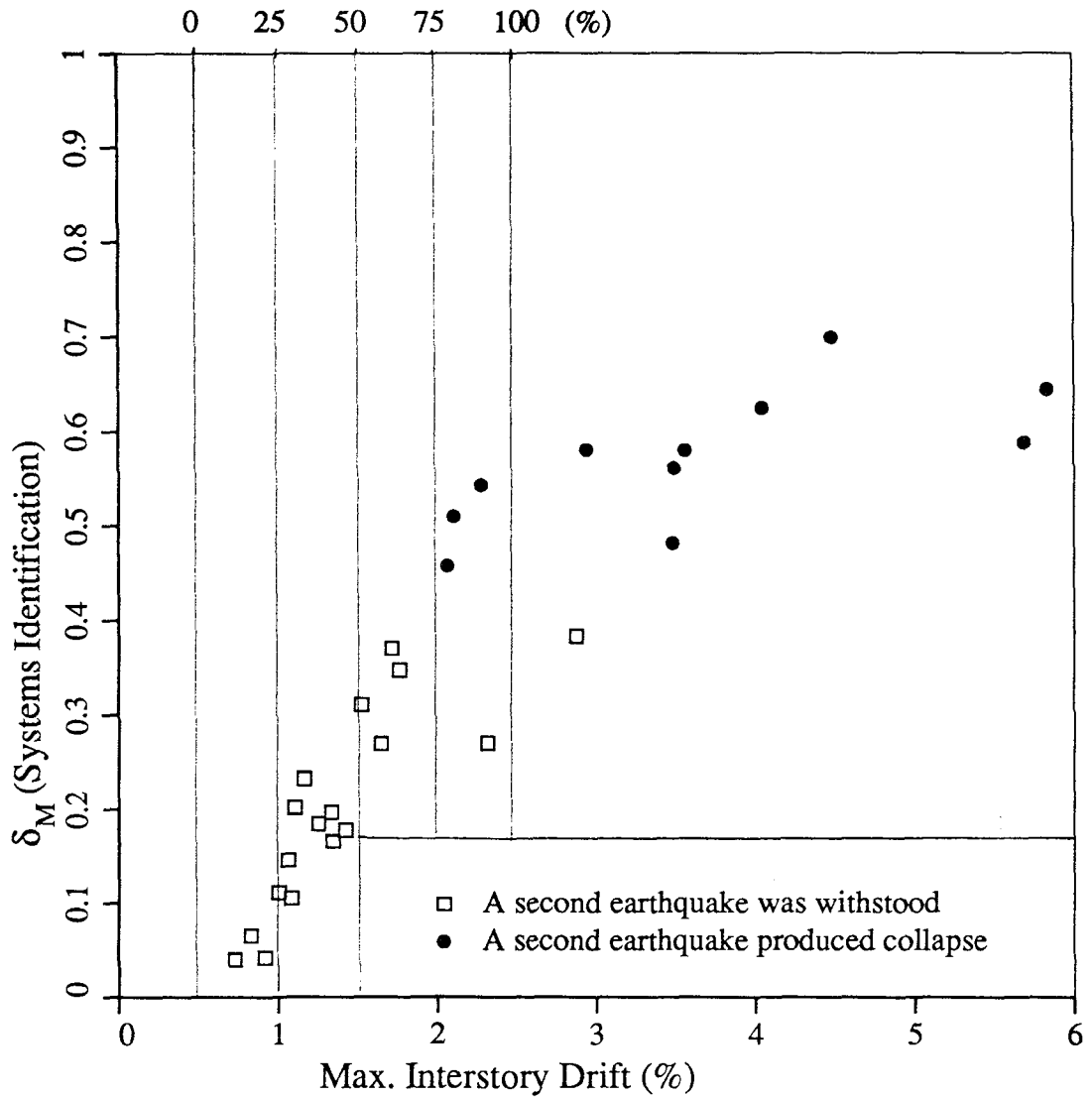


FIGURE 5-3 Maximum Softening vs. Maximum Interstory Drift

The filled circles represent the cases for which the second occurrence of the same earthquake produced collapse, according to the definition of collapse in Section 4.3.4. However, the filled circles correspond to the damage indices that were computed for the first earthquake.

If whether or not the structure collapses in the second earthquake is considered to be an objective measure of the level of damage in the first earthquake, the best global damage index would be the one that can predict the collapse of the structure in the second earthquake. In that case, there should be a cutoff value of that damage index so that a collapse resulting from the second identical earthquake only occurs for values greater than that cutoff value.

In the previous work done by DiPasquale and Cakmak [10], the probability of damage was found as a function of the Maximum Softening. Using 25 seismic simulation experiments performed at the University of Illinois at Urbana-Champaign, they found that the serviceability limit state was related to an average value of the Maximum Softening of 0.43. This criterion was also used for the damage analysis of shaking table experiments performed at the University of California at Berkeley, and of strong motion records from the San Fernando (1971) and the Imperial Valley (1979) earthquakes, giving results consistent with the actual damage observed.

This damage model was later extended to the identification of different damage states [11], using the information contained in the same experiments performed at the University of Illinois at Urbana-Champaign.

With the numerical simulations of the seismic response of moment resisting building frames performed for this study, a larger data base for the calibration of the Maximum Softening as a global damage index is available. The new information indicates that in all the cases for which the Maximum Softening is greater than 0.4 the second occurrence of the same earthquake produced a collapse.



The correlation of the Maximum Softening with other measures of damage will be obtained in the next subsection.

### 5.2.1 Maximum Interstory Drift

The interstory drift has long been considered to be an indication of seismic damage. A limitation of the drift has been recommended for the seismic design of buildings to avoid damage to nonstructural elements and to limit the inelastic deformations. In this study, the maximum interstory drift has been compared to the Maximum Softening as a global damage index.

Figure 5-3 shows the results of this comparison. The definition of the percentage of damaged structures for a given interstory drift proposed by Sozen [22], has also been included. According to M. A. Sozen, the acceptability quotient,  $A$ , is given by

$$A = (5 - 2\gamma)/4 \quad (5.1)$$

where,

$A$  : Fraccion of structures expected to remain safe

$\gamma$  : Maximum story drift in percentage

One can see in figure 5-3 how in all the cases a value of the Maximum Softening larger than 0.4 implies a collapse in the second identical earthquake according to the definition of collapse of Section 4.3.4. However, there is not a value of the maximum interstory drift that separates the structures that collapse in the second earthquake. A good correlation is observed between the two definitions of damage in the sense that an interstory drift of 1%, with only 25% of damaged structures according to Sozen, corresponds to a small value of the Maximum Softening (0.1). The average value of the maximum interstory drift that implies collapse in the second run is about 2.5%, value that would imply 100% of damaged structures according to Sozen.

Yao's definition of damage (1983)

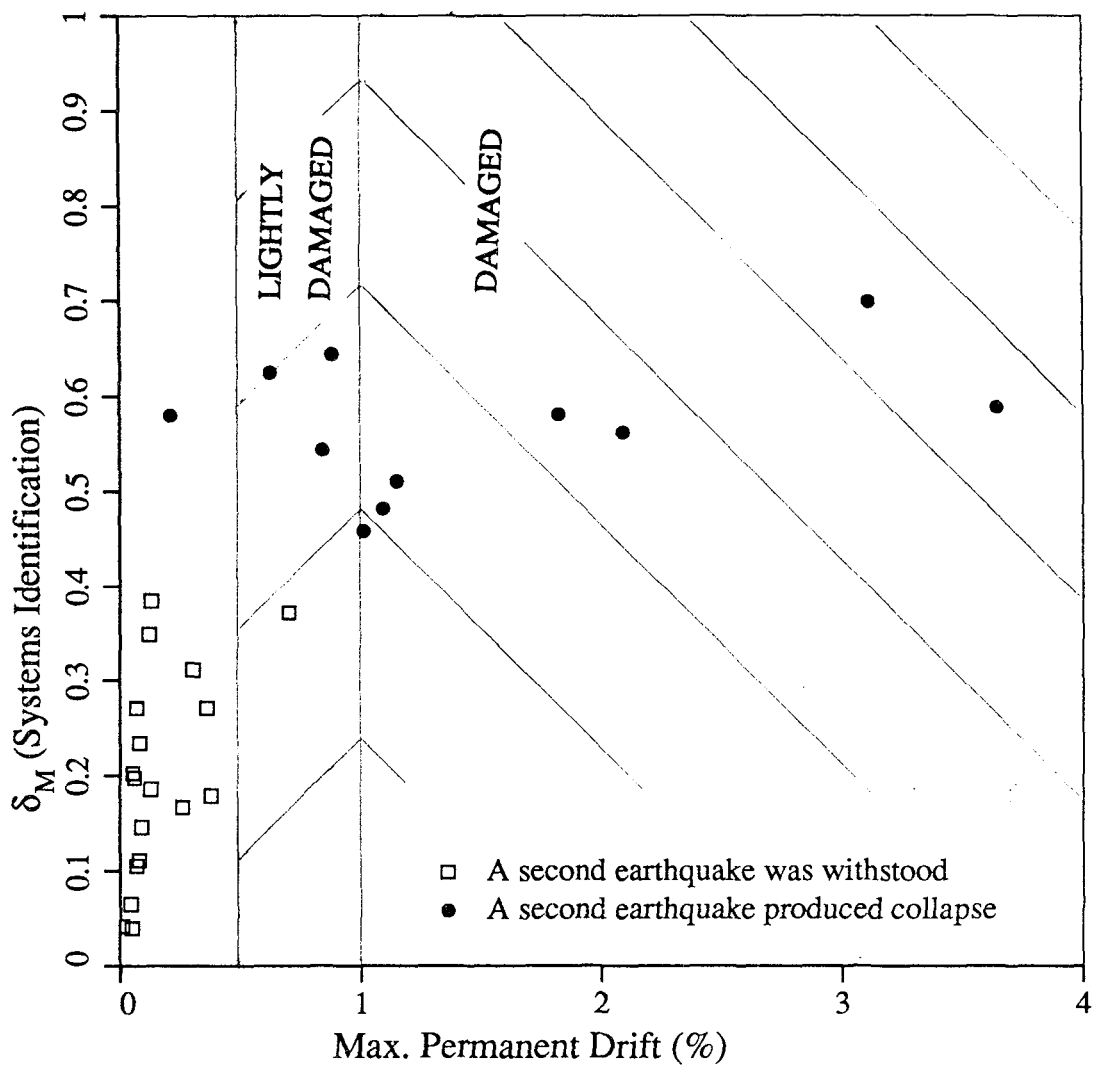


FIGURE 5-4 Maximum Softening vs. Maximum Final Drift

### 5.2.2 Maximum Final Drift

The maximum final or permanent drift is closely related to the plastic deformations in a structural system.

Toussi and Yao introduced a qualitative classification of damage, which among other things included the permanent drift experienced by building structures [23 and 24].

They defined four levels of structural damage as follows:

1. Safe

Cracks less than 0.05 mm wide. No new cracks that open. No macroscopic or global nonlinearities. The structure “stays stiff”, the vibration of the upper floors does not reflect the irregularities of the base motion. The story drift does not exceed 1% of the story height.

2. Lightly Damaged

Flexural cracks open, width less than or equal to 0.1 mm. The motion of the upper floors reflects the irregularities in the base motion. Permanent displacements can be measured and are approximately 0.5% of the story height.

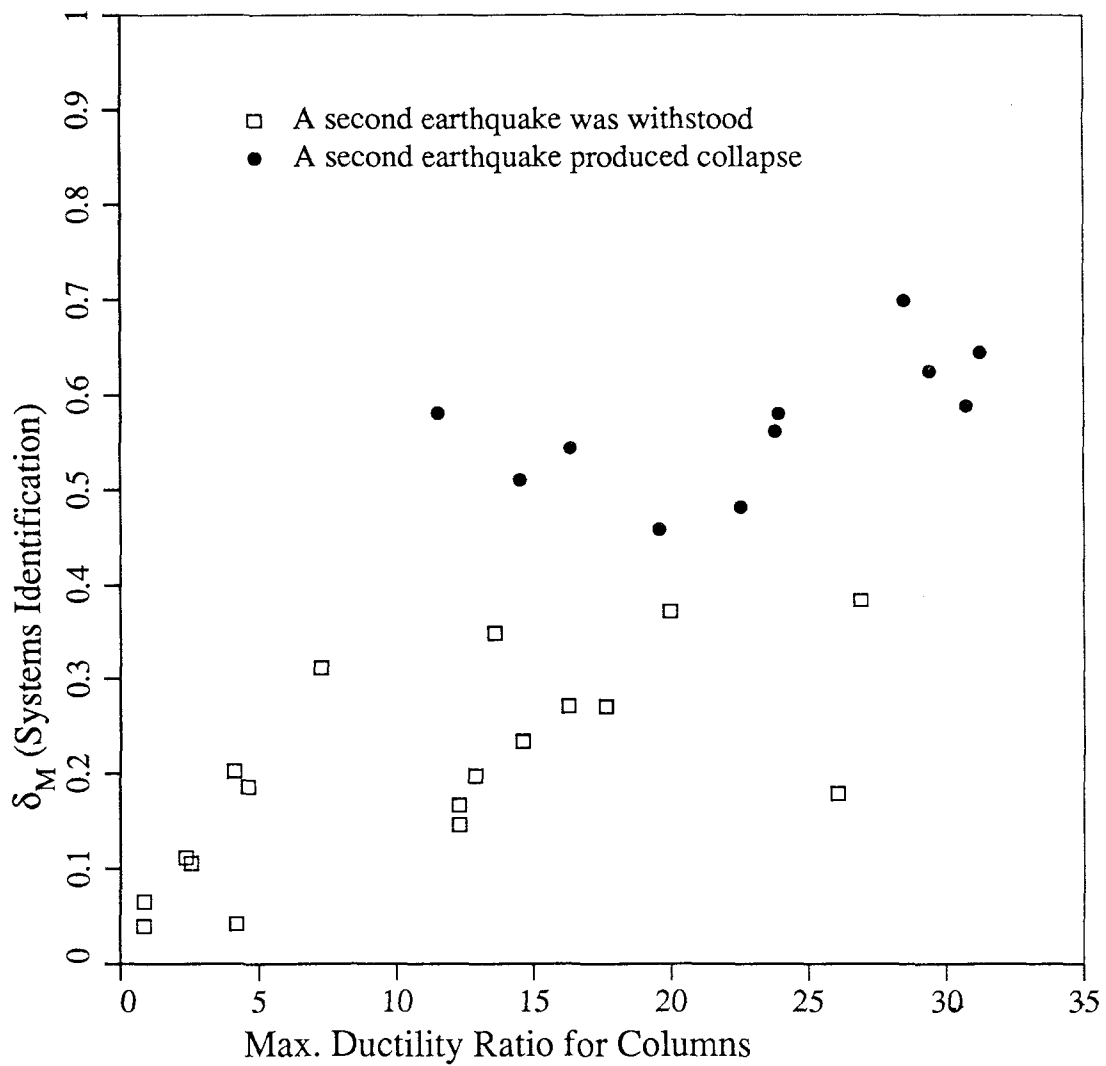
3. Damaged

Cracking is extensive, crack width of the order of 0.3mm. Possible local spalling. Permanent displacements around 1% of the story height.

4. Critically Damaged

Crack width of 0.4 mm and beyond, crushing, spalling of several elements. Top story displacement shows some aperiodicity at the end of the record. Poor correlation between base shear and top level displacement.

In figure 5-4, the Maximum Softening versus the maximum permanent drift has been plotted. The lines which represent the damaged and lightly damaged structures, according to the previous classification, have also been included.



**FIGURE 5-5 Maximum Softening vs. Maximum Ductility Ratio for Columns**

From this figure it can be concluded that the value of the Maximum Softening provides a better separation between the structures which will collapse with a repetition of the same earthquake and the structures which will withstand that second earthquake.

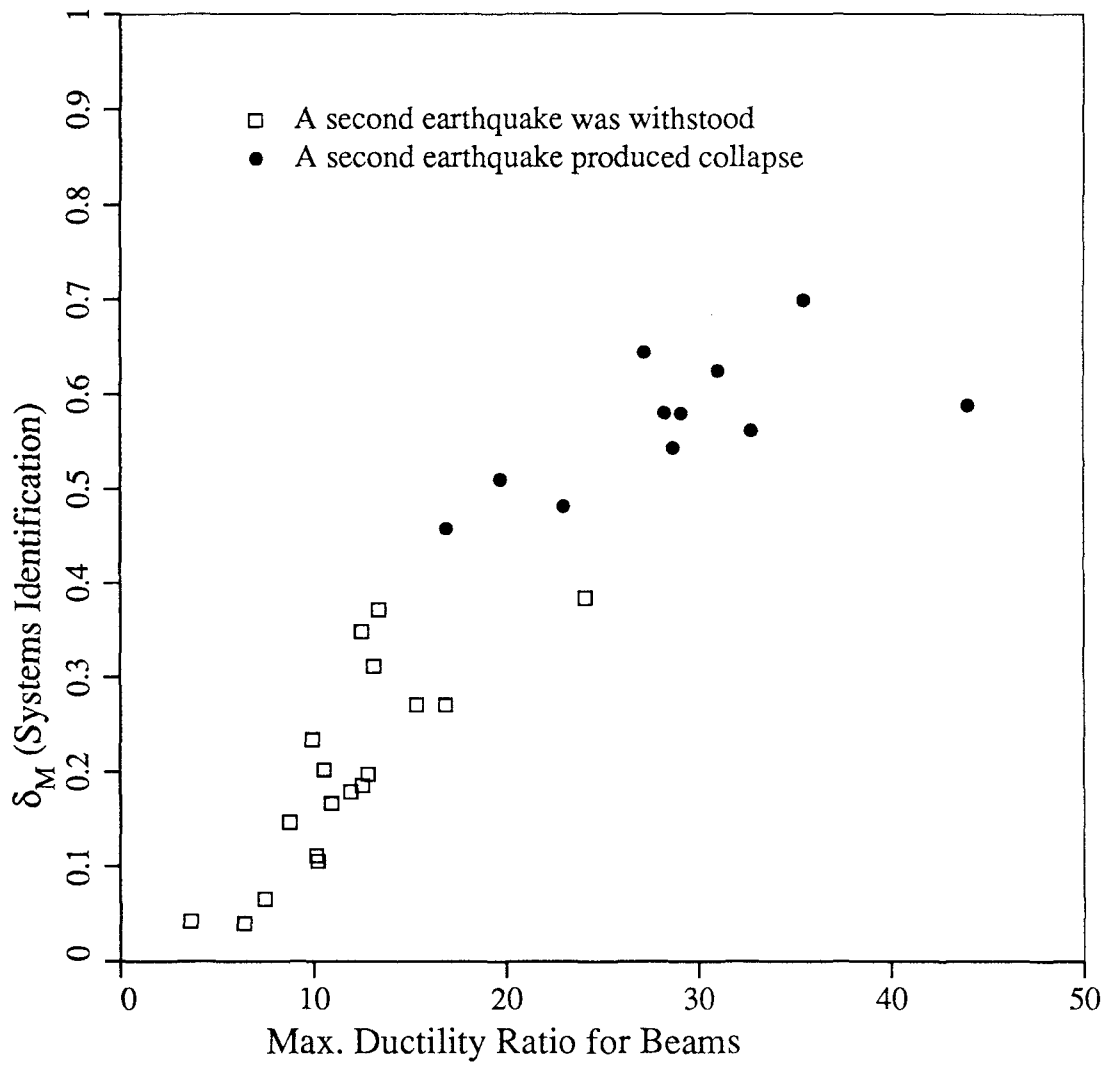
It can be observed that all but one of the runs with a Maximum Softening smaller than 0.4 had a maximum permanent drift of less than 0.5%. However, the maximum permanent drift of the structures with a Maximum Softening greater than 0.4 have a maximum permanent drift ranging from less than 0.5% to greater than 3%. A small level of damage implies a maximum permanent drift less than 0.5%, but not vice versa. This shortcoming of the maximum permanent drift as a measure of damage seems to come from the fact that even a badly damaged structure may present no permanent drift, even after strong plastic deformations.

### **5.2.3 Maximum Ductility Ratio for Beams and Columns**

The ductility ratio is frequently used as a measure of seismic damage. This concept is very useful in the design of earthquake resistant structures when using elastic models. The ductility ratio, which is the ratio between the maximum deformation and the yield deformation, can be defined as a displacement, rotation or curvature ductility ratio.

Figure 4-3 shows the relationship between the displacement ductility ratio and the curvature ductility ratio for the case of a cantilever beam with a load at the end. The curvature ductility ratio applies only to the most damaged section along the member and does not reflect the overall state of damage of the member. H. Banon *et al.* [2] compared the curvature ductility to other damage measures and concluded that it was one of the least reliable since it does not take into consideration any stiffness or strength degradation.

Reference [2] lists the curvature ductility ratio at failure for 32 specimens tested in laboratory. The average curvature ductility ratio at failure was 14.5, but presented a high variability with values from 2.1 to 35.4.



**FIGURE 5-6 Maximum Softening vs. Maximum Ductility Ratio for Beams**

In figures 5-5 and 5-6 one can see the maximum ductility ratio for columns and beams, respectively, versus the Maximum Softening.

The correlation between the maximum ductility ratio for the columns and the Maximum Softening is very poor. The high variability of the curvature ductility ratio mentioned before can be clearly observed. Structures that collapsed during the second earthquake, according to the definition of collapse in Section 4.3.4, have maximum ductility ratio values for columns ranging from 10 to 30.

The correlation between the maximum ductility ratio for beams and the Maximum Softening is much better than that for columns. The Maximum Softening is able to predict whether or not a second identical earthquake will produce a collapse, since it is possible to draw a horizontal line that separates the squares and the filled circles. Nevertheless, it is not possible to draw a vertical straight line that serves the same purpose.

The average value of the curvature ductility ratio which separates the structures that collapsed during the second earthquake, is between 15 and 20.

### **5.3 Maximum Softening vs. Weighted Averages of Local Damage Indices**

In this section, two attempts to define a global damage index are compared. The Maximum Softening, which depends on the change that occurs in a structural system's natural period, is compared to three weighted averages of local damage indices.

Local damage indices are indispensable for the identification of the damage level of individual elements. In the design process, local damage indices can highlight the elements that should be modified. However, it is very difficult to get a clear idea of a structural system's response to a given input ground motion from a long list of elemental damage indices. Global damage indices are necessary for post-earthquake evaluation of existing structures, reliability studies and design of new structures.

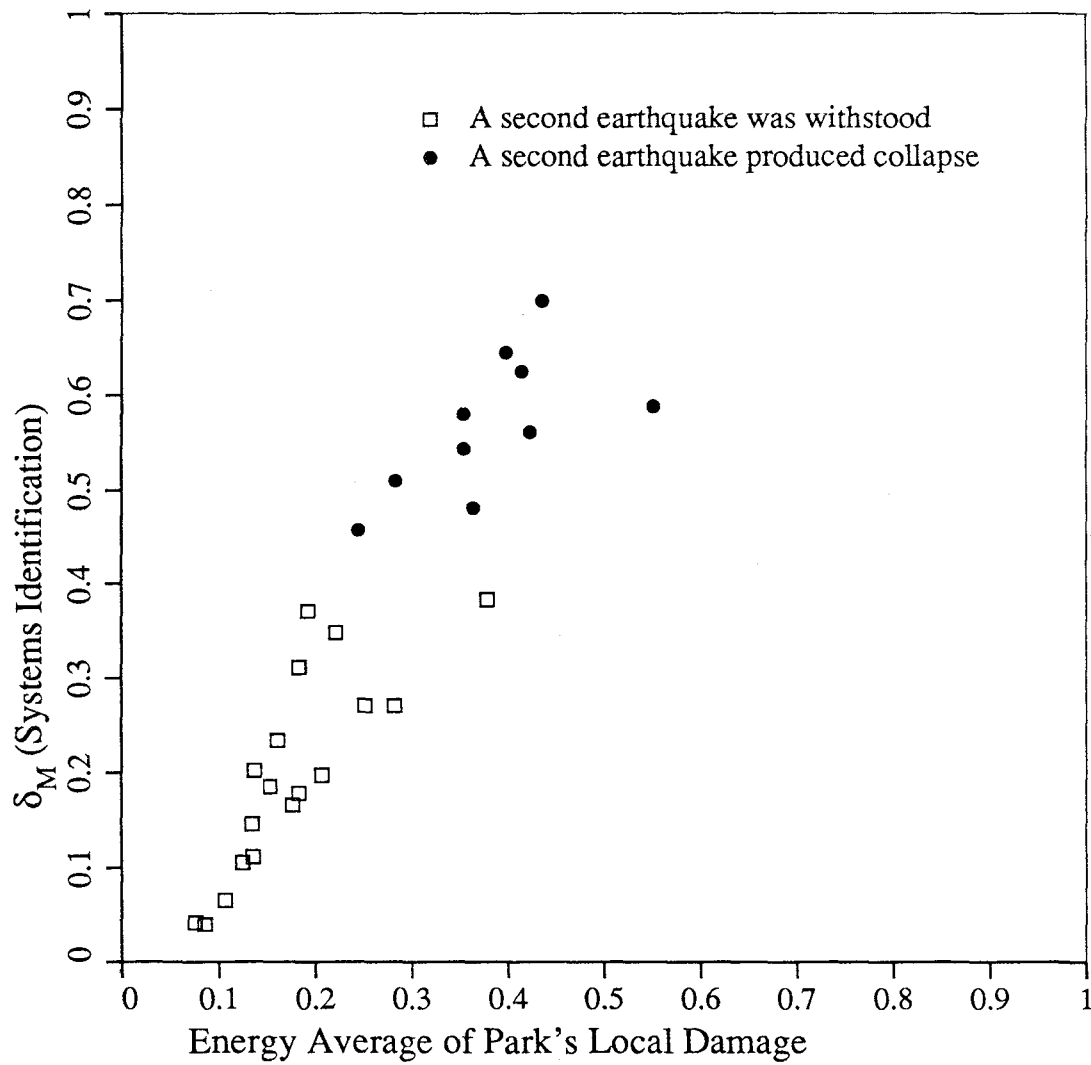


FIGURE 5-7 Maximum Softening vs. Energy Average of Park's Index



The global damage indices described in Section 2.2.1, were proposed to fill this necessity, and are based on the computation of a weighted average of the local damage.

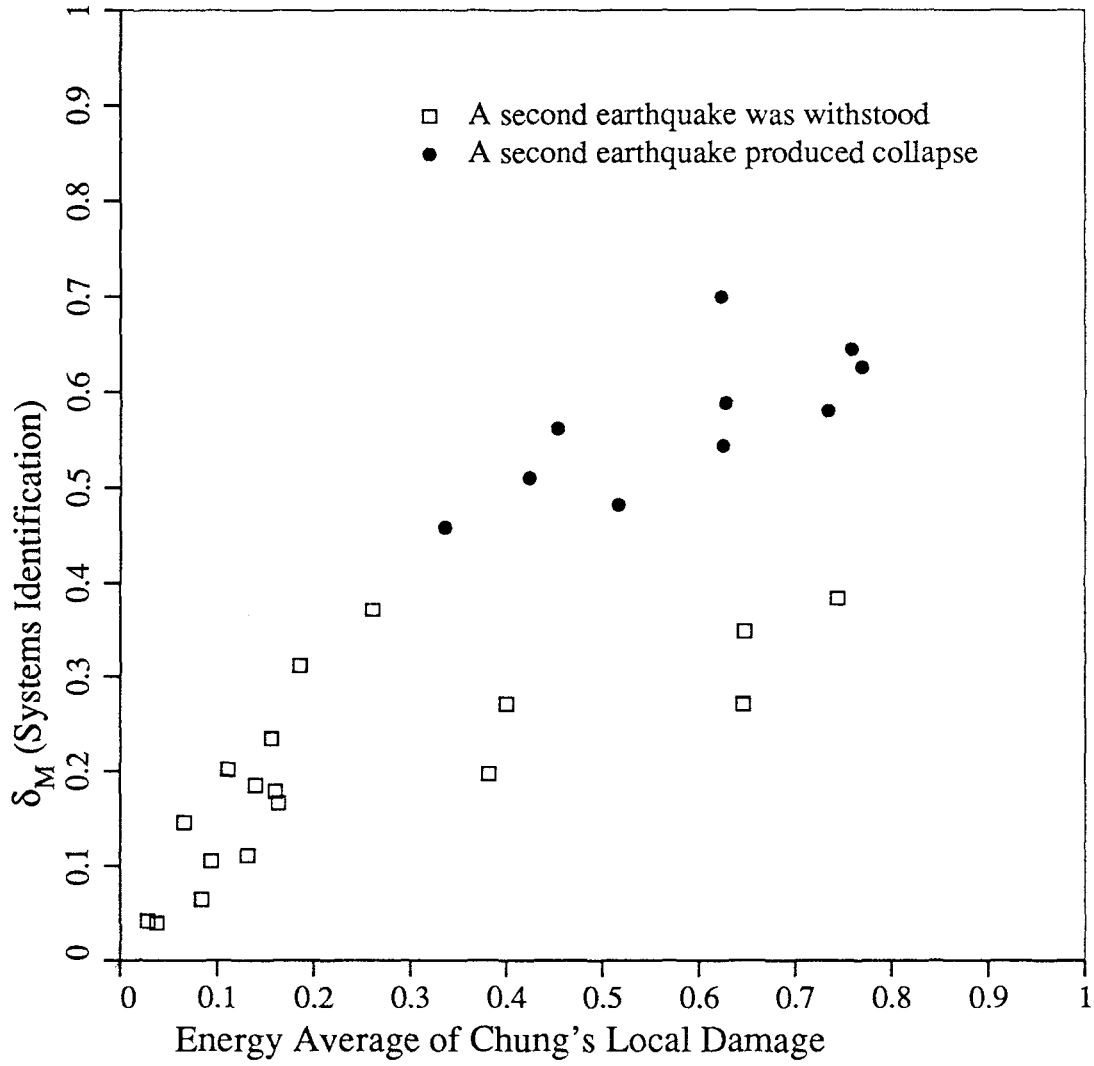
Local damage indices for reinforced concrete structures usually have complicated definitions because they have to characterize the state of damage of such a complex system as a reinforced concrete member. The remaining capacity of a reinforced concrete member depends on the deformation level, the energy dissipated and the number and intensity of the loading cycles. For a given ground motion, all this information is available when a computer model of a structure is being used, but in the evaluation of existing structures many problems arise. The damage analysis of existing structures requires the building of a computer model of a complex existing structure with many sources of uncertainty and it is necessary to have a record of the actual ground motion.

The use of the Maximum Softening as a global damage index has the advantage that it can be computed directly from the acceleration records at the base and at the top of the building. In evaluating damage in computer models, the procedure for the Maximum Softening's computation is independent of the definition of the hysteresis loops. Therefore, its computation can be easily implemented in any computer code.

### **5.3.1 Energy Average of the Modified Park and Ang's Index**

Figure 5-7 shows the relationship between the energy average of the modified Park and Ang's index, defined by Equation (2.6), and the Maximum Softening.

According to Reference [19], a range of Park's damage index of between 0.4 and 1.0 represents severe damage characterized by extensive crushing of the concrete and disclosure of buckled reinforcement. A damage index just below 0.4 represents moderate damage with extensive large cracks and spalling of the concrete. For smaller damage indices, the damage results in minor cracks and partial crushing of the concrete in the columns.



**FIGURE 5-8 Maximum Softening vs. Energy Average of Chung's Index**

Structures with a damage index below 0.4 have a substantial reserve capacity before total collapse and some reserve capacity before irreparable damage.

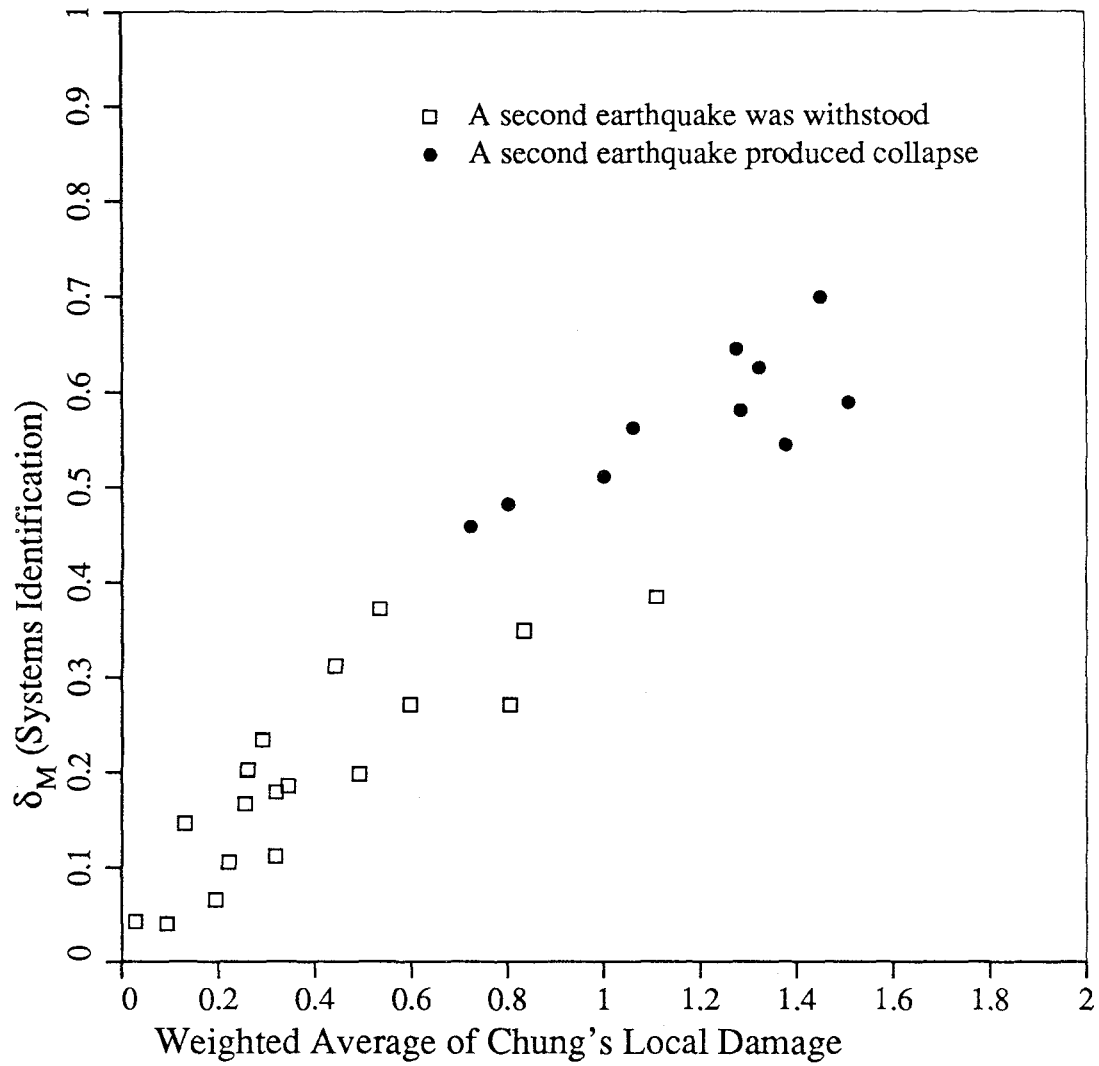
Figure 5-7 indicates that the value of the energy average of the modified Park and Ang's index is about 70% of the value of the Maximum Softening. The structures that collapse in the second occurrence of the same earthquake have an energy average of the modified Park and Ang's index of between 0.25 and 0.55. The correlation between the two indices is good, considering that they come from completely different definitions. However, the Maximum Softening provides more information about whether or not a structure will collapse during a second identical earthquake.

### **5.3.2 Energy Average of the Chung, Meyer and Shinozuka's Index**

Figure 5-8 shows the relationship between the energy average of Chung, Meyer and Shinozuka's index, defined by Equation (2.7), and the Maximum Softening. This definition of the global damage was not proposed by Chung *et al.*, but has been used here because it is similar to the definition of global damage by Park *et al.*

One can see in figure 5-8 how the correlation between the energy average of Chung, Meyer and Shinozuka's index, and the Maximum Softening is very poor.

The value of the energy average of Chung, Meyer and Shinozuka's index is unable to predict whether the structure would collapse or not during a second identical earthquake. It is not possible to draw a straight vertical line separating filled circles and squares, but is clearly possible to draw a horizontal line as shown before.



**FIGURE 5-9 Maximum Softening vs. Chung's Weighted Average**

### 5.3.3 Weighted Average of Chung, Meyer and Shinozuka's Story Index

Figure 5-9 shows the relationship between the weighted average of Chung, Meyer and Shinozuka's story index, using the triangular weighting function defined by Equation (2.8), and the Maximum Softening. This was the original definition of global damage as proposed by Chung *et al.* [7]. The correlation with the Maximum Softening is much better than in the previous case.

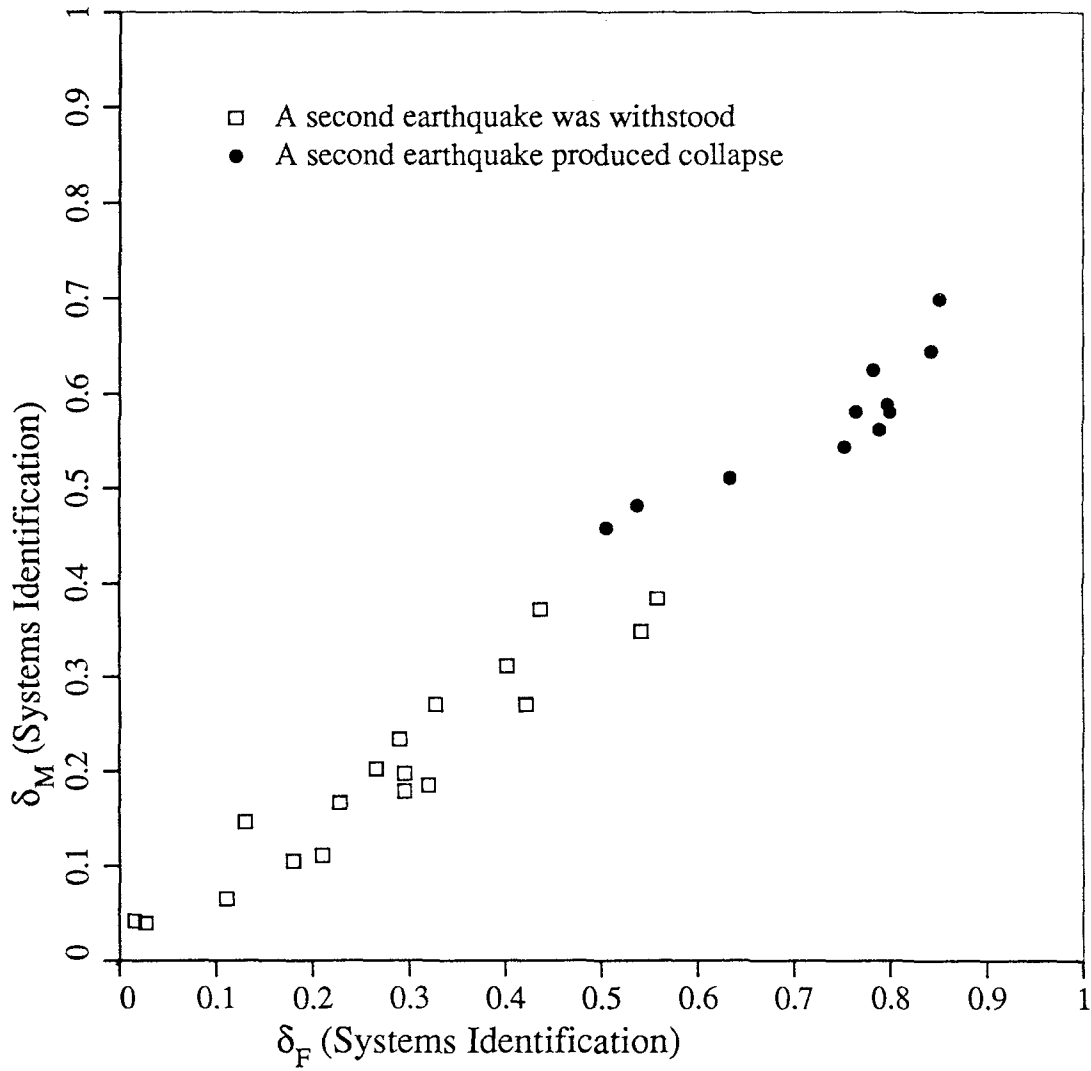
The value of the Maximum Softening is about 45% of the value of the weighted average of Chung, Meyer and Shinozuka's story damage index. Thus, a value of the weighted average of Chung's story index of 1.0 corresponds approximately to a Maximum Softening of 0.45.

The Maximum Softening is still a better predictor of the collapse on the second run.

### 5.4 Maximum Softening vs. Final Softening

The Final Softening has been shown to be approximately equal to a weighted average of the local damage when the mode shape does not change significantly after damage [11]. It is related to the global stiffness degradation. When the initial natural period is known, the Final Softening can be computed from the results of post-earthquake vibration testing.

Figure 5-10 suggests that the Final Softening, defined by Equation (2.11) could be used as a global damage index equivalent to the Maximum Softening. However, it should be noted that the Final Softening only includes information about the strength degradation, whereas the Maximum Softening also gives information about the plastic deformations. In figure 5-10 there are four points with a very similar Final Softening value of between 0.5 and 0.6. For these four earthquake runs, the amount of stiffness degradation was similar, but the value of the Maximum Softening indicates that two of those cases underwent greater plastic deformations. Precisely these two cases collapsed during the second



**FIGURE 5-10 Maximum Softening vs. Final Softening**

occurrence of the same earthquake. The Maximum Softening is then a more complete damage indicator.

The correlation between the Maximum Softening and the Final Softening for the database analyzed is quite good. For practical purposes it can be said that the Final Softening has a value 30% greater than the Maximum Softening. A Maximum Softening value of 0.45 corresponds approximately to a Final Softening value of 0.59.

The evolution of the Final Softening could also be used for the characterization of the state of aging structures.





## SECTION 6

### CONCLUSIONS

#### 6.1 Conclusions

The response of three code-designed building frames subjected to a set of artificially generated and recorded earthquakes has been obtained by using the computer code SARCF-III. Several damage indices and *traditional measures of damage* have been computed. The traditional measures of seismic damage and several local and global damage indices, have been evaluated and compared. Their relationship and correlation have been studied.

A new way of computing the global damage indices defined by DiPasquale and Cakmak [10] from a moving average of the instantaneous natural period is presented. An averaging window with a length equal to two or two and a half times the initial natural period has been found to yield results consistent with the original way of computing those indices.

Two local damage indices have been used: Chung, Meyer and Shinozuka's index and a modified Park and Ang's index. Two groups of global indices have been considered: global damage indices based on the vibrational parameters and weighted averages of the local damage indices. The *traditional measures of damage* included in this study are the maximum interstory drift, the permanent interstory drift and the maximum ductility ratio for beams and columns.

The computer program SARCF-III used to simulate the seismic response of the building frames has been improved in order to carry out this research. The computed results have been compared to the experimental results of tests done on a reinforced concrete model tested at the University of Illinois at Urbana-Champaign (UIUC) by Sozen and his associates [5]. SARCF-III has also been compared to a similar program, IDARC,

developed at State University of New York at Buffalo by Y. J. Park *et al.* [18]. Considering the uncertainties that exist in the description of the nonlinear behavior of reinforced concrete structures, a good approximation to the experimental results was obtained by using the program SARCF-III. The response of structures clearly in the nonlinear range is predicted with a higher degree of accuracy than that of structures that start to develop plasticity.

The analysis of the results of the numerical simulations that have been performed yield the following conclusions:

1. The Maximum and Final Softening can be computed by using the systems identification program, MUMOID [9], or by computing a moving average of the instantaneous natural period, thus obtaining results that are equivalent from a practical point of view.
2. The *traditional measures of damage* depend on the structural configuration. They have to be calibrated for each case. For the studied cases, the Maximum Softening predicts the structural capacity for future earthquakes more consistently than any of the *traditional measures of damage* that have herein been considered. The Maximum Softening presents a better correlation with the maximum interstory drift and with the maximum ductility ratio for beams, than with the maximum permanent drift and the maximum ductility ratio for columns.
3. For this set of numerical simulations the Maximum Softening is a more robust global damage index than the weighted averages of the local damage indices included in this report. It consistently predicts the structural capacity for future earthquakes. Local damage indices give important information at the local level, but in order to obtain a global damage index, an appropriate weighting function has to be defined. The Maximum Softening avoids the definition of a weighting function.

4. The correlation of the Maximum Softening with the energy average of the modified Park's index is good. The correlation of the Maximum Softening with the weighted average of Chung's index is only good when using a triangular shape with the maximum at the base as the weighting function for the story damage indices.
5. The Final Softening gives a less reliable indication of the global damage than does the Maximum Softening, but nevertheless its indication is equivalent to the *traditional measures of damage* and to the weighted averages of the local damage indices.

## 6.2 Suggestions for Future Research

This report provides new information about the correlation between various damage indices and the damage level derived from a set of numerical simulations of the seismic response of reinforced concrete frames. The number of structures and earthquake ground motions used in this study only allows one to draw qualitative conclusions. Statistically more meaningful results could be obtained by performing more simulations with new structural configurations. New definitions of damage indices could also be included in a more extensive evaluation.

The same procedure could be applied to other aspects of the seismic design of structures in order to take advantage of the available computer codes to shed more light on the seismic behavior of structures. Computer models are more economical than reduced scale models of a structure and allow for more flexibility. Examples of possible applications are: the study of the relationship between the type of earthquake, i.e. frequency content, magnitude, distance, etc, and the resulting damage, or the study of the cumulative damage caused by a series of seismic events during the life of a structure.

In order to pursue this approach, more accurate computer models are necessary. More research is required in the three-dimensional modeling of reinforced concrete elements.

The interaction between all the internal forces and the hysteretic behavior should be considered and nonstructural elements should be modeled.

The Maximum Softening has proven to be a robust global damage index for the studied cases, but it would be useful to check its performance in cases for which the soil-structure interaction is significant or when three-dimensional effects cannot be neglected. The applicability of the Maximum Softening to steel structures or to other structural configurations such as bridges, could also be investigated.

## SECTION 7

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